

4. 72 note books weigh 8 kg
 1 " " $\frac{8}{72}$ kg
 8 " " $\frac{8}{72} \times 9$ kg
 9 kg
 8 kg of weight is of 72 note books
 1 kg " " $\frac{72}{8}$ note books
 6 " " $\frac{72}{8} \times 6$ Note books
 54 Note books
5. A worker paid ₹ 1110 for 6 days working
 " " ₹ 1 " $\frac{6}{1110}$ " "
 " " ₹ 4625 " $\frac{6}{1110}$ 4625 working
 A worker paid ₹ 4625 for 25 days of working.
6. For 900 km travelling cost ₹ 280
 " 1 " " ₹ $\frac{280}{900}$
 " 360 " " ₹ $\frac{280}{900} \times 360$
 " " " " ₹ 112
7. A train covers 51 km in 45 minutes
 " " 1 " " $\frac{45}{51}$ minutes
 " " 221 km " $\frac{45}{51}$ 221 minutes
 " " 221 km " 195 minutes
 or 3 hr 24 minutes
8. 162 gm weight is of 6 sheets
 1 gm " " $\frac{6}{162}$ sheets
 13500 " " $\frac{6}{162}$ 13500 sheets
 or 13.5kg " 500 sheets
9. (i) In 15 months clerk earns ₹ 18000
 In 1 " " ₹ $\frac{18000}{15}$
 " 7 " " $\frac{18000}{15} \times 7$
 " " " = ₹ 8400

- (ii) ₹ 1800 is earned by a clerk in 15 months
 " " " $\frac{15}{18000}$ months
 ₹ 30000 " $\frac{15}{18000} \times 30000$ months
 25 Months
10. 25 bags of rice weighing 40kg cost ₹ 7750
 1 " " " 40 kg " ₹ $\frac{7750}{25}$
 " " " 1 kg ₹ $\frac{7750}{25 \times 40}$
 36 " " " 50 kg ₹ $\frac{7750}{25} \times \frac{36}{40}$
 36 bags for rice weighing 40kg cost ₹ 13950
11. Price of 3 Pencils or 5 rubbes ₹ 15
 " " 1 pencils or 5 rubbers ₹ $\frac{15}{3}$
 " " " 1 rubber $\frac{15}{3 \times 5}$
 " 4 " 3 rubber $\frac{15}{3 \times 5} \times 4 \times 3$
 Price of 4 Pencils or 3 rubbers ₹ 12
12. Working 8 hours/days worked completed in 12 days
 " " 1 " " 12 8 days
 " " 6 " " $\frac{12 \times 8}{6}$ days
 " " " " in 16 days
13. For 1152 bars of soap cartons needed 8
 " " " $\frac{8}{1152}$
 " 3888 " $\frac{8}{1152} \times 3888$
 27
14. 44m thickness is of 16 cardboard
 1 " " " $\frac{16}{44}$ "
 715 mm " " $\frac{16}{44} \times 715$ cardboard
 71.5 cm " " 260 cardboard

15. 16.25m of wall built by 15 men

$$1 \text{ " " " } \frac{15}{16.25} \text{ men}$$

$$26 \text{ " " " } \frac{15 \times 26}{16.25} \text{ men}$$

$$\frac{390}{16.25} \text{ men}$$

26 metres of wall built by 24 men

6

Percentage and Its Applications

Exercise-6.1

1. (i) $32\% = \frac{32}{100} = \frac{8}{25}$
- (ii) $26\frac{2}{3}\% = \frac{80}{3}\%$, $\frac{80}{300} = \frac{8}{30} = \frac{4}{15}$
- (iii) $6\frac{1}{4}\% = \frac{25}{4}\%$, $\frac{25}{100} = \frac{1}{4}$
- (iv) $0.5\% = \frac{0.5}{100} = \frac{5}{1000} = \frac{1}{200}$
- (v) $1.25\% = \frac{1.25}{100} = \frac{125}{10000} = \frac{1}{80}$
- (vi) $120\% = \frac{120}{100} = \frac{12}{10} = \frac{6}{5}$
- (vii) $0.75\% = \frac{0.75}{100} = \frac{75}{10000} = \frac{3}{400}$
- (viii) $0.05\% = \frac{5}{100}\%$, $\frac{1}{2000}$
2. (i) $\frac{53}{100} = \frac{53}{100}$, 100% , 53%
- (ii) $\frac{3}{8} = \frac{3}{8} \times \frac{25}{25} = \frac{75}{200}$, $\frac{3}{2} = \frac{75}{50}$, $\frac{75}{2}\%$
- (iii) $\frac{5}{7} = \frac{5}{7} \times 100\% = \frac{500}{7}\%$, $71\frac{3}{7}\%$
- (iv) $\frac{23}{40} = \frac{23}{40} \times 100\% = \frac{23 \times 10}{4} = \frac{230}{4}\%$, $57\frac{1}{2}\%$
- (v) $\frac{7}{20} = \frac{7}{20} \times 100\% = (7 \times 5)\% = 35\%$
- (vi) $\frac{19}{500} = \frac{19}{500} \times 100\% = \frac{19}{5}\%$, $3\frac{4}{5}\%$
- (vii) $1\frac{3}{5} = \frac{8}{5}$, $\frac{8}{5} \times 100\% = 160\%$

$$(viii) 1\frac{7}{8} = \frac{15}{8} = \frac{15}{8} \times \frac{25}{25} = \frac{375}{200} = 187\frac{1}{2}\%$$

3. (i) $26\% = \frac{26}{100} = \frac{13}{50}$, $13:50$
- (ii) $13\frac{3}{4}\% = \frac{55}{4}\%$, $\frac{55}{4} = \frac{55}{4} \times \frac{1}{100} = \frac{11}{80}$, $11:80$
- (iii) $135\% = \frac{135}{100} = \frac{27}{20}$, $27:20$
- (iv) $5.5\% = \frac{5.5}{100} = \frac{55}{1000} = \frac{11}{200}$, $11:200$
- (v) $2.5\% = \frac{2.5}{100} = \frac{25}{10000} = \frac{1}{400}$, $1:400$
- (vi) $0.4\% = \frac{0.4}{100} = \frac{4}{10000} = \frac{1}{2500}$, $1:2500$
- (vii) $0.65\% = \frac{0.65}{100} = \frac{65}{10000} = \frac{13}{2000}$, $13:2000$
- (viii) $22\% = \frac{22}{100} = \frac{11}{50}$, $11:50$
4. (i) $3:5 = \frac{3}{5} = \frac{3}{5} \times \frac{20}{20} = \frac{60}{100} = 60\%$
- (ii) $2:3 = \frac{2}{3} = \frac{2}{3} \times 100\% = \frac{200}{3}\%$, $66\frac{2}{3}\%$
- (iii) $36:75 = \frac{36}{75} = \frac{36}{75} \times \frac{4}{4} = \frac{144}{300} = 48\%$
- (iv) $1:35 = \frac{1}{35} = \frac{1}{35} \times 100\% = \frac{20}{7}\%$, $2\frac{6}{7}\%$
- (v) $11:125 = \frac{11}{125} = \frac{11}{125} \times 100\% = 8.8\%$

$$\frac{11}{5} \times \frac{4}{100} = \frac{44}{5} \% = 8\frac{4}{5} \%$$

(vi) $7:5 = \frac{7}{5} \times 100\% = 140\%$

(vii) $1:2 = \frac{1}{2} \times 100\% = 50\%$

(viii) $15:8 = \frac{15}{8} \times 100\% = 187\frac{1}{2} \%$

5. (i) $75\% = \frac{75}{100} = 0.75$

(ii) $7\% = \frac{7}{100} = 0.07$

(iii) $7.5\% = \frac{7.5}{100} = 0.075$

(iv) $13\frac{1}{2}\% = 13.5\% = \frac{13.5}{100} = 0.135$

(v) $0.2\% = \frac{0.2}{100} = 0.002$

(vi) $1\% = \frac{1}{100} = 0.01$

(vii) $0.05 = \frac{0.05}{100} = 0.0005$

(viii) $\frac{1}{4}\% = 0.25\% = \frac{0.25}{100} = 0.0025$

6. (i) $0.4 = 0.4 \times 100\% = 40\%$

(ii) $0.24 = 0.24 \times 100\% = 24\%$

(iii) $0.02 = 0.02 \times 100\% = 2\%$

(iv) $0.275 = 0.275 \times 100\% = 27.5\%$

(v) $0.063 = 0.063 \times 100\% = 6.3\%$

(vi) $1.2 = 1.2 \times 100\% = 120\%$

(vii) $2.05 = 2.05 \times 100\% = 205\%$

(viii) $0.002 = 0.002 \times 100\% = 0.2\%$

Exercise-6.2

1. (i) We have to find 70% of 500

$$\frac{70}{100} \times 500 = 350$$

(ii) $3\frac{1}{2}\%$ of 1600

$$\frac{7}{2}\% \text{ of } 1600$$

$$\frac{7}{2} \times \frac{1600}{100} = 7 \times 8 = 56$$

(iii) 20% of ₹ 150 = ₹ $\frac{20}{100} \times 150$ = ₹ 30

(iv) 90% of 130 = $\frac{90}{100} \times 130$ = 117

(v) 60% of 55 = $\frac{60}{100} \times 55$

$$= \frac{3}{2} \times \frac{11}{2} = \frac{33}{2}$$

(vi) $2\frac{1}{2}\%$ of 30 = $\frac{5}{2}\%$ of 30

$$= \frac{5}{2} \times \frac{30}{100}$$

$$= \frac{3}{4} = 0.75$$

$$2\frac{1}{2}\% \text{ of } 30 = 0.75$$

(vii) 15.5% of ₹ 3000 = ₹ $\frac{15.5}{100} \times 3000$

$$= \frac{15.5}{100} \times 3000 = ₹ 465$$

$$15.5\% \text{ of } ₹ 3000 = ₹ 465$$

(viii) 75% of 2kg = $\frac{75}{100} \times 2000$ gm

$$= 1500 \text{ gm}$$

$$75\% \text{ of } 2 \text{ kg} = 1.5 \text{ kg}$$

(ix) 32% of 1.5 lit

$$\frac{32}{100} \times 1.5 = 100 \text{ ml}$$

$$= \frac{32}{100} \times 1.5 = 10 \text{ ml}$$

$$= 480 \text{ ml}$$

$$32\% \text{ of } 1.5 \text{ lit} = 480 \text{ ml}$$

(x) 40% of $1\frac{1}{2}$ hours

$$\frac{40}{100} \times 90 \text{ minutes}$$

$$= 36 \text{ minutes}$$

$$40\% \text{ of } 1\frac{1}{2} \text{ hours} = 36 \text{ minutes}$$

(xi) $10\frac{1}{2}\%$ of 12m = 10.5% of 12km

$$\frac{10.5}{100} \times 12000 \text{ m}$$

$$= 1260 \text{ m}$$

$$10\frac{1}{2}\% \text{ of } 12 \text{ km} = 1.260 \text{ km}$$

$$(xii) \quad 250\% \text{ of ₹ } 18 = ₹ \frac{250}{100} \times 18$$

$$= ₹ 45$$

2. (i) Let $x\%$ of 32 = 80

$$\frac{x}{100} \times 32 = 80$$

$$x = \frac{80 \times 100}{32}$$

$$= \frac{8000}{32}$$

$$x = 250\%$$

$$250\% \text{ of } 32 = 80$$

(ii) Let $x\%$ of ₹ 215 = ₹ 750

$$\frac{x}{100} \times 125 = 750$$

$$x = \frac{750 \times 100}{125}$$

$$x = 600\%$$

$$600\% \text{ of ₹ } 125 = ₹ 750$$

(iii) Let $x\%$ of $3\frac{1}{2}$ kg = 25 kg

$$\frac{x}{100} \times 3\frac{1}{2} = 25$$

$$\frac{x}{100} \times \frac{7}{2} = 25$$

$$x = \frac{25 \times 100 \times 2}{7}$$

$$x = \frac{500}{7}$$

$$x = 714\frac{2}{7}\%$$

$$714\frac{2}{7}\% \text{ of } 3\frac{1}{2} \text{ kg} = 25 \text{ kg}$$

(iv) Let $x\%$ of 420g = 2.25 kg

$$\frac{x}{100} \times 420 = 2250$$

$$x = \frac{2250 \times 100}{420}\%$$

$$x = 535.75\%$$

$$535.75\% \text{ of } 420 \text{g} = 2.25 \text{ kg}$$

(v) Let $x\%$ of 1.5km = 360m

$$\frac{x}{100} \times 1500 \text{m} = 360 \text{m}$$

$$x = \frac{360 \times 100}{1500}$$

$$x = 24$$

$$24\% \text{ of } 1.5 \text{ km} = 360 \text{ m}$$

(vi) Let $x\%$ of 8 hours = 3 days

$$\frac{x}{100} \times 8 \text{ hours} = 72 \text{ hours}$$

$$x = \frac{72 \times 100}{8}$$

$$x = 900$$

$$900\% \text{ of } 8 \text{ hours} = 3 \text{ days}$$

3. (i) Reduction ₹ 40 ₹ 232 ₹ 8

$$\text{Reduction \%} = \frac{\text{Reduction}}{\text{original}} \times 100$$

$$= \frac{40}{232} \times 100 = 17.24\%$$

(ii) Reduction (6 5.4)kg

$$\text{Reduction \%} = \frac{\text{Reduction}}{\text{Original}} \times 100$$

$$= \frac{0.6}{6} \times 100 = 10\%$$

$$\text{Reduction \%} = 10\%$$

(iii) Reduction (12 10) hours

$$\text{Reduction \%} = \frac{\text{Reduction}}{\text{Original}} \times 100$$

$$= \frac{2}{12} \times \frac{100}{10} = \frac{50}{3} = 16\frac{2}{3}\%$$

$$= 16\frac{2}{3}\%$$

4. (i) Increase (12 10) months

$$2 \text{ months}$$

$$\text{Increase \%} = \frac{\text{Increase}}{\text{Original}} \times 100$$

$$= \frac{2}{10} \times 100 = 20\%$$

$$\text{Increase \%} = 20\%$$

(ii) Increase ₹ (50 40) ₹ 10

$$\text{Increase \%} = \frac{\text{Increase}}{\text{Original}} \times 100$$

$$= \frac{10}{40} \times 100 = 25\%$$

$$\text{Increase \%} = 25\%$$

(iii) Increase (81 72) 9 Marks

$$\text{Increase \%} = \frac{\text{Increase}}{\text{Original}} \times 100$$

$$\frac{9}{72} \times 100 = \frac{100}{8} \times \frac{25}{2} = 12\frac{1}{2}\%$$

Increase % $12\frac{1}{2}\%$

5. % of marks secured by Sandhya

$$\frac{630}{900} \times 100 = 70\%$$

% of Marks secured by Monika

$$\frac{650}{1300} \times 100 = 50\%$$

Performance of Sandhya is better.

6. % of books sold

$$\frac{\text{Sold books}}{\text{total}} \times 100 = \frac{2640}{12000} \times 100$$

books sold 22%

7. Let students appeared in exams x

students passed 95%

" " failed $(100 - 95)\%$

5% of x 60

$$\frac{5}{100} \times x = 60$$

$$x = \frac{60 \times 100}{5}$$

x 1200

1200 students appeared in exams

8. Let Mohan have ₹ x

10% of x ₹ 15

$$\frac{10x}{100} = 15$$

$$x = \frac{5 \times 100}{10}$$

x ₹ 150

Mohan have ₹ 150 before he purchased pencil box.

9. Reduction in price of Jam 70 56

₹ 14

reuction % $\frac{\text{reduction}}{\text{original}} \times 100$

$$\frac{14}{70} \times 100 = 20\%$$

reduction % 20%

10. Let number x

x 10% of x

x 10% of x 55

$$x - \frac{10x}{100} = 55$$

$$x - \frac{x}{10} = 55$$

$$\frac{10x - x}{10} = 55$$

$$\frac{9x}{10} = 55$$

$$x = \frac{55 \times 10}{9}$$

x 50

Number is 50

11. Let number x

x $\frac{8x}{100}$ 115

$$\frac{100x - 8x}{100} = 115$$

$$\frac{92x}{100} = 115$$

$$x = \frac{115 \times 100}{92}$$

x 125

Number is 125

12. Let original salary x

x 15% of x 9200

$$x - \frac{15x}{100} = 9200$$

$$\frac{100x - 15x}{100} = 9200$$

$$\frac{85x}{100} = 9200$$

$$x = \frac{9200 \times 100}{85}$$

x ₹ 8000

original salary of siddarth ₹ 8000

13. Marks got in maths 80% of 150

$$\frac{80}{100} \times 150$$

Marks in maths 120

Marks got in English

70% of marks in Maths

70% of 120

$$\frac{70}{100} \times 120 = 84$$

Marks got in Hindi

$$\frac{75}{100} \times 84 = 63$$

Marks in Maths 120
 Marks in English 84
 Marks in Hindi 63

14. % of male workers
 (100 - 25)% = 75%

Let total workers be x

$$\frac{75}{100} \times x = 360$$

$$x = \frac{360 \times 100}{75} = 480$$

Total workers in factory 480

15. Donated to trust 15% of 1,20,000

$$\frac{15}{100} \times 1,20,000 = ₹ 18,000$$

Amount donated to trust ₹ 18,000
 remaining amount 1,20,000 - 18,000 = 1,02,000

Amount received by her each daughter and son

$$\frac{102000}{3}$$

$$₹ 34000$$

16. Ram obtained 91% of 600

$$\frac{91}{100} \times 600 = 546$$

546 marks

to get 94% Ram should obtain 94% of 600

$$\frac{94}{100} \times 600 = 564$$

Ram should get (564 - 546) = 18 more marks

17. Decrease in the price of computer

$$\frac{55000 - 52800}{55000} \times 100 = \frac{2200}{55000} \times 100 = 4\%$$

$$\text{Decrease \%} = \frac{\text{Decrease}}{\text{original}} \times 100 = \frac{2200}{55000} \times 100 = 4\%$$

18. Present cost of article ₹ 60

cost after 1 year 60 - 5% of 60 = 60 - 3 = 57

Cost after 1 year ₹ 57

Cost particle after 2nd year 57 - 5% of 57 = 57 - 3.15 = 53.85

$$57 - \frac{5}{100} \times 57 = 53.85$$

$$57 - \frac{3.15}{100} \times 57 = 53.85$$

$$53.85 - \frac{3.15}{100} \times 53.85 = 51.5$$

Cost of particle after 2 years 51.5

19. Let population 1 year ago x

$$x - 10\% \text{ of } x = 2,04,600$$

$$x - \frac{10x}{100} = 2,04,600$$

$$x - \frac{x}{10} = 2,04,600$$

$$\frac{10x - x}{10} = 2,04,600$$

$$\frac{9x}{10} = 2,04,600$$

$$x = \frac{2,04,600 \times 10}{9} = 2,27,333.33$$

$$x = 2,27,333$$

population 1 year ago 2,27,333

20. Let cost of petrol ₹ 100

Now price of petrol

$$₹ 100 - 20\% \text{ of } 100 = ₹ 80$$

$$₹ (100 - 20) = ₹ 80$$

Reduction on needed 120 - 100 = 20

$$\text{Reduction \% needed} = \frac{20}{120} \times 100 = 16\frac{2}{3}\%$$

$$\frac{100}{6}$$

$$\frac{50}{3} = 16\frac{2}{3}\%$$

Exercise-6.3

1. (i) We have, CP ₹ 200, SP ₹ 224

$$\begin{array}{r}
 P \quad SP \quad CP \\
 \quad 224 \quad 200 \quad 24 \\
 P \% \quad \frac{P}{CP} \quad 100 \\
 \quad \frac{24}{200} \quad 100 \\
 P \% \quad 12\%
 \end{array}$$

- (ii) We have, CP ₹ 450, SP ₹ 400

$$\begin{array}{r}
 \text{loss} \quad CP \quad SP \\
 \quad 450 \quad 400 \quad 50 \\
 l \% \quad \frac{l}{CP} \quad 100 \\
 \quad \frac{50}{450} \quad 100 \\
 \text{loss \%} \quad 11\frac{1}{9}\%
 \end{array}$$

- (iii) We have, CP ₹ 550, gain ₹ 22

$$\begin{array}{r}
 \text{gain \%} \quad \frac{g}{CP} \quad 100 \quad \frac{22}{550} \quad 100 \\
 \text{gain \%} \quad 4\%
 \end{array}$$

- (iv) We have, CP ₹ 216, loss ₹ 72

$$\begin{array}{r}
 l \% \quad \frac{l}{CP} \quad 100 \\
 \quad \frac{72}{216} \quad 100 \\
 l \% \quad 33\frac{1}{3}\%
 \end{array}$$

- (v) We have, SP ₹ 500, loss ₹ 100

$$\begin{array}{r}
 CP \quad SP \quad \text{loss} \\
 500 \quad 100 \\
 ₹ 600 \\
 \text{loss \%} \quad \frac{l}{CP} \quad 100 \\
 \quad \frac{100}{600} \quad 100 \\
 \text{loss \%} \quad 16\frac{2}{3}\%
 \end{array}$$

- (vi) We have, SP ₹ 12, profit ₹ 4

$$\begin{array}{r}
 CP \quad SP \quad \text{Profit} \\
 12 \quad 4 \\
 CP \quad ₹ 8 \\
 \text{Profit \%} \quad \frac{P}{CP} \quad 100 \\
 \quad \frac{4}{8} \quad 100 \\
 \text{profit} \quad 50\%
 \end{array}$$

2. (i) We have, CP ₹ 500, gain 25%

$$\begin{array}{r}
 SP \quad \frac{100 \quad g \%}{100} \quad CP \\
 \quad \frac{100 \quad 25}{100} \quad 500 \\
 \quad \frac{125}{100} \quad 500 \\
 SP \quad ₹ 625
 \end{array}$$

- (ii) We have, CP ₹ 60, loss $12\frac{1}{2}\%$

$$\begin{array}{r}
 \therefore SP \quad \frac{100 \quad l \%}{100} \quad CP \\
 \quad \frac{100 \quad 12.5}{100} \quad 60 \\
 \quad \frac{87.5}{100} \quad 60 \\
 SP \quad ₹ 52.5
 \end{array}$$

- (iii) We have, CP ₹ 150, loss 20%

$$\begin{array}{r}
 \therefore SP \quad \frac{100 \quad l \%}{100} \quad CP \\
 \quad \frac{100 \quad 20}{100} \quad 150 \\
 \quad \frac{80}{100} \quad 150 \\
 SP \quad ₹ 120
 \end{array}$$

- (iv) We have, CP ₹ 80, gain 2.5%

$$\begin{array}{r}
 \therefore SP \quad \frac{100 \quad g \%}{100} \quad CP \\
 \quad \frac{100 \quad 2.5}{100} \quad 80 \\
 \quad \frac{10.25}{100} \quad 80 \\
 \quad \frac{8200}{100} \\
 SP \quad ₹ 82
 \end{array}$$

3. (i) We have, SP ₹ 924, gain 10%

$$\begin{array}{r}
 \therefore CP \quad \frac{SP \quad 100}{100 \quad g \%} \\
 \quad \frac{924 \quad 100}{100 \quad 10} \\
 \quad \frac{92400}{100} \\
 CP \quad ₹ 840
 \end{array}$$

(ii) We have, $SP = ₹ 1755$, gain 12.5%

$$CP = \frac{SP}{100 + g\%} = \frac{1755}{100 + 12.5} = \frac{175500}{112.5} = ₹ 1560$$

(iii) We have, $SP = ₹ 851$, loss 8%

$$\therefore CP = \frac{SP}{100 - l\%} = \frac{851}{100 - 8} = \frac{85100}{92} = ₹ 925$$

(iv) We have, $SP = ₹ 560$, $l = 6\frac{2}{3}\%$

$$\frac{20}{3}\% \therefore CP = \frac{SP}{100 - l\%} = \frac{560}{100 - \frac{20}{3}} = \frac{56000}{\frac{300 - 20}{3}} = \frac{56000 \times 3}{280} = ₹ 600$$

4. CP of tricycle $₹ 560$

SP of tricycle $₹ 630$

gain on " " $₹ (630 - 560) = ₹ 70$

$$g\% \text{ on tricycle} = \frac{g}{CP} \times 100 = \frac{70}{560} \times 100 = \frac{8}{25} \times 100 = 12\frac{1}{2}\%$$

5. CP of an article $₹ 400$

SP " " $₹ 336$

loss on " " $₹ (400 - 336) = ₹ 64$

$$\text{loss\% on article} = \frac{\text{loss}}{CP} \times 100$$

$$\frac{64}{400} \times 100$$

loss on article 16%

6. Total CP of Radio $₹ (5863 - 137)$

$₹ 6000$

SP of Radio $₹ 5700$

loss on Radio $6000 - 5700$

$₹ 300$

$$\text{loss\% on Radio} = \frac{300}{6000} \times 100 = 5\%$$

7. Let CP of 6 toffees 1

$$\text{CP of 1 toffee} = \frac{1}{6}$$

$$\text{SP of 4 toffees} = 1$$

$$\text{SP of 1 toffee} = \frac{1}{4}$$

gain $\frac{SP - CP}{CP} \times 100$

$$\frac{1}{4} - \frac{1}{6}$$

$$\frac{3 - 2}{12} = \frac{1}{12}$$

$$\text{gain\%} = \frac{g}{CP} \times 100 = \frac{1}{12} \times 100 = 8\frac{1}{3}\%$$

$$\frac{1}{12} \times 100$$

$$\frac{1}{6} \times 100$$

$$\frac{1}{2} \times 100$$

$$\frac{1}{2} \times 100 = 50\%$$

8. Let SP of 20 pens 1

$$\text{" " 1 pen} = \frac{1}{20}$$

$$\text{CP of 15 pens} = 1$$

$$\text{" " 1 pen} = \frac{1}{15}$$

loss $\frac{CP - SP}{CP} \times 100$

$$\frac{1}{15} - \frac{1}{20}$$

$$\frac{4 - 3}{60} = \frac{1}{60}$$

$$\text{loss} = \frac{1}{60} \times 100 = 1\frac{2}{3}\%$$

$$\text{loss \%} = \frac{\frac{1}{60}}{\frac{1}{15}} \times 100$$

$$= \frac{1}{60} \times \frac{15}{1} \times 100$$

$$\text{loss \%} = 25\%$$

9. CP of 8 toffees ₹ 1

$$\text{" 1 " } \frac{1}{8}$$

Now SP of 6 toffees ₹ 1

$$\text{" " 1 toffee } \frac{1}{6}$$

$$\text{Profit } \frac{SP}{CP} = \frac{1}{\frac{1}{6}} = 6$$

$$\text{Profit } \frac{1}{24}$$

$$\text{Profit \%} = \frac{P}{CP} \times 100$$

$$= \frac{1}{\frac{24}{1}} \times 100$$

$$\text{Profit \%} = \frac{1}{24} \times \frac{8}{1} \times 100$$

$$\text{Profit \%} = 33\frac{1}{3}\%$$

10. Total CP of Almirah ₹ (2465 + 35)

$$= ₹ 2500$$

$$\text{gain \%} = 16\%$$

$$\text{SP of Almirah} = \frac{100 + 16}{100} \times 2500$$

$$\therefore SP = \frac{100 + g\%}{100} \times CP$$

$$= \frac{116}{100} \times 2500$$

$$\text{SP of Almirah} = ₹ 2900$$

11. We have SP of rickshaw ₹ 2640

$$\text{CP of rickshaw} = \frac{\text{loss } 12\%}{\frac{2640}{100 - 12}}$$

$$\therefore CP = \frac{SP}{100 - l\%} \times 100$$

$$= \frac{264000}{88} = ₹ 3000$$

Now to get 12% gain

$$SP = \frac{100 + g\%}{100} \times CP$$

$$= \frac{100 + 12}{100} \times 3000$$

$$= 112 \times 30$$

$$\text{SP of rickshaw} = ₹ 3360$$

to get 12%

12. Let CP = x, SP = ₹ 322

$$\text{gain \%} = \frac{x}{6}$$

$$g\% = \frac{g}{CP} \times 100$$

$$= \frac{x}{6} \times 100$$

$$= \frac{x}{6} \times \frac{50}{3}$$

$$g\% = 16\frac{2}{3}\%$$

13. CP of 100 bats 100 × 40

$$= ₹ 4000$$

$$\text{SP of 100 bats} = \frac{100 + 20}{100} \times 4000$$

$$= \frac{120}{100} \times 4000 = ₹ 48000$$

Now CP of 20 bats 20 × 40 = ₹ 800

SP of 20 bats at 5% gain

$$= \frac{100 + 5}{100} \times 800$$

$$= 105 \times 8 = ₹ 840$$

$$\text{SP of remaining 80 bats} = 480$$

$$- 840$$

$$\hline ₹ 3960$$

$$\text{CP of remaining 80 bats} = 80 \times 40$$

$$= ₹ 3200$$

$$\text{Profit on 80 bats} = 3960 - 3200$$

$$= 760$$

$$\text{Profit \% on Remaining} = \frac{\text{Profit}}{CP} \times 100$$

$$\frac{760}{3200} \times 100$$

$$23.75\%$$

14. SP of 1st radio ₹ 924

$$\text{CP of 1st radio } ₹ \frac{924}{100} \times 100$$

$$\frac{92400}{120} ₹ 770$$

$$\text{SP of IInd radio } ₹ 924$$

$$\text{CP of IInd radio } \frac{924}{100} \times 100$$

$$\frac{92400}{80}$$

$$₹ 1155$$

$$\text{TCP } 1155 \quad 770$$

$$₹ 1925$$

$$\text{TSP } ₹ 1848$$

$$\text{loss } 1925 \quad 1848$$

$$77$$

$$\text{loss \% } \frac{77}{1925} \times 100$$

$$\frac{77000}{1925}$$

$$\text{loss in whole transaction } 4\%$$

15. Let Ram Gopal purchased x kg of each tea

$$\text{CP of both types of tea}$$

$$9x \quad 7x$$

$$9x \quad 7x$$

$$16x$$

$$\text{S.P. of both types of tea } 2x \quad 8 \quad 16x$$

$$\text{Profit " } 16x \quad 16x$$

$$0$$

No profit no loss.

16. Let C.P. ₹ 32,000,

$$\text{loss } \frac{1}{8} \times 32000 = 4000$$

$$\text{loss \% } \frac{l}{\text{C.P.}} \times 100$$

$$\frac{4000}{32000} \times 100$$

$$12.5\%$$

$$\text{and S.P. } 32000 \quad 4000$$

$$₹ 28000$$

17. C.P. of 11 pencils ₹ 10

$$\text{C.P. of 1 Pencil } ₹ \frac{10}{11}$$

Now S.P. of 10 pencils ₹ 11

$$\text{" " 1 Pencil } ₹ \frac{11}{10}$$

Profit S.P. – C.P.

$$\frac{11}{10} - \frac{10}{11}$$

$$\frac{121}{110} - \frac{100}{110}$$

$$\frac{21}{110}$$

[LCM of 10 and 11 = 110]

$$\text{Profit \% } \frac{\frac{21}{110}}{\frac{10}{11}} \times 100$$

$$\frac{11}{110} \times \frac{21}{10} \times 100$$

$$\frac{21}{110} \times 110 = 21\%$$

Profit 21%

18. C.P. of 50 pencils ₹ 80

$$\text{" pencils } ₹ \frac{80}{50} = ₹ \frac{8}{5}$$

Now S.P. of 40 pencils ₹ 90

$$\text{S.P. of 1 pencil } ₹ \frac{90}{40} = ₹ \frac{9}{4}$$

Profit S.P. – C.P.

$$\frac{9}{4} - \frac{8}{5} = \frac{45}{20} - \frac{32}{20}$$

[∵ LCM of 4 and 5 = 20]

$$\frac{13}{20}$$

$$\text{Profit \% } \frac{\frac{13}{20}}{\frac{8}{5}} \times 100$$

$$\frac{13}{20} \times \frac{5}{8} \times 100$$

$$\frac{13 \times 5 \times 100}{20 \times 8}$$

$$\frac{325}{8}$$

$$\text{Profit \% } 40 \frac{5}{8} \%$$

19. C.P. of 2400 pens (200 dozens)

$$\frac{2400}{12} = 15$$

$$200 \times 15$$

$$\text{C.P. of 2400 pens } \frac{2400}{12} = 15$$

$$(200 \text{ dozens}) \quad 200 \times 15$$

$$\text{C.P. of 2400 pens } ₹ 3000$$

I Case

S.P. of 5 pens	₹ 8	
" " " pens	$\frac{8}{5}$	
" " Pens	$\frac{8}{5}$	1050
	8	210
	₹ 1680	

II Case

S.P. of 1 pen	₹ 2	1350
SP of Remaining	2	1350
1350 Pens	₹ 2700	
Total S.P.	2700	
	+ 1680	
	<u>4380</u>	
Total C.P.	300	
Profit	1380	
Profit%	$\frac{1380}{3000} \times 100$	46%

Exercise-6.4

1. (i) We have,
 P ₹ 64000, R 6% p.a., T 2 years

$$\text{S.I.} = \frac{P \times R \times T}{100} = \frac{64000 \times 6 \times 2}{100}$$

$$\text{S.I.} = ₹ 7680$$

and Amount 64000 + 7680
 ₹ 71680

- (ii) We have,
 P ₹ 2650, R 8% p.a.,
 T $2\frac{1}{2}$ years

$$\text{S.I.} = \frac{P \times R \times T}{100} = \frac{2650 \times 8 \times \frac{5}{2}}{100}$$

$$\text{S.I.} = ₹ 530$$

Amount ₹ 2650 + 530
 ₹ 3180

- (iii) We have, P ₹ 1500, R 12% p.a.,
 T 3 years 3 month

$$3\frac{3}{12} \text{ years} = 3\frac{1}{4} \text{ years} = \frac{13}{4} \text{ year}$$

$$\text{S.I.} = \frac{1500 \times 12 \times \frac{13}{4}}{100}$$

$$\text{S.I.} = ₹ 585$$

$$\text{Amount} = ₹ (1500 + 585) = ₹ 2085$$

- (iv) We have,

$$P = ₹ 9600, R = 7\frac{1}{2}\% \text{ p.a.}, \frac{15}{2}\%$$

$$t = 5 \text{ months}, t = \frac{5}{12} \text{ years}$$

$$\text{S.I.} = \frac{P \times R \times t}{100} = \frac{9600 \times 15 \times 5}{100 \times 2 \times 12}$$

$$\text{S.I.} = ₹ 300$$

$$\text{Amount} = ₹ (9600 + 300) = ₹ 9900$$

- (v) We have

$$P = ₹ 5000, R = 9\% \text{ p.a.},$$

$$T = 146 \text{ days} = \frac{146}{365} \text{ year}$$

$$\text{S.I.} = \frac{5000 \times 9 \times 146}{100 \times 365}$$

$$\text{S.I.} = ₹ 180$$

$$\text{Amount} = ₹ 5000 + 180 = ₹ 5180$$

2. Money borrowed (Principal) ₹ 6000

rate 12%

Time 3 year 8 months

$$3\frac{8}{12} \text{ year} = 3\frac{2}{3} \text{ years}$$

$$\text{Time} = \frac{11}{3} \text{ years}$$

$$\text{Interest Charged} = \frac{6000 \times 12 \times 11}{100 \times 3}$$

$$\text{Interest} = ₹ 2640$$

Amount of clear off the debt

$$₹ (6000 + 2640)$$

$$₹ 8640$$

3. We have,

$$\text{S.P.} = ₹ 829.50, r = 10\%, \text{ time} = 3 \text{ years}$$

$$\text{S.I.} = \frac{P \times r \times t}{100}$$

$$829.50 = \frac{P \times 10 \times 3}{100}$$

$$\frac{82950}{10 \ 3} \quad P$$

$$\frac{2765}{\text{sum}} \quad P$$

4. We have rate 11%, time $2\frac{3}{12}$ years

$$2\frac{1}{4} \text{ years} \quad \frac{9}{4} \text{ years}$$

$$\text{Amount} \quad ₹ 4491$$

Let Principal x

$$\text{S.I.} \quad 4491 \quad x$$

$$\text{S.I.} \quad \frac{P \ r \ t}{100}$$

$$(4491 \ x) \frac{x \ 11 \ 9}{100 \ 4}$$

$$400(4491 \ x) \ 99x$$

$$1796400 \ 400x \ 99x$$

$$1796400 \ 499x$$

$$₹ 3600 \ x$$

$$\text{Now principal} \quad ₹ 3600$$

$$\text{Now, S.I.} \quad \frac{P \ r \ t}{100}$$

$$\frac{3600 \ 11 \ 3}{100}$$

$$\text{S.I.} \quad 1188$$

$$₹ 3600 \text{ Amounts to } ₹ (3600) + 1188 = ₹ 4788 \text{ in 3 years.}$$

5. We have,

$$P \ ₹ 3600, A \ ₹ 4734$$

$$t \ 3\frac{1}{2} \text{ years} \quad \frac{7}{2} \text{ years}$$

$$\text{S.I.} \quad 4734 \quad 3600$$

$$₹ 1134$$

$$\text{S.I.} \quad \frac{P \ R \ t}{100}$$

$$1134 \quad \frac{3600 \ R \ 7/2}{100}$$

$$\frac{1134 \ 100 \ 2}{36000 \ 7} \quad R$$

$$9 \ R$$

$$\text{at } 9\% \text{ rate } ₹ 3600 \text{ amounts to}$$

$$₹ 4734 \text{ in } 3\frac{1}{2} \text{ years.}$$

6. We have,

$$P \ ₹ 5600, A \ ₹ 6720, R \ 8\% \text{ pa}$$

$$\text{S.I.} \quad 6720 \quad 5600$$

$$\text{Now, S.I.} \quad \frac{₹ 1120}{P \ R \ t}$$

$$\frac{1120}{100}$$

$$1120 \quad \frac{5600 \ 8 \ t}{100}$$

$$\frac{1120 \ 100}{5600 \ 8} \quad t$$

$$\frac{20}{8} \quad t \quad \frac{5}{2} \quad t$$

$$2\frac{1}{2} \text{ years} \quad t$$

$$\text{In } 2\frac{1}{2} \text{ years } ₹ 5600 \text{ amounts to}$$

$$₹ 6720 \text{ at } 8\% \text{ pa}$$

7. Let principal x

$$\text{Amount} \quad \frac{8}{5}x$$

$$\text{S.I.} \quad \frac{8}{5}x \quad x \quad \frac{3x}{5}$$

$$\text{S.I.} \quad \frac{P \ r \ t}{100}$$

$$\frac{3x}{5} \quad \frac{x \ r \ 5}{100}$$

$$\frac{3x \ 100}{5 \ x \ 5} \quad r$$

$$12\% \quad r$$

$$\text{At } 12\% \text{ sum becomes } \frac{8}{5} \text{ of itself in}$$

$$5 \text{ years.}$$

8. Vibha borrowed ₹ 430,

$$\text{Rate } 12\%,$$

$$\text{Time } \frac{219}{365} \text{ years}$$

$$\text{S.I.} \quad \frac{P \ R \ t}{100}$$

$$\frac{430 \ 12 \ 219}{100 \ 365}$$

$$\text{S.I.} \quad ₹ 30.96$$

$$\text{Amount paid by Vibha } ₹ (430 + 30.96) ₹ 460.96$$

9. Amount borrowed (Principal) ₹ 8400

$$\text{Rate } \frac{25}{2}\%$$

$$\text{Time } \text{Jan} + \text{Feb} + \text{March} + \text{April} + \text{May} + \text{June}$$

$$\begin{array}{r} 21 \quad 28 \quad 31 \quad 30 \quad 31 \quad 4 \\ 145 \text{ days} \\ \text{Interest} \quad \frac{8400 \quad 25 \quad 145}{100 \quad 2 \quad 365} \end{array}$$

$$\begin{array}{l} \text{Amount paid by Mr. Verma} \\ \text{₹ (8400 + 420)} \\ \text{₹ 8820} \end{array}$$

10. We have Principal ₹ 400

$$\begin{array}{l} \text{Amount ₹ 448} \\ \text{S.I. ₹ 48} \end{array}$$

$$\therefore \text{S.I.} \quad \frac{p \quad r \quad t}{100}$$

$$48 \quad \frac{400 \quad 4 \quad t}{100}$$

$$\frac{48 \quad 100}{400 \quad 4} \quad t$$

In 3 years ₹ 400 Amounts to ₹ 448 at 4% p.a.

11. Let ₹ x yield ₹ 1416 in 5 years at $\frac{19}{2}\%$

$$\begin{array}{l} \text{S.I.} \quad 1416 \quad x \\ (1416 \quad x) \quad \frac{x \quad 19 \quad 5}{100 \quad 2} \end{array}$$

$$(1416 \quad x) \quad \frac{95x}{200}$$

$$\begin{array}{r} 200(1416 \quad x) \quad 45x \\ 283200 \quad 200x \quad 95x \\ 283000 \quad 295x \\ 960 \quad x \end{array}$$

₹ 960 yield ₹ 1416 in 5 years at $\frac{19}{2}\%$

12. We have,

P ₹ 4500, A ₹ 5400, time 3 years

S.I. ₹ (5400 - 4500) ₹ 900

$$\text{S.I.} \quad \frac{P \quad R \quad t}{100}$$

$$900 \quad \frac{4500 \quad R \quad 3}{100}$$

$$\frac{\frac{20}{900}}{45 \quad 3} \quad R$$

$$R \quad 6\frac{2}{3}\%$$

13. Let P x A $2x$

S.I. A P

$$2x \quad x \quad x$$

$$\therefore \text{S.I.} \quad \frac{p \quad r \quad t}{100}$$

$$x \quad \frac{x \quad 10 \quad t}{100}$$

$$\frac{100x}{10x} \quad t \quad 10 \text{ years} \quad t$$

In 10 years a sum of money double itself at 10% S.I.

14. (i) We have, A ₹ 4637.50,

S.I. ₹ 1137.50

P ₹ (4637.50 - 1137.50)

P ₹ 3500.00

(ii) We have, A ₹ 1000, S.I. ₹ 3,750

P A S.I.

₹ (10000 - 3,750)

P ₹ 6,250

15. (i) Rohit borrowed Rate (P) ₹ 4000

time 2 years, Rate 15%

Interest paid by Rohit

$$\frac{p \quad r \quad t}{100}$$

$$4000 \quad 15 \quad 2$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

$$\frac{100}{40 \quad 30}$$

Amount paid by Rohit to clear the debt

$$4000 \quad 1200$$

$$₹ 5200$$

7

Algebraic Expressions

Exercise-7.1

1. (i) $3x - 5$ where x is a number

(ii) $q - \frac{3}{4}p$

(iii) $(a - b) - 9$

- (iv) b^2
- (v) $\frac{x}{y} - 7$
- 2. (i) $5p^2q^2r^2$ monomial
- (ii) $3x^2y + 2z$ monomial
- (iii) $3 + 7x^2$ binomial
- (iv) $\frac{5a^2 - 3b^2}{c}$ trinomial
- (v) $7x^5 - \frac{3x}{y}$ binomial
- (vi) $5p^2 - 3q + 3p^2q^2$ trinomial
- (vii) $m^3 + 2n^3 + 5m^2$ polynomial
- (viii) $9a^3b^3c^3 + 5a^2 + 1$ trinomial
- (ix) $5x^4 + \frac{2x^2 - 3x + 1}{5}$ polynomial

- 3.
- | | Numerical Coefficient | Literal Coefficient |
|-----------------------------|-----------------------|---------------------|
| (i) $9p^2q^2r^2$ | 9 | $p^2q^2r^2$ |
| (ii) $\frac{7}{2}xy^2$ | $\frac{7}{2}$ | xy^2 |
| (iii) $\frac{4}{9}a^2b^2cd$ | $\frac{4}{9}$ | a^2b^2cd |
| (iv) $\frac{3}{4x^2y}$ | $\frac{3}{4}$ | $\frac{1}{x^2y}$ |
| (v) $3x^2y + 2z$ | $\frac{3}{2}$ | $\frac{x^2y}{z}$ |
| (vi) $\frac{2ax}{3by}$ | $\frac{2}{3}$ | $\frac{ax}{by}$ |

4. We have, $\frac{2}{3}p^2q^2r^5$
- (i) Coefficient of p^2 is $\frac{2}{3}pq^2r^5$
 - (ii) Coefficient of $2pq$ is $\frac{1}{3}p^2qr^5$
 - (iii) Coefficient of $\frac{1}{3}p^2qr$ is $\frac{2}{3}pqr^4$
 - (iv) Coefficient of $\frac{1}{3}p^2qr$ is $2pqr^4$
 - (v) Coefficient of $2p^2q^2r$ is $\frac{1}{3}pr^4$
 - (vi) Coefficient of p^3q^2 is $\frac{2}{3}r^5$
 - (vii) Coefficient of r^5 is $\frac{2}{3}p^3q^2$
 - (viii) $\frac{2}{3}pqr^2 + p^2qr^3$

5. Like terms are
- (i) $3abc, \frac{2}{3}cab, 7bac$
 - (ii) $7pq^2, \frac{2}{3}q^2p, 5ab^2, \frac{2}{7}b^2a$
 - (iii) $(3p^2q, \sqrt{5}qp^2, qp^2, (\sqrt{5}qp, 4pq))$
 - (iii) $(3x^2yz, \sqrt{5}yzx)$
 - $\sqrt{7}myz^2, \frac{4}{3}z^2xy$
 - $\frac{2}{5}y^2xz, 9xzy^2$

6. Polynomials are
- $\frac{2}{5}x^4 + \sqrt{3}x^2 + 5x + 1$ degree 4
 - $4a^3b^2 + 3ab + 5ab + \frac{2}{3}$ degree 5
 - $2m^2n^4 + \sqrt{3}mn^3 + \frac{2}{7}m^7 + 9m^2$ degree 7

7. (i) $3m + 5$ for $\frac{mn}{m} + 2$
- (ii) $x^2 + 4x + 5$ for $x + 3$
- (iii) $\frac{3}{a} + \frac{2}{b} + \frac{1}{4}$ for $a = 2, b = 3$
- (iv) $m^2 + n^2 + 2mn$ for $m = \frac{1}{2}, n = \frac{1}{3}$
- (v) $x + 3 + 2(x + 5)$ for $x = 2$

$$\begin{array}{r}
 \text{(vi) } y^2 - 2(y - 7) \text{ for } y = 3 \\
 (3)^2 - 2(3 - 7) \\
 9 - 2 \cdot 10 \\
 9 - 20 \\
 11
 \end{array}$$

Exercise-7.2

$$\begin{array}{r}
 \text{1. (i) } 3x^2 - 4y^2 - 5xy - 6x^2 \\
 9xy - 3y^2 - 8x^2 \\
 \text{Collecting like terms} \\
 x^2(3 - 6 - 8) - y^2(-4 - 3)
 \end{array}$$

$$\begin{array}{r}
 -xy(5 - 9) \\
 x^2(-1) - y^2(-7) - xy(-4) \\
 x^2 - y^2 - 4xy \\
 \text{(ii) } \frac{2}{3}x^2 - 5x - 3x - \frac{4}{5} - 2x^3 \\
 \frac{7}{2}x^2 - 5x - 1 - 2x^4
 \end{array}$$

$$\begin{array}{r}
 \text{Collecting like terms} \\
 x^3 - \frac{2}{3} - 2 - 2x^4 - x^2 - 5 - \frac{7}{2} \\
 x(3 - 5) - \frac{4}{5} - 1 \\
 x^3 - \frac{4}{3} - 2x^4 - x^2 - \frac{17}{2}
 \end{array}$$

$$\begin{array}{r}
 8x - \frac{1}{5} \\
 2x - \frac{4}{3}x^3 - \frac{17}{2}x^2 - 8x - \frac{1}{5} \\
 \text{(iii) } \frac{1}{2}p - 3q - \frac{2}{3}r - \frac{4}{5}p - \frac{3}{2}q \\
 2r - \frac{2}{3}p - 7r
 \end{array}$$

$$\begin{array}{r}
 \text{Collecting like terms} \\
 p - \frac{1}{2} - \frac{4}{5} - \frac{2}{3} - q - 3 - \frac{3}{2} \\
 r - \frac{2}{3} - 2 - 7 \\
 p - \frac{15}{30} - \frac{24}{30} - \frac{20}{30} - q - \frac{6}{2} - \frac{3}{2} \\
 r - \frac{2}{3} - \frac{6}{3} - \frac{21}{3}
 \end{array}$$

$$\frac{59}{30}p - \frac{3}{2}q - r - \frac{25}{3}$$

$$\begin{array}{r}
 \frac{59}{30}p - \frac{3}{2}q - \frac{25}{3}r \\
 \text{3. (i) } \begin{array}{r} 2a - 7b - 5c - 2 \\ 3a - 2b - 9c \\ 4a - 6b - 5c - 4 \\ \hline 3a - 11b - 19c - 6 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(ii) } \begin{array}{r} 3x - 4y - z \\ 2x - 5y - z \\ 6x - 7z \\ \hline 3x - 9y - 2z - 5 \\ 8x - 10y - 5z - 5 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(iii) } \begin{array}{r} 4x - 7x^2 - 9 \\ 3x^2 - 4 - 5x \\ 7x^3 - 1 - 11x \\ + 6x^2 - 13x \\ \hline 11x^3 - 2x^2 - 14 - 29x \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(iv) } \begin{array}{r} 5ax - 3by - 7cz \\ 11ax - 7by - 3cz \\ \hline ax - 3by - 12cz \\ 7ax - by - 16cz \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{3. (i) } \begin{array}{r} 3a - 5b - 9c - 3 \\ 5a - 3b - 11c - 2 \\ \hline (-) (+) (-) (+) \\ 2a - 8b - 2ac - 5 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(ii) } \begin{array}{r} 7x^2 - 10xy - y - 5 \\ 3x^2 - 9xy - y^2 \\ \hline (-) (+) (-) \\ 4x^2 - xy - 2y^2 - 5 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(iii) } \begin{array}{r} 3p^2 - 4q^2 - 8r^2 \\ 4p^2 - 5q^2 - 7r^2 \\ \hline (-) (-) (+) \\ p^2 - 9q^2 - r^2 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{(iv) } \begin{array}{r} 9m^4 - 5m^2 - 7m - 6 \\ 5m^4 - 2m^2 - 3 - 3m^3 \\ \hline (-) (-) (+) (+) \\ 4m^4 - 3m^2 - 7m - 9 - 3m^3 \\ \hline \text{or } 4m^4 - 3m^3 - 3m^2 - 7m - 9 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \text{4. Perimeter of Rectangle } 2(l + b) \\
 2[(3x^2 - 2y^2) + (x^2 - 3xy)] \\
 2[3x^2 - 2y^2 + x^2 - 3xy]
 \end{array}$$

$$(iii) \text{ To find, } \begin{array}{r} \frac{5}{2}p^4q^4r \\ \frac{2}{7}ab^2 \\ 7ab \quad 3a^3 \end{array} \begin{array}{r} a^1 \quad 3 \quad 1 \\ b^1 \quad 2 \end{array}$$

$$\begin{array}{r} 6a^5b^3 \\ 7ab \quad 3a^3 \end{array} \frac{2}{7}ab^2 \quad 6a^5b^3$$

$$(iv) \text{ To find, } \begin{array}{r} \frac{1}{2}x^2 \quad \frac{3}{5}xy \quad \frac{2}{3}yz \quad \frac{5}{7}xyz \\ \frac{1}{2} \quad \frac{3}{5} \quad \frac{2}{3} \quad \frac{5}{7} \end{array} \begin{array}{r} x^2 \quad 1 \quad 1 \\ y^1 \quad 1 \quad 1 \quad z^1 \quad 1 \end{array}$$

$$\begin{array}{r} \frac{1}{7}x^4y^3z^2 \\ \frac{1}{2}x^2 \quad \frac{3}{5}xy \quad \frac{2}{3}yz \quad \frac{5}{7}xyz \\ \frac{1}{7}x^4y^3z^2 \end{array}$$

$$2. (i) \text{ To find } \begin{array}{r} 3xyz \quad (3x \quad 5y \quad 7z) \\ 3xyz \quad 3x \quad 3xy \quad 5y \end{array} \begin{array}{r} 3xyz \quad 7z \\ 9x^2yz \quad 15xy^2 \quad 21xyz^2 \end{array}$$

$$(ii) \text{ To find, } \begin{array}{r} 2pq \quad (2p^2 \quad 3pq \quad 5q^2 \quad 5) \\ 2pq \quad 2p^2 \quad 2pq \quad 3pq \\ 2pq \quad 5q^2 \\ 4p^3q \quad 6p^2q^2 \quad 10pq^3 \quad 10pq \end{array}$$

$$(ii) \text{ To find, } \begin{array}{r} 35ab \quad \frac{2}{3}a^2b \quad \frac{4}{5}ab^2 \quad \frac{2}{7}ab \quad 3 \\ 35ab \quad \frac{2}{3}a^2b \quad 35ab \quad \frac{4}{5}ab^2 \\ 35ab \quad \frac{2}{7}ab \quad 35ab \quad 3 \\ \frac{70}{3}a^3b^2 \quad 28a^2b \\ 10a^2b^2 \quad 15ab \end{array}$$

$$(iv) \text{ To find, } \begin{array}{r} 6x^3 \quad 7x^5 \quad 4x^3 \quad 5x^2 \quad \frac{2}{3}x \quad 6 \end{array}$$

$$\begin{array}{r} 6x^3 \quad 7x^5 \quad 6x^3 \quad 4x^3 \\ 6x^3 \quad 5x^2 \quad 6x^3 \quad \frac{2}{3}x \quad 6x^3 \quad 6 \\ 42x^8 \quad 24x^6 \quad 30x^5 \quad 4x^4 \quad 36x^3 \end{array}$$

3. (i) To find :

$$(5x - 2)(3x - 4)$$

Ist Method : Horizontal Method

$$\begin{array}{r} 5x(3x - 4) - 2(3x - 4) \\ \text{(Distributive law)} \end{array}$$

$$15x^2 - 20x - 6x + 8$$

$$15x^2 - 26x + 8$$

IInd Method : Column Method

$$\begin{array}{r} 5x \quad 2 \\ \times 3x \quad 4 \\ \hline 15x^2 \quad 6x \\ \quad 20x \quad 8 \\ \hline 15x^2 \quad 26x \quad 8 \end{array}$$

$$(ii) (ax + b)(cx + d) = ax(cx + d) + b(cx + d)$$

[distributive law]

$$\begin{array}{r} acx^2 \quad adx \quad bcx \quad bd \\ acx^2 \quad (ad + bc)x \quad bd \end{array}$$

$$(iii) (4p - 7)(2 - 3p) = 4p(2 - 3p) - 7(2 - 3p)$$

$$8p - 12p^2 - 14 + 21p$$

$$8p + 21p - 12p^2 - 14$$

$$29p - 12p^2 - 14$$

$$(iv) (2x^2 - 3)(3x - 5) = 2x^2(3x - 5) - 3(3x - 5)$$

$$6x^3 - 10x^2 - 9x + 15$$

$$6x^3 - 10x^2 - 9x + 15$$

$$(v) 2a - \frac{1}{2}a - \frac{1}{3}a = 2a - a\left(\frac{1}{3} + \frac{1}{2}\right) = 2a - a\left(\frac{2}{6} + \frac{3}{6}\right) = 2a - a\left(\frac{5}{6}\right) = 2a - \frac{5}{6}a = \frac{12}{6}a - \frac{5}{6}a = \frac{7}{6}a$$

$$2a^2 - a \frac{2}{6} - \frac{3}{6} - \frac{1}{6}$$

$$2a^2 - \frac{5a}{6} - \frac{1}{6}$$

$$2a^2 - \frac{5a}{3} - \frac{1}{3}$$

$$(vi) \begin{pmatrix} 3x & 5y \\ 5x & 3y \end{pmatrix} \begin{pmatrix} 5x & 3y \\ 3x & 5y \end{pmatrix} \\ \begin{pmatrix} 15x^2 & 9xy & 25xy & 15y^2 \\ 15x^2 & 16xy & 15y^2 \end{pmatrix}$$

4. (i) We have to find

$$\begin{pmatrix} 3x & 1 \\ 2x^2 & 3x & 1 \end{pmatrix} \begin{pmatrix} 3x & 1 \\ 1 & 2x^2 & 3x & 1 \end{pmatrix} \\ \begin{pmatrix} 6x^3 & 9x^2 & 3x & 2x^2 & 3x & 1 \\ 6x^3 & 11x^2 & 1 \end{pmatrix}$$

$$(ii) \text{ To find } \begin{pmatrix} x & 2y \\ x & 2y & 3 \end{pmatrix} \begin{pmatrix} x & 2y & 3 \\ x & 2y & 3 \end{pmatrix} \\ \begin{pmatrix} x^2 & 2xy & 3x & 2xy & 4y^2 & 6y \\ (x & 2y)(x & 2y & 3) & x^2 & 3x & 4y^2 & 6y \end{pmatrix}$$

$$(iii) \text{ To find } \begin{pmatrix} 2x & 3 \\ 2 & 3x & 5x^2 \end{pmatrix} \begin{pmatrix} 2x & 3 & 5x^2 \\ 2x & 3x & 5x^2 \end{pmatrix} \\ \begin{pmatrix} 4x & 6x^2 & 10x^3 & 6 & 9x & 15x^2 \\ 10x^3 & 6x^2 & 21x^2 & 4x & 9x & 6 \\ 10x^3 & 9x^2 & 13x & 6 \end{pmatrix} \\ \begin{pmatrix} (2x & 3)(2 & 3x & 5x^2) \\ 10x^3 & 9x^2 & 13x & 6 \end{pmatrix}$$

(iv) To find, $\begin{pmatrix} 5 & 3x \\ 3x^3 & 2x^2 & 5 \end{pmatrix} \begin{pmatrix} 5 & 3x \\ 3x^3 & 2x^2 & 5 \end{pmatrix}$

$$\begin{pmatrix} 3x(3x^3 & 2x^2 & 5) \\ 15x^3 & 10x^2 & 25 & 9x^4 \\ & & 6x^3 & 15x \\ 9x^4 & 15x^3 & 6x^3 & 10x \\ & & & 15x & 25 \\ 9x^4 & 21x & 10x^2 & 15x & 25 \end{pmatrix}$$

5. (i) To find,

$$\begin{pmatrix} 2x^2 & x & 5 \\ 3x^2 & 2x & 1 \end{pmatrix} \begin{pmatrix} 2x^2 & x & 5 \\ 3x^2 & 2x & 1 \end{pmatrix} \\ \begin{pmatrix} 2x & 1 \\ 5(3x^2 & 2x & 1) \end{pmatrix}$$

$$\begin{pmatrix} 6x^4 & 4x^3 & 2x & 3x^3 & 2x^2 \\ & & x & 15x^2 & 10x & 5 \\ 6x^4 & 4x^3 & 3x^3 & 2x & 2x^2 \\ & & 15x^2 & x & 10x & 5 \\ 6x^4 & x^3 & 19x^2 & 9x & 5 \end{pmatrix}$$

(ii) To find,

$$\begin{pmatrix} 2y^2 & 1 & 3y^2 \\ 2 & 3y & 5y^2 \end{pmatrix} \begin{pmatrix} 2 & 3y & 5y^2 \\ 1 & 2 & 3y & 5y^2 \end{pmatrix} \\ \begin{pmatrix} 2y^2(2 & 3y & 5y^2) & 1(2 & 3y & 5y^2) \\ & & 3y^2(2 & 3y & 5y^2) \\ 4y^2 & 6y^3 & 10y^4 & 2 & 3y \\ & & 5y^2 & 6y^2 & 9y^3 & 15y^4 \\ 10y^4 & 15y^4 & 6y^3 & 9y^3 \\ & & 4y^2 & 5y^2 & 3y & 2 \\ 25y^4 & 15y^3 & 15y^2 & 3y & 2 \end{pmatrix}$$

(ii) To find,

$$\begin{pmatrix} x^2 & 3x & 5 \\ 5x^3 & 7x^2 & 2x & 3 \end{pmatrix} \begin{pmatrix} x^2 & 3x & 5 \\ 5x^3 & 7x^2 & 2x & 3 \end{pmatrix} \\ \begin{pmatrix} 3x(5x^3 & 7x^2 & 2x & 3) \\ 5(5x^3 & 7x^2 & 2x & 3) \\ 5x^5 & 7x^4 & 2x^3 & 2x^2 & 15x^4 \\ 21x^3 & 6x^2 & 9x & 25x^3 \\ & & 35x^2 & 10x & 15 \end{pmatrix}$$

$$(iv) \begin{pmatrix} x^2 & xy & y^2 \\ 4x^2 & 24xy & 3y^2 \end{pmatrix} \begin{pmatrix} x^2 & xy & y^2 \\ 4x^2 & 24xy & 3y^2 \end{pmatrix} \\ \begin{pmatrix} x^2(4x^2 & 24xy & 3y^2) \\ xy(4x^2 & 24xy & 3y^2) \\ y^2(4x^2 & 24xy & 3y^2) \\ 4x^4 & 24x^3y & 3x^2y^2 & 4x^3y \\ 3x^2y^2 & 24x^2y^2 & 3xy^3 & 24xy^3 \\ & & 4x^2y^2 & 3y^4 \\ 4x^4 & 24x^3y & 4x^3y & 3x^2y^2 \\ & & 24x^2y^2 & 2xy^3 & 24xy^3 \\ & & & 4x^3y & 3y^4 \\ 4x^4 & 20x^3y & 21x^2y^2 & 21xy^3 \\ & & & 4x^3y & 3y^4 \end{pmatrix}$$

(v) To find,

$$\begin{pmatrix} 2p & 3q & 5 \\ 5p & 2q & 3 \end{pmatrix} \begin{pmatrix} 2p & 3q & 5 \\ 5p & 2q & 3 \end{pmatrix} \\ \begin{pmatrix} 2p(5p & 2q & 3) & 3q(5p & 2q & 3) \\ & & 5(5p & 2q & 3) \end{pmatrix}$$

$$\begin{array}{r}
 10p^2 \quad 4pq \quad 6p \quad 15pq \quad 6q^2 \\
 \quad 9q \quad 25p \quad 10q \quad 15 \\
 10p^2 \quad 25p \quad 4pq \quad 15pq \\
 \quad 6p \quad 9q \quad 10q \quad 6q^2 \quad 15 \\
 10p^2 \quad 11pq \quad 19p \quad 19q \\
 \quad 6q^2 \quad 15
 \end{array}$$

6. To find, $[(x-2)(x-3)](x-4)$

$$\begin{array}{r}
 [x(x-3) - 2(x-3)](x-4) \\
 (x^2 - 3x + 2x - 6)(x-4) \\
 (x^2 - 5x + 6)(x-4) \\
 x^2(x-4) - 5x(x-4) + 6(x-4) \\
 x^3 - 4x^2 - 5x^2 + 20x + 6x - 24 \\
 x^3 - 9x^2 + 26x - 24
 \end{array}$$

(ii) To find,

$$\begin{array}{r}
 [(x-3)(x-3)][(x-4)(x-4)] \\
 [x(x-3) - 3(x-3)][(x-4)(x-4)] \\
 [x^2 - 3x - 3x + 9] \\
 [x^2 - 4x + 4x - 16] \\
 (x^2 - 9)(x^2 - 16) \\
 x^2(x^2 - 16) - 9(x^2 - 16) \\
 x^4 - 16x^2 - 9x^2 + 144 \\
 x^4 - 25x^2 + 144
 \end{array}$$

Exercise-7.4

1. (i) To find, $45x^2 - 15x$

$$\frac{45x^2}{15x} - 3x$$

(ii) To find, $\frac{25x}{x} - 25$

$$\frac{25x}{x} - 25$$

(iii) To find, $25x^2 - x^2$

$$\frac{25x^2}{x^2} - 25$$

(iv) To find, $24a^2b^2 - 3ab$

$$\frac{24a^2b^2}{3ab} - 8ab$$

(v) To find, $85x^2yz - 5xyz$

$$\frac{85x^2yz}{5xyz} - 17x$$

$$85x^2yz - 5xyz - 17x$$

(vi) To find, $21p^2q^2r^2 - pqr$

$$\frac{21p^2q^2r^2}{pqr}$$

$$21pqr$$

$$21p^2q^2r^2 - pqr - 21pqr$$

2. (i) To find, $(25x^3 - 5x^2 - 6) - 5x$

$$\frac{25x^3}{5x} - \frac{5x^2}{5x} - \frac{6}{5x}$$

$$5x^2 - x - \frac{6}{5x}$$

$$(25x^3 - 5x^2 - 6) - 5x$$

$$5x^2 - x - \frac{6}{5x}$$

(ii) To find,

$$(12x^2y^2 - 9x^2y - 12xy^2 - 6xy) - \frac{2}{3}$$

$$\frac{12x^2y^2}{2/3} - \frac{9x^2y}{2/3} - \frac{12xy^2}{2/3} - \frac{6xy}{2/3}$$

$$12 \cdot \frac{3}{2}x^2y^2 - 9 \cdot \frac{3}{2}x^2y$$

$$12 \cdot \frac{3}{2}xy^2 - 6 \cdot \frac{3}{2}xy$$

$$18x^2y^2 - \frac{27}{2}x^2y - 18xy^2 - 9xy$$

(ii) To find,

$$(8x^2y^2 - 6x^2y - 4xy^2) - 2xy$$

$$\frac{8x^2y^2}{2xy} - \frac{6x^2y}{2xy} - \frac{4xy^2}{2xy}$$

$$4xy - 3x - 2y$$

(iv) To find, $(x^3 - 6x^2 - 5x) - x$

$$\frac{x^3}{x} - \frac{6x}{x} - \frac{5x}{x}$$

$$x^2 - 6x - 5$$

3. (i) $(15x^2 - 6x - 3) - (x - 1)$

$$(x-1) \overline{)15x^2 - 6x - 3} \quad \begin{array}{l} 15x \\ 9 \\ 9 \end{array}$$

$$\begin{array}{r}
 15x^2 \\
 -15x^2 \\
 \hline
 15x
 \end{array}$$

$$\begin{array}{r}
 15x \\
 -15x \\
 \hline
 9x - 3
 \end{array}$$

$$\begin{array}{r}
 9x - 3 \\
 +9x - 3 \\
 \hline
 18x - 6
 \end{array}$$

Quotient $15x - 9$ Remainder 6

(ii) To find,
 $(4x^3 \ 24x^2 \ 52x \ 16) \div (2x \ 3)$

$$\begin{array}{r}
 2x^2 \ 9x \ 25/2 \\
 2x \ 3 \overline{) 4x^3 \ 24x^2 \ 52x \ 16} \\
 \underline{4x^3 \ 6x^2} \\
 18x^2 \ 52x \ 16 \\
 \underline{18x^2 \ 27x} \\
 (+) \quad (-) \\
 25x \ 16 \\
 \underline{75} \\
 (-) \quad (+) \\
 43 \\
 \underline{2} \\
 \text{Quotient} \quad 2x^2 \ 9x \ \frac{25}{2} \\
 \text{Remainder} \quad \frac{43}{2}
 \end{array}$$

(ii) To find,
 $(x^4 \ 2x^3 \ 3x^2 \ 5x \ 3) \div (x \ 5)$

$$\begin{array}{r}
 x^2 \ 7x^2 \ 38x \ 195 \\
 x \ 5 \overline{) x^4 \ 2x^3 \ 3x^2 \ 5x \ 15} \\
 \underline{x^4 \ 5x^3} \\
 (-) \quad (-) \\
 7x^3 \ 3x^2 \ 5x \ 15 \\
 \underline{7x^3 \ 35x^2} \\
 (+) \quad (+) \\
 38x^2 \ 5x \ 15 \\
 \underline{43x^2 \ 190x} \\
 195x \ 115 \\
 \underline{195x \ 975} \\
 (+) \quad (+) \\
 900 \\
 \text{Quotient} \quad x^3 \ 7x^2 \ 38x \ 195 \\
 \text{Remainder} \quad 900
 \end{array}$$

(iv) To find,
 $(x^5 \ 28x^3 \ 3x^2 \ 16x) \div x \ 3$

$$\begin{array}{r}
 x^4 \ 3x^3 \ 19x^2 \ 54x \ 178 \\
 x \ 3 \overline{) x^5 \ 28x^3 \ 3x \ 16x} \\
 \underline{x^5 3x^4} \\
 (-) \quad (+)
 \end{array}$$

$$\begin{array}{r}
 3x^4 \ 28x^3 \ 3x^2 \ 16x \\
 \underline{3x^4 \ 9x^3} \\
 - \quad + \\
 19x^3 \ 3x^2 \ 16x \\
 \underline{19x^3 \ 57x^2} \\
 + \quad - \\
 54x^2 \ 16x \\
 \underline{54x^2 \ 162x} \\
 178x \\
 \underline{178x \ 534} \\
 + \quad - \\
 534
 \end{array}$$

(v) $x^3 \ 3 \overline{) x^4 \ 6x^3 \ 17x^2 \ 15}$

$$\begin{array}{r}
 x^2 \ 36x \ 20 \\
 x^3 \ 3 \overline{) x^4 \ 6x^3 \ 17x^2 \ 15} \\
 \underline{x^4 3x^2} \\
 (-) \quad (-) \\
 6x^3 \ 20x^2 \ 15 \\
 \underline{6x^3 18x} \\
 (-) \quad (-) \\
 20x^2 \ 18x \ 15 \\
 \underline{20x^2 60} \\
 (+) \quad (+) \\
 18x \ 75
 \end{array}$$

Quotient $x^2 \ 6x \ 20$
 Remainder $18x \ 75$

4. (i) To find,
 $(x^2 y^2 \ x^2 \ y^2) \div (x^2 \ 1)$

$$\begin{array}{r}
 y^2 \ 1 \\
 x^2 \ 1 \overline{) x^2 y^2 \ x^2 \ y^2 \ 1} \\
 \underline{x^2 y^2 y^2} \\
 (-) \quad (+) \\
 x^2 \ 1 \\
 \underline{x^2 \ 1} \\
 (+) \quad (-) \\
 0
 \end{array}$$

Quotient $y^2 \ 1$ Remainder 0

(ii) To find,
 $(x^3 \ x^2 \ x \ 1) \div (x^2 \ 1)$

$$\begin{array}{r}
 x^2 \quad 1 \overline{) x^3 \quad x^2 \quad x \quad 1} \\
 \underline{x^3 \quad \quad x } \\
 (-) \quad (-) \\
 \quad x^2 \quad 1 \\
 \quad \underline{x^2 \quad 1} \\
 \quad (-) \quad (-) \\
 \quad \quad \underline{0}
 \end{array}$$

Quotient $x + 1$
Remainder 0

(iii) To find, $(x^2 - xy + y - x) \div (x - y)$

$$\begin{array}{r}
 (x - y) \overline{) x^2 - xy + y - x} \\
 \underline{x^2 - xy} \\
 (-) \quad (+) \\
 \quad y - x \\
 \quad \underline{y - x} \\
 \quad (-) \quad (+) \\
 \quad \quad \underline{0}
 \end{array}$$

Quotient $x + 1$
Remainder 0

(iv) To find,

$$(x^2 - y^2 - 2xy + 1) \div (x - y + 1)$$

$$\begin{array}{r}
 x - y + 1 \overline{) x^2 - y^2 - 2xy + 1} \\
 \underline{x^2 - xy - x} \\
 (-) \quad (-) \quad (+) \\
 \quad y^2 - xy - x + 1 \\
 \quad \underline{y^2 - xy - y} \\
 \quad \quad (-) \quad (-) \quad (+) \\
 \quad \quad \quad x - y + 1 \\
 \quad \quad \quad \underline{x - y + 1} \\
 \quad \quad \quad (-) \quad (-) \quad (+) \\
 \quad \quad \quad \quad \underline{0}
 \end{array}$$

Quotient $x - y + 1$
Remainder 0

(v) To find,

$$(x^6 - 3x^4 + 3x^2 - 1) \div (x^3 - 3x^2 + 3x - 1)$$

$$\begin{array}{r}
 x^3 - 3x^2 + 3x - 1 \overline{) x^6 - 3x^4 + 3x^2 - 1} \\
 \underline{x^6 - 3x^5 + 3x^4 - x^3} \\
 (-) \quad (-) \quad (-) \quad (-) \\
 \quad 3x^5 - 6x^4 + x^3 + 3x^2 - 1 \\
 \quad \underline{3x^5 - 9x^4 + 9x^3 + 3x^2} \\
 \quad \quad (+) \quad (+) \quad (+) \quad (+) \\
 \quad \quad \quad 8x^3 - 6x^2 + 1 \\
 \quad \quad \quad \underline{8x^3 - 9x^2 + 9x} \\
 \quad \quad \quad (-) \quad (-) \quad (-) \quad (-) \\
 \quad \quad \quad \quad 1x^3 - 3x^2 + 3x + 1 \\
 \quad \quad \quad \quad \underline{1x^3 - 3x^2 + 3x + 1} \\
 \quad \quad \quad \quad (+) \quad (+) \quad (+) \quad (+) \\
 \quad \quad \quad \quad \quad \quad \quad \underline{0}
 \end{array}$$

Quotient $x^3 - 3x^2 + 3x - 1$
Remainder 2

5. (i) Dividend (Divisor) (Quotient) +
Remainder

$$\begin{array}{r}
 (x - 2)(x^2 - 2x + 3) + 0 \\
 x(x^3 - 2x^2 + 3x - 2) + 0 \\
 2(x^2 - 2x + 3) + 0 \\
 x^3 - 2x^2 + 3x - 2x^2 + 6x - 6 + 0 \\
 4x - 6 + 0
 \end{array}$$

Dividend $x^3 - x + 6$

(ii) Dividend $(x^2 - 2)(x - 2) + 0$
 $x^2(x - 2) - 2(x - 2) + 0$

Dividend $x^3 - 2x^2 - 2x + 4 + 0$

(iii) Dividend $(x - y + 1)(y - x + 1) + 0$
 $xy - x^2 + x - y^2 + xy$

Dividend $2xy - x^3 - y^2 + x + 1$

(iv) Dividend

$$\begin{array}{r}
 (\text{Divisor}) \times \text{Quotient} + \text{Remainder} \\
 (x - 3)(5x^4 - 2x^3 - 6x^2 + 3x - 9) + 7 \\
 5x^5 - 2x^4 - 6x^3 + 3x^2 - 9x + 15x^4 - 6x^3 \\
 18x^2 - 9x - 27 + 7 \\
 \text{Dividend } 5x^5 - 13x^4 - 15x^2 - 20
 \end{array}$$

Exercise-8.1

1. (i) We have,

$$\begin{array}{r} 9x - 6 = 21 \\ 9x = 27 \\ x = 3 \end{array}$$

Checking

$$\begin{array}{l} \text{LHS} \quad (9x - 6) \\ \quad \quad 9(3) - 6 \\ \quad \quad 27 - 6 \\ \quad \quad 21 \end{array}$$

$$\text{LHS} = \text{RHS} \quad \text{Hence Proved}$$

(ii) We have,

$$\begin{array}{r} 3x - 5 = 2x + 8 \\ 3x - 2x = 8 + 5 \\ x = 3 \end{array}$$

Checking :

$$\begin{array}{l} \text{LHS} \quad \quad \quad \text{RHS} \\ 3(3) - 5 \quad 2(3) + 8 \\ 14 \quad \quad 14 \quad \text{Hence Proved} \end{array}$$

(iii) We have,

$$\begin{array}{r} 2(5x - 4) = 4(3x - 5) \\ 10x - 8 = 12x - 20 \\ 2x = 28 \\ x = 14 \end{array}$$

Checking :

$$\begin{array}{l} \text{LHS} \quad 2[5(14) - 4] \\ \quad \quad 2[70 - 4] \\ \quad \quad 2[74] \\ \quad \quad 148 \\ \text{RHS} \quad 4[3(14) - 5] \\ \quad \quad 4[42 - 5] \\ \quad \quad 4 \cdot 37 \\ \quad \quad 148 \end{array}$$

$$\text{LHS} = \text{RHS} \quad \text{Hence proved}$$

(iv) We have,

$$\begin{array}{r} 3x - 2(2x - 5) = 2(x - 3) + 8 \\ 3x - 4x + 10 = 2x - 6 + 8 \\ x + 10 = 2x + 2 \\ x - 2x = 2 - 10 \\ -x = -8 \\ x = 8 \end{array}$$

Checking :

$$\begin{array}{l} \text{LHS} \\ 3(8) - 2[2(8) - 5] \end{array}$$

$$12 - 2(8 - 5)$$

$$12 - 2 \cdot 3$$

$$12 - 6$$

$$6$$

$$\text{RHS} \quad 4[4 - 3] + 8$$

$$2(7) + 8$$

$$14 + 8$$

$$6$$

$$\text{LHS} = \text{RHS} \quad \text{Hence Proved}$$

(v) We have,

$$\frac{x}{2} - \frac{x}{3} = \frac{x}{5} + 6$$

$$\frac{x}{2} - \frac{x}{3} - \frac{x}{5} = 6$$

$$\frac{15x - 10x - 6x}{30} = 6$$

$$-x = 30$$

$$25x - 6x = 6 \cdot 30$$

$$19x = 180$$

$$x = \frac{180}{19}$$

$$x = \frac{180}{19}$$

Checking:

$$\begin{array}{l} \text{LHS} \quad \frac{180}{19} - \frac{180}{19} \\ \quad \quad \frac{180 - 180}{19} \\ \quad \quad \frac{0}{19} \\ \quad \quad 0 \end{array}$$

$$\frac{250}{19} - \frac{250}{19}$$

$$19 \cancel{0} = 19$$

$$\text{RHS} \quad \frac{180}{19} + 6$$

$$\frac{180 + 114}{19}$$

$$\frac{294}{19}$$

$$\frac{180 \cdot 570}{95} = \frac{750}{95} = \frac{250}{19}$$

$$\frac{180 \cdot 570}{95} = \frac{750}{95} = \frac{250}{19}$$

$$\frac{250}{19}$$

$$\text{LHS} = \text{RHS} \quad \text{Hence proved}$$

(vi) We have,

$$\frac{x - 5}{x - 9} = 7$$

$$x - 5 = 7(x - 9)$$

$$x - 5 = 7x - 63$$

$$x - 7x = 63 - 5$$

$$\begin{array}{r} 6x \quad 68 \\ x \quad \frac{68}{6} \\ x \quad \frac{34}{3} \end{array}$$

Checking :

$$\begin{array}{r} \frac{34}{3} \quad 5 \quad \frac{34}{3} \quad 15 \\ \frac{34}{3} \quad 9 \quad \frac{34}{3} \quad 27 \\ \frac{49}{7} \quad 7 \quad \text{RHS} \end{array}$$

Hence Proved

(vii) We have,

$$\begin{array}{r} 2(x \quad 2) \quad 3(4x \quad 1) \quad 0 \\ 2x \quad 4 \quad 2x \quad 3 \quad 0 \\ \quad \quad \quad 14x \quad 7 \quad 0 \\ x \quad \frac{7}{14} \quad x \quad \frac{1}{2} \end{array}$$

Checking :

LHS

$$2 \frac{1}{2} \quad 2 \quad 3 \quad 4 \quad \frac{1}{2} \quad 1$$

$$\begin{array}{r} (1 \quad 4) \quad 3(2 \quad 1) \\ 3 \quad 3 \end{array}$$

$$0 \quad \text{RHS} \quad (\text{Hence Proved})$$

(viii) $2x \frac{1}{3} \frac{1}{5} x$

$$\begin{array}{r} 2x \quad x \quad \frac{1}{5} \quad \frac{1}{3} \\ 3x \quad \frac{3}{15} \quad \frac{5}{15} \end{array}$$

$$3x \quad \frac{8}{15} \quad x \quad \frac{8}{45}$$

Checking :

$$\begin{array}{r} \text{LHS} \quad \text{RHS} \\ 2 \quad \frac{8}{45} \quad \frac{1}{3} \quad \frac{1}{5} \quad \frac{8}{45} \\ 16 \quad 15 \quad \frac{9}{8} \quad \frac{45}{45} \\ \frac{45}{45} \quad = \quad \frac{1}{45} \end{array}$$

LHS = RHS

Hence proved

(ix) $\frac{1}{2}x \quad 3 \quad 5 \quad \frac{1}{3}x$

$$\begin{array}{r} \frac{1}{2}x \quad \frac{1}{3}x \quad 5 \quad 3 \\ \frac{3x}{6} \quad \frac{2x}{6} \quad 8 \\ x \quad 8 \quad 6 \\ x \quad 48 \end{array}$$

Checking :

$$\begin{array}{r} \text{LHS} \quad \text{RHS} \\ \frac{1}{2} \quad 48 \quad 3 \quad 5 \quad \frac{1}{3} \quad 48 \\ 24 \quad 3 \quad 5 \quad 16 \\ 21 \quad = \quad 21 \end{array}$$

LHS = RHS Hence proved

(x) We have, $\frac{x}{2} \quad \frac{x}{4} \quad \frac{1}{8}$

$$\begin{array}{r} 2x \quad 1x \quad \frac{1}{8} \\ 4 \quad \frac{1}{8} \\ \frac{3x}{4} \quad \frac{1}{8} \end{array}$$

$$x \quad \frac{1}{8} \quad \frac{1}{3} \quad x \quad \frac{1}{6}$$

Checking :

$$\begin{array}{r} \text{LHS} \quad \frac{1}{6} \quad \frac{1}{2} \quad \frac{1}{6} \quad \frac{1}{4} \\ \frac{1}{12} \quad \frac{1}{24} \quad \frac{2}{24} \quad \frac{1}{24} \\ \frac{3}{24} \\ \frac{1}{8} \quad \text{RHS} \quad \text{Hence Proved} \end{array}$$

2. (i) We have,

$$\begin{array}{r} 0.5x \quad \frac{x}{3} \quad 0.25x \quad 7 \\ \frac{3 \quad 0.5x \quad 1 \quad x}{3} \quad 0.25x \quad 7 \\ 1.5x \quad x \quad 3(0.25x \quad 7) \\ 2.5x \quad 0.75x \quad 21 \\ 2.5x \quad 0.75x \quad 21 \\ 1.75x \quad 21 \\ x \quad \frac{21}{1.75} \\ x \quad 12 \end{array}$$

(ii) $0.18(5x \quad 4) = 0.5x \quad 0.8$
 $0.90x \quad 0.72 \quad 0.5x \quad 0.8$

$$\begin{array}{r}
 0.90x \quad 0.5x \quad 0.8 \quad 0.72 \\
 0.40x \quad 1.52 \\
 x \quad \frac{1.52}{0.40} \\
 x \quad 3.8
 \end{array}$$

(iii) $2.4(3 - x) + 0.6(2x - 3) = 0$

$$\begin{array}{r}
 7.2x \quad 2.4x \quad 1.2x \quad 1.8 = 0 \\
 2.4x \quad 1.2x \quad 1.8 \quad 7.2 \\
 3.6x \quad 9.0 \\
 x \quad \frac{9.0}{3.6} \\
 x \quad 2.5
 \end{array}$$

(iv) We have,

$$\begin{array}{r}
 0.5x \quad (0.8 - 0.2x) \quad 0.2 \quad 0.3x \\
 0.5x \quad 0.8 + 0.2x \quad 0.2 \quad 0.3x \\
 0.5x \quad 0.2x \quad 0.3x \quad 0.2 + 0.8 \\
 1.0x \quad 1.0 \\
 x \quad 1
 \end{array}$$

3. (i) We have,

$$\begin{array}{r}
 \frac{x - 2}{x - 2} = \frac{7}{3} \\
 3(x - 2) = 7(x - 2) \\
 \text{[cross multiplying]} \\
 3x - 6 = 7x - 14 \\
 6 - 14 = 7x - 3x \\
 20 = 4x \\
 5 = x
 \end{array}$$

(ii) We have

$$\begin{array}{r}
 \frac{2x - 5}{3x - 4} = 3 \\
 2x - 5 = 3(3x - 4) \\
 \text{[Cross multiplying]} \\
 2x - 5 = 9x - 12 \\
 2x - 9x = 12 - 5 \\
 7x = 7 \\
 x = 1
 \end{array}$$

(iii) We have,

$$\begin{array}{r}
 \frac{2x - 1}{3} = \frac{6x - 2}{5} = \frac{1}{3} \\
 5(2x - 1) = 3(6x - 2) = \frac{1}{3} \\
 15 = 18x - 6 \\
 10x - 5 = 18x - 6 \\
 15 = 18x - 6 \\
 8x - 1 = 5 \\
 8x = 4
 \end{array}$$

$$\begin{array}{r}
 x = \frac{4}{8} \\
 x = \frac{1}{2}
 \end{array}$$

(iv) We have,

$$\begin{array}{r}
 \frac{2x - 3}{5} = \frac{x - 3}{4} = \frac{4x - 1}{7} \\
 4(2x - 3) = 5(x - 3) = \frac{4x - 1}{7} \\
 20 = 5x - 15 \\
 8x - 12 = 5x - 15 \\
 3x = -3 \\
 x = -1
 \end{array}$$

(v) We have,

$$\begin{array}{r}
 \frac{(2x - 1)(2x - 3)}{(2x - 1)(x - 1)} = \frac{6}{7} \\
 \frac{2x - 1}{x - 1} = \frac{6}{7} \\
 7(2x - 1) = 6(x - 1) \\
 14x - 7 = 6x - 6 \\
 8x = 1 \\
 x = \frac{1}{8}
 \end{array}$$

(vi)

$$\begin{array}{r}
 \frac{(5x - 3)(4x - 2)}{(5x - 3)(x - 1)} = \frac{7}{4} \\
 \frac{5x - 3}{x - 1} = \frac{7}{4} \\
 4(5x - 3) = 7(x - 1) \\
 20x - 12 = 7x - 7 \\
 13x = 5 \\
 x = \frac{5}{13}
 \end{array}$$

$$\begin{array}{r}
 x \frac{3}{19} \\
 \text{(vii) } \frac{4x}{x-3} - \frac{12x-1}{3x-2} \\
 \frac{4x(3x-2) - (12x-1)(x-3)}{12x^2 - 8x - 12x^2 + 36x - x + 3} \\
 \frac{8x - 37x + 3}{29x - 3} \\
 x - \frac{3}{29}
 \end{array}$$

(viii) We have,

$$\begin{array}{r}
 \frac{3x-1}{3x-1} - \frac{2x-1}{2x-1} \\
 \frac{(3x-1)(2x-1) - (2x-1)(3x-1)}{6x^2 - 3x - 2x + 1 - 6x^2 + 2x - 3x + 1} \\
 \frac{x-1 - x+1}{2x-1-1} \\
 \frac{2x-0}{x-0}
 \end{array}$$

$$\begin{array}{r}
 \text{(ix) } \frac{x-2}{6} - \frac{11x-1}{3-4} - \frac{3x-4}{12} \\
 \frac{x-2}{6} - \frac{4(11x-1)-3}{12} - \frac{3x-4}{12} \\
 \frac{x-2}{6} - \frac{44-4x-3}{12} - \frac{3x-4}{12} \\
 \frac{x-2}{6} - \frac{4x-41}{12} - \frac{3x-4}{12} \\
 \frac{2(x-2) - 1(4x-41) - 3x+4}{12} \\
 \frac{2x-4-4x+41-3x+4}{12} \\
 \frac{6x-37-3x+4}{6x-3x-4-37} \\
 \frac{3x-33}{x-11}
 \end{array}$$

(x) We have,

$$\begin{array}{r}
 \frac{9x-7}{2} - x - \frac{x-2}{7} = 36 \\
 \frac{9x-7}{2} - \frac{7x-(x-2)}{7} = 36 \\
 \frac{9x-7}{2} - \frac{7x-x-2}{7} = 36
 \end{array}$$

$$\begin{array}{r}
 \frac{9x-7}{2} - \frac{6x-2}{7} = 36 \\
 \frac{7(9x-7) - 2(6x-2)}{14} = 36 \\
 \frac{63x-49-12x+4}{14} = 36 \\
 \frac{51x-45-36}{51x-45-504} = 36 \\
 \frac{5x-459}{x-9} = 36
 \end{array}$$

Exercise-8.2

1. Let the number be x

$$\begin{array}{r}
 x - \frac{x}{2} = 72 \\
 \frac{2x-x}{2} = 72 \\
 \frac{3x}{2} = 72 \\
 x = \frac{72 \times 2}{3} \\
 x = 24 \times 2 \\
 x = 48
 \end{array}$$

Number is 48

2. Let number be x

$$\begin{array}{r}
 x - \frac{2}{3}x = 55 \\
 \frac{3x-2x}{3} = 55 \\
 \frac{5x}{3} = 55 \times 3 \\
 x = \frac{55 \times 3}{5} \\
 x = 33
 \end{array}$$

Number is 33

3. Let number be x

$$\begin{array}{r}
 x - 21 = 71 - x \\
 x + x = 71 + 21 \\
 2x = 92 \\
 x = 46
 \end{array}$$

Number is 46

4. Let number be x

$$\begin{array}{r}
 x - \frac{2}{3}x = 20 \\
 \frac{3x-2x}{3} = 20 \\
 \frac{x}{3} = 20
 \end{array}$$

- $$\frac{x}{3} = 20$$
- $$x = 60$$
- Number is 60
5. Let number be x
- $$\frac{2}{3}x - \frac{1}{3}x = 3$$
- $$\frac{2x - 1x}{3} = 3$$
- $$x = 3 \times 3$$
- $$x = 9$$
- Number is 9
6. Let first odd number x
- Next " " $x + 2$
- $$x + (x + 2) = 76$$
- $$2x + 2 = 76$$
- $$2x = 74$$
- $$x = 37$$
- two consecutive odd numbers are 37 and 39.
7. Let first even number x
- 2nd " " $x + 2$
- 3rd " " $x + 4$
- Now, $x + (x + 2) + (x + 4) = 90$
- $$3x + 6 = 90$$
- $$3x = 90 - 6$$
- $$3x = 84$$
- $$x = 28$$
- Ist even number 28
- 2nd even number 28 + 2 = 30
- 3rd even number 28 + 4 = 32
8. Let breadth of rectangle x metres
- Length " " $(2x)$ metres
- Perimeter of rectangle 150
- $$2(l + b) = 150$$
- $$2[2x + x] = 150$$
- $$2(3x) = 150$$
- $$6x = 150$$
- $$x = 25$$
- breadth 25 metres
- and length 50 metres
9. Let third side of triangle x
- equal sides are $(2x - 5)$
- Perimeter of triangle 55
- $$x + (2x - 5) + (2x - 5) = 55$$
- $$5x - 10 = 55$$

- $$5x - 65 = 13$$
- third side of triangle 13 metres
- and equal sides of triangle
- $$2(13) - 5 = 26 - 5 = 21 \text{ metres}$$
10. Let Hari babu total property x
- given to his son $\frac{x}{3}$
- " " daughter $\frac{x}{4}$
- Remaining property $x - \frac{x}{3} - \frac{x}{4}$
- wife share $x - \frac{4x + 3x}{12}$
- $$x - \frac{7x}{12} = \frac{12x - 7x}{12}$$
- $$18000 = \frac{5x}{12}$$
- $$18000 \times 12 = 5x$$
- $$x = \frac{432000}{5} = ₹ 43200$$
- Total property of Hari babu ₹ 43200
11. Let present age of Raju's cousin x years
- " " " Raju $(x + 19)$
- After 5 years Cousin's age $x + 5$
- " " " Raju's age $(x + 19)$
- After 5 years cousin's age $x + 5$
- " " " Raju's age $(x + 19) + 5 = (x + 24)$
- Now, $\frac{x + 5}{x + 14} = \frac{3}{2}$ (given)
- $$2(x + 5) = 3(x + 14)$$
- $$2x + 10 = 3x + 42$$
- $$3x - 2x = 42 - 10$$
- $$x = 52$$
- Cousin's age 52 years
- Raju's age 52 + 19 = 33 years
12. Let age of son x years
- " " man $(x + 30)$ years
- After 12 years

Age of son $(x - 12)$ years
 " " man $(x - 30) - 12$
 $(x - 42)$ years
 Now age of man $3(\text{Age of son})$
 $x - 42 = 3(x - 12)$
 $x - 42 = 3x - 36$
 $42 - 36 = 3x - x$
 $6 = 2x$
 $3 = x$

Age of son 3 years
 " man 33 years

13. Let five years ago age of son x years
 " " " man $7x$ years

Present age of son $(x - 5)$ years
 Present age of man $(7x - 5)$ years
 After 5 years age of man $(7x - 10)$
 " " " " son $(x - 10)$
 Now age of man $3(\text{Age of son})$
 $7x - 10 = 3(x - 10)$
 $7x - 10 = 3x - 30$
 $4x = 20$
 $x = 5$

Present age of son $x - 5$
 $5 - 5$
 10 years
 " " " man $7x - 5$
 $7 - 5 = 2$
 40 years

14. Let denominator x

numerator $x - 4$
 Now, $\frac{(x - 4) - 1}{x - 1} = \frac{1}{2}$
 $\frac{x - 3}{x - 1} = \frac{1}{2}$
 $2x - 6 = x - 1$
 $2x - x = 6 - 1$
 $x = 5$
 denominator 5
 and numerator $7 - 4 = 3$
 fraction is $\frac{3}{5}$

15. Let unit place digit x
 ten's " " $8 - x$
 Now two digit number is $10(8 - x) + x$
 After reversing the digits two digit number is $10x + (8 - x)$

$[10(8 - x) + x] = 10(8 - x) + x$
 $(80 - 10x) + x = 80 - 9x$
 $80 - 9x = 10x + (8 - x)$
 $80 - 9x = 10x + 8 - x$
 $80 - 9x = 9x + 8$
 $80 - 8 = 9x + 9x$
 $72 = 18x$
 $x = 4$

unit place digit is 4
 and ten's place digit is $(8 - 4) = 4$
 two digit number is 44.

16. Let present age of Manoj x years

After 12 years age of Manoj $(x - 12)$
 4 years ago " " " $(x - 4)$
 $(x - 12) = 3(x - 4)$ [given]
 $x - 12 = 3x - 12$
 $x - 3x = -12 + 12$
 $-2x = 0$
 $x = 0$

Present age of Manoj 12 years

17. Let unit place digit x

ten's place digit $(9 - x)$
 two digit number $10(9 - x) + x$
 given,
 $[10(9 - x) + x] = 90 - 10x + x = 90 - 9x$
 $90 - 9x = 90 - 9x$
 $81 - 9x = 90 - 9x$
 $81 - 90 = 9x - 9x$
 $-9 = 0$
 $x = 0$

unit place digit 0
 ten's place digit $9 - 0 = 9$
 two digit number is 90

18. Let two numbers be $5x$ and $8x$

$\frac{5x - 2}{8x - 2} = \frac{2}{3}$ [given]
 $15x - 6 = 16x - 4$
 $15x - 16x = -4 + 6$
 $-x = 2$
 $x = -2$

Original numbers are 5, 2, 8, 2, 10, 16

19. Let share of Suman x

Suman share $4x$
 Deepti share $2x$
 Neha share $2x$

Now, Suman share + Deepti share + Neha share = ₹ 2100

$$\begin{array}{r}
 x \quad 4x \quad 2x \quad ₹ 21000 \\
 7x \quad 21000 \\
 x \quad 21000 \\
 x \quad \frac{21000}{7} \\
 x \quad ₹ 3000 \\
 \text{Suman share} \quad ₹ 3000 \\
 \text{Deepti share} \quad ₹ (4 \times 3000) \\
 \quad ₹ 12000 \\
 \text{Neha share} \quad 2 \times 3000 \\
 \quad ₹ 6000
 \end{array}$$

20. Let three numbers be $4x, 5x, 6x$

$$\begin{array}{r}
 6x \quad 4x \quad 5x \quad 55 \quad (\text{given}) \\
 10x \quad 5x \quad 55 \\
 5x \quad 55 \\
 x \quad 11 \\
 \text{Numbers are } 4 \times 11, 5 \times 11, 6 \times 11 \\
 44, 55, 66
 \end{array}$$

Exercise-9.1

1. (i) Supplement of 70° $180^\circ - 70^\circ = 110^\circ$
(ii) " " 135° $180^\circ - 135^\circ = 45^\circ$
(iii) " " 50° $180^\circ - 50^\circ = 130^\circ$
(iv) " " 120° $180^\circ - 120^\circ = 60^\circ$
(v) " " 90° $180^\circ - 90^\circ = 90^\circ$

2. (i) Complement of 55° $90^\circ - 55^\circ = 35^\circ$
(ii) " " 73° $90^\circ - 73^\circ = 17^\circ$
(iii) " " 45° $90^\circ - 45^\circ = 45^\circ$
(iv) " " 40° $90^\circ - 40^\circ = 50^\circ$
(v) " " 30° $90^\circ - 30^\circ = 60^\circ$

3. Let the complementary angles be $7x, 11x$

$$\begin{array}{r}
 7x \quad 11x \quad 90 \\
 18x \quad 90 \\
 x \quad 5 \\
 \text{Complementary angles are} \\
 7 \times 5, 11 \times 5 \\
 35^\circ, 55^\circ
 \end{array}$$

4. Let supplementary angles be $2x, 7x$

$$\begin{array}{r}
 2x \quad 7x \quad 180 \\
 9x \quad 180 \\
 x \quad 20 \\
 \text{Supplementary angles are} \\
 2 \times 20, 7 \times 20 \\
 40^\circ, 140^\circ
 \end{array}$$

5. Let the angles be x
Its complementary $90^\circ - x$

given, $x + \frac{1}{2}(90^\circ - x) = 30^\circ$

$$\begin{array}{r}
 x \quad 45 \quad \frac{x}{2} \quad 30 \\
 x \quad 75 \quad \frac{x}{2}
 \end{array}$$

$$x + \frac{x}{2} = 75$$

$$\frac{3x}{2} = 75$$

$$x = \frac{75 \times 2}{3} = 50$$

angles 50°

6. Let smaller angle x

larger angle $3x - 15$

$$x + (3x - 15) = 135$$

$$4x - 15 = 135$$

$$4x = 120$$

$$x = 30$$

smaller angle 30°

larger angle $3 \times 30 - 15 = 105^\circ$

7. Let smaller angle x

larger angle $3x - 20$

$$x + (3x - 20) = 180$$

$$4x - 20 = 180$$

$$4x = 200$$

$$x = 50$$

smaller angle 50°

larger angle 130°

8. (i) $x + y + z = 180$ (straight line)

$$55^\circ + y + 66^\circ = 180$$

$$121^\circ + y = 180$$

$$y = 180 - 121$$

$$y = 59^\circ$$

(ii) $x + y + z = 180$ (straight line)

$$35^\circ + 2x + z = 180$$

$$35^\circ + 2(35^\circ) + z = 180$$

$$35^\circ + 70^\circ + z = 180$$

$$105^\circ + z = 180$$

$$z = 180 - 105$$

$$z = 75^\circ$$

(iii) Let $x = 3k, y = 5k, z = 7k$

$$x + y + z = 180 \quad \text{straight line}$$

$$3k + 5k + 7k = 180$$

$$15k = 180$$

$$\begin{array}{r}
 k \quad 12 \\
 x \quad 3 \quad 12, y \quad 5 \quad 12, z \quad 7 \quad 12 \\
 x \quad 36 \quad y \quad 60 \quad z \quad 84 \\
 \text{9. We have, } (2x - 5) + 3x = 180 \text{ straight line} \\
 5x = 180 \\
 5x = 175 \\
 x = 35 \\
 \text{Angles are } (2 \times 35 - 5), 3 \times 35 \\
 75^\circ, 105^\circ
 \end{array}$$

10. We have,

$$\begin{array}{r}
 AOC + BOC = 180 \quad (\text{straight line}) \\
 (3b - 10) + 2a = 180 \\
 2a + 3b = 180 + 10 \\
 2a + 3b = 190 \quad \dots(1) \\
 4a + 3b = 20 \quad \dots(2) \text{ [given]}
 \end{array}$$

Adding (1) and (2)

$$\begin{array}{r}
 6a + 3b = 210 \\
 6a + 3b = 20 \\
 a = 35
 \end{array}$$

Put in (2)

$$\begin{array}{r}
 4 \times 35 + 3b = 20 \\
 140 + 3b = 20 \\
 140 + 20 = 3b \\
 160 = 3b \\
 40 = b \\
 a = 35, b = 40
 \end{array}$$

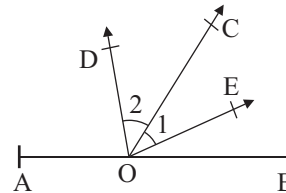
$$\begin{array}{r}
 BOC = 2a + 2 \times 35 \\
 BOC = 70 \\
 \text{and } AOC = 3b - 10 \\
 3 \times 40 - 10 \\
 120 - 10 \\
 AOC = 110
 \end{array}$$

11. $BOD + BOE + COE = 180$
 $40 + (x - 5) + (3x - 7) = 180$
 (straight line)

$$\begin{array}{r}
 4x = 180 - 35 \\
 4x = 145 \\
 4x = 128 \\
 x = 32 \\
 \text{(i) } AOC = 180 - (COE + BOE) \\
 180 - [(3x - 7) + (x - 5)] \\
 180 - [4x - 12] \\
 180 - [4 \times 32 - 12] \\
 180 - [128 - 12] \\
 180 - 116 \\
 AOC = 64
 \end{array}$$

$$\begin{array}{r}
 \text{(ii) } AOD = 180 - 40 \\
 140 \\
 \text{(iii) } COE = 3x - 7 \\
 3 \times 40 - 7 \\
 COE = 113
 \end{array}$$

12. Given : OD, OE are bisectors of AOC and BOC



To prove : $\angle DOE = 90^\circ$

$$\begin{array}{r}
 \text{(1) } AOC + BOC = 180 \quad \text{straight line} \\
 \text{(2) } \frac{1}{2} AOC + \frac{1}{2} BOC = 90 \quad \text{bisector} \\
 \frac{1}{2} (AOC + BOC) = 90 \\
 \angle DOE = \frac{180}{2}
 \end{array}$$

or $\angle DOE = 90^\circ$

13. (i) $\therefore \angle AOB + \angle COB = 180$
 straight line

$$\begin{array}{r}
 70 + x = 180 \\
 x = 110
 \end{array}$$

(ii) $\angle POQ + \angle ROQ = 180$
 straight line

$$\begin{array}{r}
 3x + 2x = 180 \\
 5x = 180 \\
 x = 36
 \end{array}$$

(iii) $\angle LON + \angle NOP + \angle MOP = 180$

$$\begin{array}{r}
 35 + x + 60 = 180 \\
 x + 95 = 180 \\
 x = 180 - 95 \\
 x = 85
 \end{array}$$

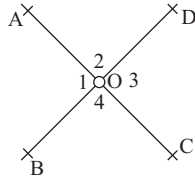
(iv) $\angle AOB + \angle BOC + \angle COD$
 $\angle DOE + \angle AOE = 360$

$$\begin{array}{r}
 47 + x + 83 + 92 + 75 = 360 \\
 x + 297 = 360 \\
 x = 360 - 297 \\
 x = 63
 \end{array}$$

(v) $\angle POQ + \angle QOR + \angle ROS$
 $\angle SOP = 360$

$$\begin{array}{r} x + 2x + 3x + 2x = 360 \\ 8x = 360 \\ x = 45 \end{array}$$

14. Given,



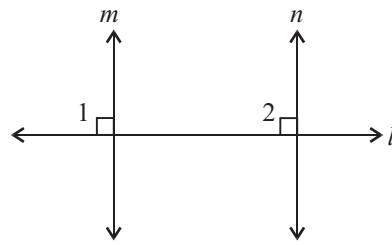
$$\begin{array}{r} 1 = 48 \\ \text{To find : } 2, 3, 4 \\ \therefore 1 + 2 = 180 \\ 48 + 2 = 180 \\ 2 = 180 - 48 \\ 2 = 132 \\ 3 = 1 = 48 \\ \text{Vertically opposite angles} \\ 4 = 2 = 132 \\ \text{Vertically opposite angles} \end{array}$$

15. Given : $\angle COE = 90^\circ$

- (i) Linear pairs $(5, 1), (5, 4)$
- (ii) Supplementary angles $(5, 1), (5, 4)$
- (iii) Vertically opposite angles $(1, 4)$
- (iv) Complementary angles $(1, 2)$

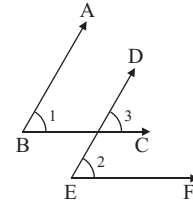
Exercise-9.2

1. We have, $1 = 65$
 $\therefore 1 + 2 = 180$ Linear pair
 $65 + 2 = 180$
 $2 = 115$
 $5 = 1 = 65$ Corresponding angles
 $6 = 2 = 115$ V.O.A.
 $3 = 1 = 65$
 $4 = 2 = 115$
 $8 = 4 = 115$ Corresponding angles
 $7 = 3 = 65$
2. We have,



$$\begin{array}{r} 1 = 90, 2 = 90 \\ 1 = 2 \\ m \parallel n \\ \text{(corresponding angles are equal)} \end{array}$$

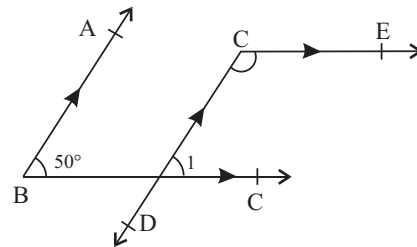
3. We have,



$$\begin{array}{r} 1 = 75 \\ \therefore 3 = 1 = 75 \\ \text{(Corresponding angles)} \\ 2 = 3 = 75 \end{array}$$

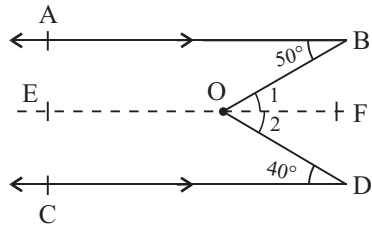
4. $(2x + 3) + (3x + 2) = 180$
 cointerior angles are supplementary
 $5x + 5 = 180$
 $5x = 185$
 $x = 37$

5. Given, $AB \parallel CD, BC \parallel CE$



$$\begin{array}{r} 1 = 50 \text{ Corresponding angles} \\ 1 + \angle CED = 180 \\ \text{Co-interior angles are supplementary} \\ 50 + \angle CED = 180 \\ \angle CED = 130 \end{array}$$

6. Draw a line EOF parallel to AB and CD



$$\begin{array}{l} 1 = 50 \\ 2 = 40 \end{array} \text{ alternate angles}$$

$$BOD = 1 + 2$$

$$= 50 + 40$$

$$BOD = 90$$

7. a 65 Vertically opposite angles

$$\begin{array}{l} \therefore a + b = 180 \\ 65 + b = 180 \quad \text{co-interior angles} \\ b = 180 - 65 \\ b = 115 \\ b + c = 180 \\ 115 + c = 180 \\ c = 180 - 115 \\ c = 65 \\ c + d = 180 \\ 65 + d = 180 \\ d = 180 - 65 \\ d = 115 \end{array}$$

8. $x = 70$ corresponding angles

$$y = 70 \text{ alternate angles}$$

9. $x = 70$ alternate angles

$$y = 70 \text{ corresponding angles}$$

$$x = 60 \text{ alternate angles}$$

10. $y = 50$

11. $x = 125$ 180 Linear pair

$$x = 180 - 125$$

$$x = 55$$

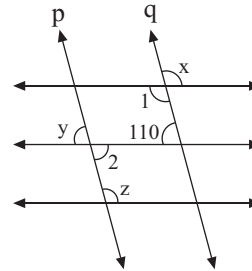
$x + y = 180$ co-interior angles

$$55 + z = 180$$

$$z = 180 - 55$$

$$z = 125$$

12.



$$y = 110 \text{ corresponding angles}$$

$$1 = x \text{ vertically opposite angles}$$

$$1 + 110 = 180 \text{ co-interior angles}$$

$$x + 110 = 180$$

$$x = 70$$

$$2 = y$$

Vertically opposite angles

$$2 + z = 180 \text{ Co-interior angles}$$

$$y + z = 180$$

$$110 + z = 180$$

$$z = 70$$

13. $b = 45$ alternate angles

$$a = 35 \text{ alternate angles}$$

10

Triangles and Their Properties

Exercise-10.1

1. (i) $x = 45$ 55 180

Sum angle property of triangle

$$x + 100 = 180$$

$$x = 80$$

(ii) $x = 90$ 60 180

$$x + 150 = 180$$

$$x = 30$$

(iii) $x = 40$ 105 180

$$x + 145 = 180$$

$$x = 180 - 145$$

$$x = 35$$

(iv) $x + x + x = 180$

sum angle property of triangle

$$3x = 180$$

$$x = 60$$

(v) $2x + x = 90$ x

(sum angle property of triangle)

$$3x = 90$$

$$x = 30$$

$$\begin{array}{r}
 \text{(vi) } 70 \quad x \quad x \quad 180 \\
 \quad \quad 70 \quad 2x \quad 180 \\
 \quad \quad \quad 2x \quad 110 \\
 \quad \quad \quad \quad x \quad 55
 \end{array}$$

2. (i) ACD A B
 Exterior angle equal to sum of interior opposite angles

$$\begin{array}{r}
 x \quad 60 \quad 50 \\
 x \quad 110 \\
 x \quad y \quad 180 \quad \text{(Linear pair)} \\
 110 \quad y \quad 180 \\
 \quad \quad y \quad 70
 \end{array}$$

(ii) PRD P Q

$$\begin{array}{r}
 110 \quad y \quad 40 \\
 110 \quad 40 \quad y \\
 80 \quad y \\
 x \quad 110 \quad 180 \quad \text{(Linear pair)} \\
 \quad \quad x \quad 70
 \end{array}$$

(iii) x 70 (vertically opposite angles)
 x 60 y 180
 (sum angle property of triangle)
 70 60 y 180
 130 y 180
 y 50

(iv) SRP P Q
 Exterior angle equal to sum of interior opposite angles

$$\begin{array}{r}
 x \quad 90 \quad 30 \\
 x \quad 120 \\
 y \quad 180 \quad x \quad \text{Linear pair} \\
 180 \quad 120 \\
 y \quad 60
 \end{array}$$

(v) 140 90 x
 Exterior angle equal to sum of interior opposite angles

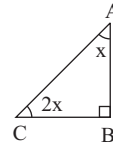
$$\begin{array}{r}
 140 \quad 90 \quad x \\
 50 \quad x \\
 y \quad 140
 \end{array}$$

Vertically opposite angles

3. Let angles of triangle be $4x$, $3x$, $2x$
- $$\begin{array}{r}
 4x \quad 3x \quad 2x \quad 180 \\
 \text{(sum angle property of triangle)} \\
 9x \quad 180 \\
 x \quad 20 \\
 \text{angles of triangle are} \\
 4 \quad 20, 3 \quad 20, 2 \quad 20 \\
 80, 60, 40
 \end{array}$$

4. Let acute angles be $2x$, $1x$

$$\begin{array}{r}
 x \quad 2x \quad 90 \quad 180 \\
 3x \quad 90 \quad 180 \\
 3x \quad 90 \\
 x \quad 30
 \end{array}$$



Acute angles are 30 , $2 \quad 30$ 30 , 60

5. Let equal angles of triangle be x

$$\begin{array}{r}
 x \quad x \quad 100 \quad 180 \\
 2x \quad 180 \quad 100 \\
 2x \quad 80 \\
 x \quad 40
 \end{array}$$

equal angles are 40 , 40

6. \therefore sum of exterior angles of triangle

$$\begin{array}{r}
 360 \\
 (3x \quad 5) \quad (2x \quad 27) \quad (3x \quad 24) \quad 360 \\
 8x \quad 8 \quad 360 \\
 8x \quad 352 \\
 x \quad 44
 \end{array}$$

7. Let $2 \quad A \quad 3 \quad B \quad 6 \quad C \quad k$

$$A \quad \frac{k}{2}, \quad B \quad \frac{k}{3}, \quad C \quad \frac{k}{6}$$

$$\therefore \quad A \quad B \quad C \quad 180 \\
 \frac{k}{2} \quad \frac{k}{3} \quad \frac{k}{6} \quad 180 \\
 \frac{3k \quad 2k \quad k}{6} \quad 180$$

$$\frac{6k}{6} \quad 180$$

$$k \quad 180$$

$$A \quad \frac{180}{2}, \quad B \quad \frac{180}{3}, \quad C \quad \frac{180}{6}$$

$$A \quad 90, \quad B \quad 60, \quad C \quad 30$$

8. Let interior opposite angles be $2x$, $3x$

$$\therefore \quad \text{Exterior angle} \quad \text{sum of interior opposite angles}$$

$$100 \quad 2x \quad 3x$$

$$100 \quad 5x$$

$$20 \quad x$$

Interior opposite angles

$$2 \quad 20, 3 \quad 20$$

$$40, 60$$

third angle 180 (40 60)

$$80$$

9. Let a cute angle be $1x$ and $4x$

$$\therefore \quad \text{sum of all angles of triangle} \quad 180$$

$$1x \quad 4x \quad 90 \quad 180$$

$$15x \quad 180 \quad 90$$

$$\begin{array}{r}
 15x = 90 \\
 x = 6 \\
 \text{Acute angles } 11, 6, 4, 6, 66, 24 \\
 \therefore \angle F = \angle B = \angle C = 180 \\
 50 + 30 + z = 180 \\
 80 + z = 180 \\
 z = 100 \\
 y = 30; z = x = 100
 \end{array}$$

11. (i) Exterior angle = sum of interior angle

$$\begin{array}{r}
 \angle DAC = \angle B + \angle C \\
 107 = x + 57 \\
 50 = x
 \end{array}$$

(ii) In $\triangle CAD$

$$\begin{array}{r}
 x + 45 + 105 = 180 \\
 x + 150 = 180 \\
 180 - 150 = x \\
 x = 30 \\
 x + 65 + y = 180 \\
 30 + 65 + y = 180 \\
 95 + y = 180 \\
 y = 180 - 95 \\
 y = 85
 \end{array}$$

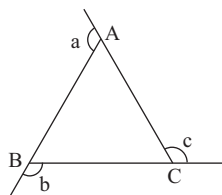
(Linear pair)

12. $\angle ACD = \angle A + \angle B$
(Exterior angle = to sum of interior opposite angles)

$$\begin{array}{r}
 \angle ACD = 25 + 100 \\
 \angle ACD = 125 \\
 \text{Similarly, } \angle ACD = \angle D + \angle ACD \\
 20 + 125 = \angle ACD \\
 \angle AED = 145
 \end{array}$$

13. $\angle C = \angle A$
(Exterior angle property)
 $18 + 50 = y + 68$
 $x + y = \angle D$
(Exterior angle property)
 $68 + 35 = x + 103$

14. To prove: $a + b + c = 360$



$$\begin{array}{r}
 a = 180 - \angle A \\
 b = 180 - \angle B \\
 c = 180 - \angle C
 \end{array}$$

Linear pair

adding all three steps

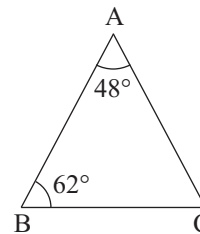
$$\begin{array}{r}
 a + b + c = 180 + 180 + 180 \\
 = 540 - (\angle A + \angle B + \angle C) \\
 = 540 - 180 \\
 = 360
 \end{array}$$

or sum of exterior angles of triangle is equal to 360° .

15. (a) No a triangle cannot have two right angles.
(b) No, a triangle can not have two obtuse angles.
(c) Yes, a triangle have two acute angles.
(d) No a triangle cannot have all angles greater than 60° .
(e) No a triangle cannot have all angles less than 60° .
(f) Yes a triangle have all angles equal to 60°

Exercise-10.2

1.



$$\begin{array}{r}
 \therefore \angle A + \angle B + \angle C = 180 \\
 48 + 62 + \angle C = 180 \\
 110 + \angle C = 180 \\
 \angle C = 70
 \end{array}$$

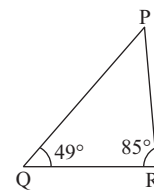
Largest side AB ($\because \angle C$ is largest)
smallest side BC ($\because \angle A$ is smallest)

2. $\angle P + \angle Q + \angle R = 180$

$$\begin{array}{r}
 \angle P = 49 + 85 = 134 \\
 \angle P + \angle Q = 180 \\
 \angle P = 180 - 134 \\
 \angle P = 46
 \end{array}$$

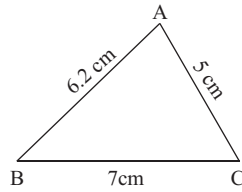
PQ is largest side

($\because \angle R$ is largest)



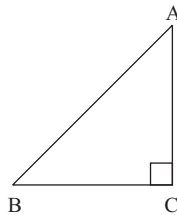
QR is smallest side
 $(\because P$ is smallest)
 Ascending order of side are
 $QR < PR < PQ$

3.



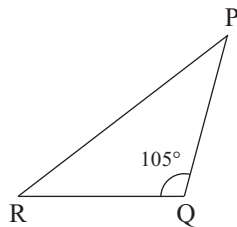
A is largest $\because BC$ is largest
 B is smallest $\because AC$ is smallest
 descending order of angles
 $A > C > B$

4. If $C = 90^\circ$



AB is longest because in right angled triangle 90° is largest angle and side opposite to it longest.

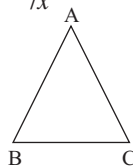
5. $\because Q = 105^\circ$



PR is longest because in obtuse angled triangle obtuse angle is largest angle and side opposite to it is longest.

6. We have, $A : B : C = 3 : 5 : 7$

Let $A = 3x, B = 5x, C = 7x$
 $3x + 5x + 7x = 180$
 $15x = 180$
 $x = 12$
 $A = 36, B = 60, C = 84$

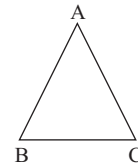


$B = 5, C = 7, A = 36$
 $B = 60, C = 84$
 AB is longest $\because C$ is largest
 BC is smallest A is smallest

7. We have,

$AB : BC : CA = 3 : 8 : 5$

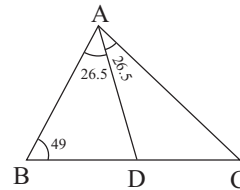
A is largest
 $(\because BC$ is longest)
 C is smallest AB is smallest



8. $A = 180 - 100 = 80$ Linear pair
 $C = 180 - 135 = 45$ Linear pair

$\therefore A = 80, B = 125, C = 45$
 $AB < AC < BC \therefore C < B < A$

9.



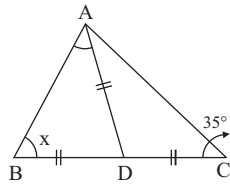
$\angle BAD = \angle CAD = \frac{A}{2}$ bisector
 $\frac{53}{2} = 26.5$

$A = 53, B = 49, C = 180 - 102 = 78$
 $\angle ADC = 26.5 + 49 = 75.5$

Exterior angle $\angle ADC$ = sum of interior opposite angle

In $\triangle ADC$
 $\angle DAC = 26.5, \angle C = 78, \angle ADC = 75.5$
 Descending order of sides in $\triangle ADC$
 $AD > AC > DC$
 $\therefore ADC < C < DAC$

$$\begin{aligned}
 10. \quad & \frac{AD}{AB} = \frac{DC}{AC} = \frac{35}{70} \quad \therefore AD = DC \\
 & \frac{AD}{AB} = \frac{DC}{AC} = \frac{35}{70} \\
 & \frac{AD}{AB} = \frac{DC}{AC} = \frac{35}{70}
 \end{aligned}$$



Let $\angle BAD = \angle DBA = x$
 (angles opposite to equal sides)

In $\triangle ABD$

$$\begin{aligned}
 x + x + 70 &= 180 \\
 2x &= 110 \\
 x &= 55
 \end{aligned}$$

$\frac{AC}{AB} = \frac{DC}{AD} \therefore \frac{AC}{AD} = \frac{DC}{AB}$

Exercise-10.3

1. (a) $MN^2 + LM^2 = LN^2$
 (Pythagoras theorem)

$$\begin{aligned}
 14^2 + 48^2 &= 50^2 \\
 196 + 2304 &= 2500 \\
 MN^2 + (50)^2 &= 50^2 \\
 MN &= 50 \text{ cm}
 \end{aligned}$$

(b) $AC^2 + AB^2 = BC^2$
 (Pythagoras theorem)

$$\begin{aligned}
 15^2 + 8^2 &= 17^2 \\
 225 + 64 &= 289 \\
 AC^2 + 17^2 &= 17^2 \\
 AC &= 17 \text{ cm}
 \end{aligned}$$

(c) $XY^2 + XZ^2 = YZ^2$
 (Pythagoras theorem)

$$\begin{aligned}
 26^2 + XZ^2 &= 24^2 \\
 676 + XZ^2 &= 576 \\
 676 - 576 &= XZ^2 \\
 100 &= XZ^2
 \end{aligned}$$

$$\begin{aligned}
 & 10^2 + XZ^2 = 24^2 \\
 & 100 + XZ^2 = 576 \\
 & XZ^2 = 576 - 100 \\
 & XZ^2 = 476 \\
 & XZ = \sqrt{476} \approx 21.8 \text{ cm}
 \end{aligned}$$

(d) $DF^2 + DE^2 = EF^2$

$$\begin{aligned}
 37^2 + DE^2 &= 12^2 \\
 1369 + DE^2 &= 144 \\
 1369 - 144 &= DE^2 \\
 1225 &= DE^2 \\
 35^2 &= DE^2 \\
 35 \text{ cm} &= DE
 \end{aligned}$$

(e) $AB^2 + AC^2 = BC^2$
 (Pythagoras theorem)

$$\begin{aligned}
 (4.5)^2 + 6^2 &= BC^2 \\
 20.25 + 36 &= BC^2 \\
 56.25 &= (7.5)^2 \\
 AB &= 7.5 \text{ cm}
 \end{aligned}$$

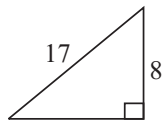
(f) $PR^2 + QP^2 = QR^2$
 (Pythagoras Theorem)

$$\begin{aligned}
 (10.1)^2 + QP^2 &= (9.9)^2 \\
 102.01 + QP^2 &= 98.01 \\
 102.01 - 98.01 &= QP^2 \\
 4 &= QP^2 \\
 2^2 &= QP^2 \\
 2 \text{ cm} &= QP
 \end{aligned}$$

2. (i) We have sides 2, 3, 4
 $\therefore 2^2 + 3^2 = 4^2$
 2, 3, 4 can be the sides of triangle.
- (ii) We have sides 5, 7, 12
 $\therefore 5^2 + 7^2 \neq 12^2$
 5, 7, 12 cannot be the sides of triangle.
- (iii) We have sides 3.4, 2.1, 5.3
 $\therefore 3.4 + 2.1 > 5.3$, $3.4 + 5.3 > 2.1$,
 $2.1 + 5.3 > 3.4$
 3.4, 2.1, 5.3 can be the sides of triangle

- (iv) We have sides 2.5, 1.3, 4
 $\therefore 2.5 + 1.3 < 4$
 2.5, 1.3, 4 can not be sides of triangle.
- (v) We have sides 16, 7, 8
 $\therefore 16 + 7 > 8, 16 + 8 > 7$ and $7 + 8 < 16$
 16, 7, 8 cannot be the sides of triangle.
- (vi) We have sides 8.5, 16.3, 4.9
 $\therefore 8.5 + 16.3 > 4.9,$
 $8.5 + 4.9 < 16.3$
 8.5, 16.3, 4.9 can not be sides of triangle.

3. $\therefore (\text{Hypotenuse})^2 = (\text{Ist side})^2 + (\text{other side})^2$



$$17^2 = 8^2 + (\text{2nd side})^2$$

$$289 = 64 + (\text{2nd side})^2$$

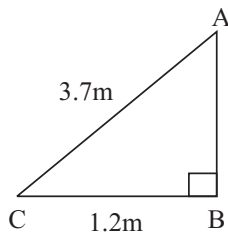
$$289 - 64 = (\text{2nd side})^2$$

$$225 = (\text{2nd side})^2$$

$$15^2 = (\text{2nd side})^2$$

other side is 15 cm

4. AC is ladder and AB is wall



$$\therefore AC^2 = AB^2 + BC^2$$

$$(3.7)^2 = AB^2 + (1.2)^2$$

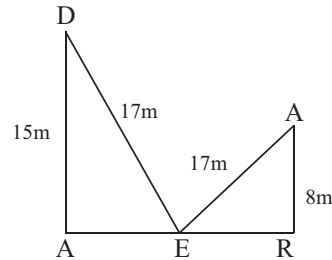
$$13.69 = AB^2 + 1.44$$

$$12.25 = AB^2$$

$$(3.5)^2 = AB^2$$

ladder will reach upto 3.5m on the wall.

5. A and D are windows BC is street



In $\triangle AEB$,

$$17^2 = 15^2 + BE^2$$

$$289 = 225 + BE^2$$

$$64 = BE^2$$

$$8 = BE$$

In $\triangle DCE$

$$17^2 = 15^2 + CE^2$$

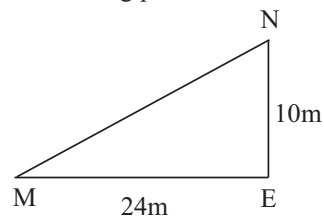
$$289 = 225 + CE^2$$

$$64 = CE^2$$

$$8 = CE$$

Width of street $CE + BE$
 $8 + 8 = 16$
 16 m

6. Let M is starting point



$$MN^2 = ME^2 + NE^2$$

$$MN^2 = 24^2 + 10^2$$

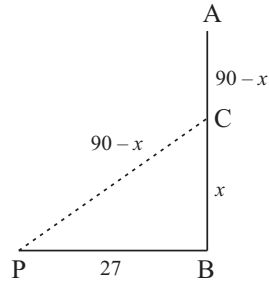
$$MN^2 = 576 + 100$$

$$MN^2 = 676$$

$$MN = 26$$

Man is 26m away from starting point

7. Let AB is plant broken at C touches the ground at P .

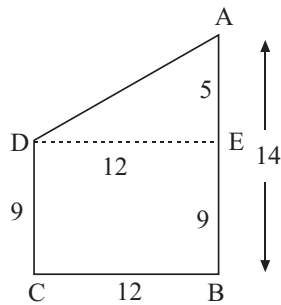


Let from x cm from the ground it is broken.

$$\begin{aligned} \therefore \frac{AC}{PC^2} &= \frac{PC}{BC^2} = \frac{90-x}{PB^2} \\ (90-x)^2 &= x^2 + 27^2 \\ 8100 - 180x + x^2 &= x^2 + 729 \\ 8100 - 180x &= 729 \\ 7371 &= 180x \\ 40.95 &= x \end{aligned}$$

Plant is broken 40.95 cm from the ground

8. Let AB and CD are two poles
Draw $DE \parallel AB$



$$\begin{aligned} DE &= BC = 12 \\ BE &= DC = 9 \\ AE &= 14 - 9 = 5 \\ \text{In } \triangle ADE \\ AD^2 &= DE^2 + AE^2 \\ &= 12^2 + 5^2 \end{aligned}$$

$$\begin{aligned} 169 &= AD^2 + 13^2 \\ AD &= 13 \end{aligned}$$

Distance between their tops is 13 cm.

9. In $\triangle ADC$

$$\begin{aligned} AC^2 &= AD^2 + DC^2 \\ 25^2 &= 15^2 + DC^2 \\ 625 &= 225 + DC^2 \\ 400 &= DC^2 \\ 20^2 &= DC^2 \end{aligned}$$

$$\begin{aligned} DC &= 20 \text{ cm} \\ BD &= 28 - 20 = 8 \text{ cm} \end{aligned}$$

- In $\triangle ABD$

$$\begin{aligned} AB^2 &= AD^2 + BD^2 \\ AB^2 &= 15^2 + 8^2 \\ &= 225 + 64 \\ &= 289 \\ AB &= 17^2 \\ AB &= 17 \text{ cm} \end{aligned}$$

10. In $\triangle ABC$

$$\begin{aligned} AC^2 &= AB^2 + BC^2 \\ 20^2 &= (4\sqrt{11})^2 + BC^2 \\ 400 &= 16 + 11BC^2 \\ 400 &= 176 + 11BC^2 \\ 576 &= 11BC^2 \end{aligned}$$

$$\begin{aligned} AC^2 &= 24^2 \\ AC &= 24 \text{ cm} \end{aligned}$$

- In $\triangle CDE$

$$\begin{aligned} CE^2 &= DE^2 + CD^2 \\ 6^2 &= 8^2 + CD^2 \\ 36 &= 64 + CD^2 \end{aligned}$$

$$CE^2 = 100$$

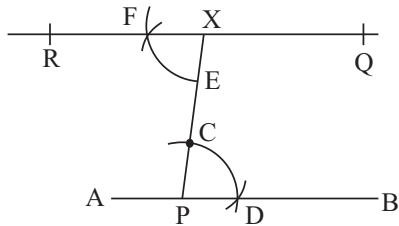
$$CE^2 = 10^2$$

$$CE = 10 \text{ cm}$$

$$\begin{aligned} \therefore AE^2 &= 26^2 = 676 \\ AC^2 &= CE^2 + AE^2 = 100 + 676 \\ AC^2 &= AC^2 + CE^2 \\ ACE &= 90 \end{aligned}$$

Exercise-11.1

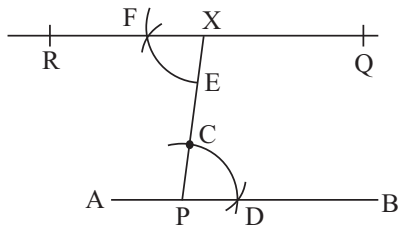
1. (i) Steps of Construction



- (1) Draw AB 5 cm.
- (2) Take any point X outside of AB .
- (3) Join X with AB at a point P .
- (4) At P draw an arc of any radius meeting XP at C and D .
- (5) At X draw an arc with same radius meeting PX at E .
- (6) With E as centre and radius CD cut the previous arc at F .
- (7) Draw a line passing through F and X call it RQ .

$$RQ \parallel AB$$

2. Steps of constructions

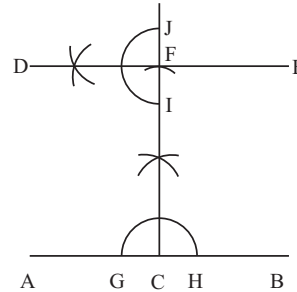


- (1) Draw PQ 6.3
- (2) Take any point X outside it.
- (3) Join X with PQ at E .
- (4) With E as centre and any radius draw an arc cutting XE at A and B .
- (5) With X as centre and same radius draw an arc cutting XC at C .
- (6) With C as centre and radius AB cut previous arc at D .

- (7) Join XD and produce it to form line RS

$$RS \parallel PQ$$

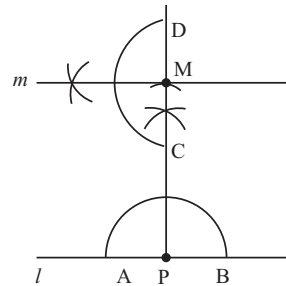
3. Steps of constructions



- (1) Draw any line AB .
- (2) Take any point C on it.
- (3) Draw perpendicular at C .
- (4) With C as centre and radius equal to 5 cm cut an arc on perpendicular at F .
- (5) At F draw perpendicular and produce it to form line DE .

$$DE \parallel AB$$

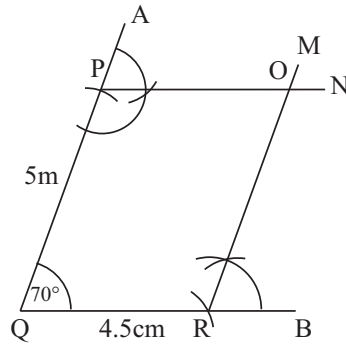
4. Steps of constructions :



- (1) Draw a line AB .
- (2) Take any point P on it.
- (3) With P as centre and radius equal to 3 cm cut an arc on the perpendicular.
- (4) At M draw perpendicular and produce it to form a line m .

$$m \perp AB$$

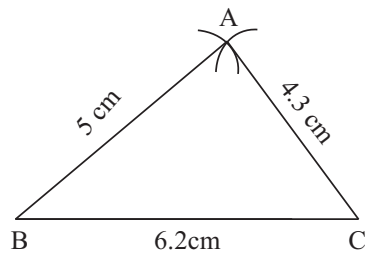
5. Steps of constructions :



- (1) draw $\angle AOB = 70^\circ$
- (2) With Q as centre and radius equal to 4.5 cm cut on arc R on QB .
- (3) With Q as and radius equal to 5 cm cut an arc P on QA .
- (4) At R draw $MRB = \angle AQB$
- (5) At R draw $APN = \angle PQB$ meeting previous MRB at O .
 $PM = QR = 4.5$ cm
 $OR = QP = 5$ cm
 $(\because QROP \text{ is a parallelogram})$

Exercise-11.2

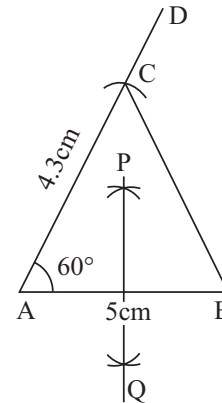
1. Steps of construction :



- (1) Draw $BC = 6.2$ cm
- (2) With C as centre and radius 4.3 cut an arc.
- (3) With B as centre and radius 5 cm cut the previous arc at A .
- (4) Join AB and AC
 ABC is required triangle.

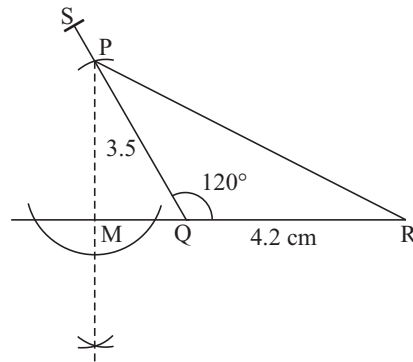
2. Steps of construction :

- (1) Draw $AB = 5$ cm
- (2) At A draw $\angle DAB = 60^\circ$
- (3) With A as centre and radius 4.3 cm cut the AD at C .



- (4) Join BC
 ABC is required triangle
- (5) With A as centre and radius more than half of AB cut two arcs.
- (6) With B as centre and same radius cut the previous arcs at P and Q .
- (7) Join PQ which is required perpendicular bisector.

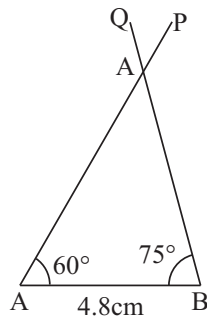
3. Steps of construction :



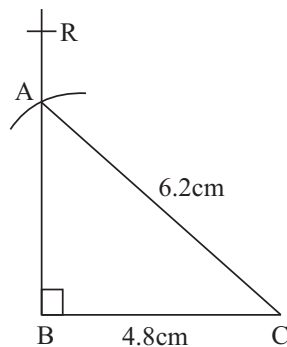
- (1) Draw $QR = 4.2$ cm
- (2) At Q draw $\angle SQR = 120^\circ$
- (3) With Q as centre and radius 3.5 cm cut an arc QS . Join PR
 PQR is required triangle.

4. Steps of construction

- (1) Draw BC 4.8 cm
 - (2) At B draw PBC 60°
 - (3) At C draw QCB 75°
- Meeting previous angle at A
 ABC is required triangle.

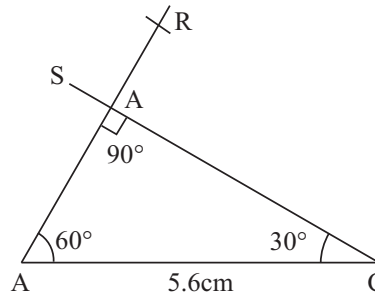


5. Step of construction :



- (1) Draw BC 4.8 cm
 - (2) At B draw B 90°
 - (3) With C as centre and radius 6.2 cm cut BR at A .
 - (4) Join AC
- ABC is required triangle.

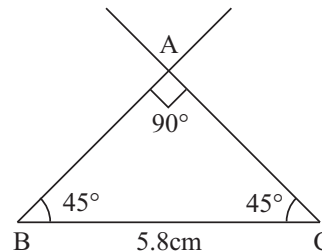
6. If one acute angle of right angled triangle is 30° then other acute angle is 60° .



Steps of construction

- (1) Draw BC 5.6 cm
 - (2) At B draw RBC 60°
 - (3) At C draw SCB 30°
- Meeting previous angle at A
 ABC is required triangle.

7. Each acute angle of right angled triangle is 45°



Steps of construction :

- (1) Draw BC 5.8 cm
 - (2) At B and C draw angle 45° each meeting each other at A .
- ABC is required isosceles right angled triangle.

12

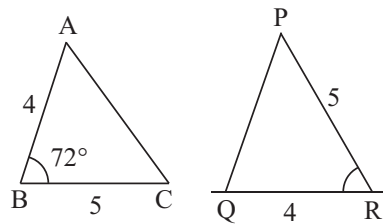
Congruence

Exercise-12

1. (i) Yes the triangles are congruent by SSS congruence condition.
- (ii) Yes the triangles are congruent by ASA congruence condition.
- (iii) No the triangles are not congruent.
- (iv) Yes the triangles are congruent by ASA congruence condition.

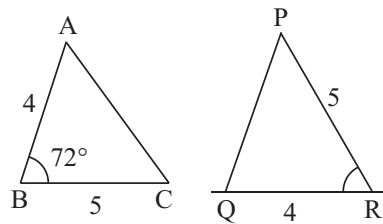
- (v) No the triangles are not congruent.
- (vi) Yes the triangles are congruent by ASA congruence condition.

2. (i) Yes $\triangle ABC \cong \triangle PRQ$ by SAS

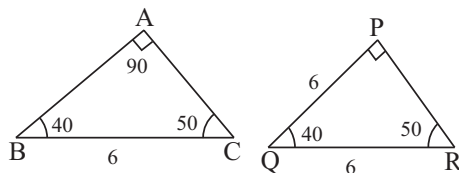


$\therefore AB = PR, \angle B = \angle R, BC = QR$

(ii) Same as (i)

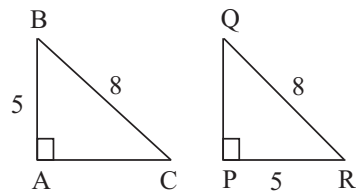


(iii) $\angle B = 180 - (90 + 50) = 40$



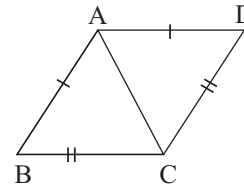
No the triangles are not congruent.

(iv) Yes $\triangle ABC \cong \triangle PRQ$ By RHS



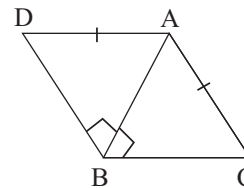
$\therefore \angle A = \angle P, BC = QR, AB = PR$

(v) Figure is according to given condition



Yes, $\triangle ABC \cong \triangle ADC$ (By sss)
 $\therefore AB = AD, BC = DC, AC = AC$

(vi) Yes $\triangle ABC \cong \triangle ABD$ (By RHS)
 $\therefore \angle ABC = \angle ABD = 90^\circ$
 $AC = AD$



$AB = AD$

3. $\triangle AOB$ is not \cong to $\triangle EOD$

\therefore Only $\angle A = \angle E, \angle B = \angle D$
 (alternate angles)

But no sides are equal

4. (i) $\triangle ADB \cong \triangle BDC$ (alternate angles)

In $\triangle DAB$ and $\triangle BCD$

$AD = BC$ (given)

$\angle ADB = \angle DBC$ (alternate angles)

$BD = BD$

$\therefore \triangle DAB \cong \triangle BCD$ (By SAS)

5. $\angle A = \angle D = 180 - (65 + 30) = 85$

$AO = DO = 3\text{ cm}$

$\angle AOB = \angle DOC = 30^\circ$

$\therefore \triangle AOB \cong \triangle DOC$ (By ASA)

6. Yes, $\triangle LPQ \cong \triangle MPQ$ (By SSS)

$\therefore PL = PM$

$PQ = PQ, LQ = MQ$

7. In $\triangle PQR$ and $\triangle SQR$

$PR = SR$

$$\begin{array}{l} \overline{PR} = \overline{SR} \\ \overline{QR} = \overline{QR} \\ \overline{PQ} = \overline{SQ} \end{array} \quad \text{By SAS}$$

8. In $\triangle AOB$ and $\triangle DOC$

$$\begin{array}{l} \angle A = \angle D \quad \text{alternate angles} \\ \overline{AB} = \overline{CD} \quad \text{common} \\ \angle B = \angle C \quad \text{alternate angles} \end{array}$$

9. In $\triangle ABC$ and $\triangle DCB$

$$\begin{array}{l} \overline{AB} = \overline{DC} \quad (\text{given}) \\ \overline{AC} = \overline{BD} \quad (\text{given}) \\ \text{and } \overline{BC} = \overline{BC} \end{array}$$

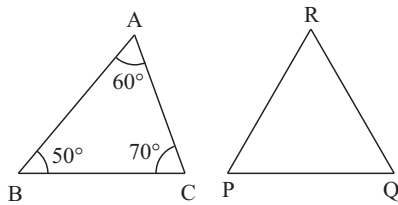
(By SSS)

In $\triangle ABD$ and $\triangle DCA$

$$\begin{array}{l} \overline{AD} = \overline{AD} \\ \overline{AB} = \overline{CD} \\ \overline{BD} = \overline{AC} \end{array}$$

(By SSS)

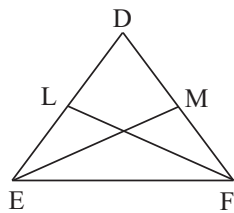
10.



$$\begin{array}{l} \angle C = 180 - (50 + 70) = 60 \\ \therefore \begin{array}{l} \overline{AB} = \overline{RP} \\ \overline{AC} = \overline{RQ} \\ \overline{BC} = \overline{PQ} \end{array} \end{array}$$

C.P.C. t C

11. In $\triangle DEM$ and $\triangle DFL$



$$\begin{array}{l} \overline{DE} = \overline{DF} \quad (\text{given}) \\ \overline{DD} = \overline{DD} \quad (\text{common}) \\ \overline{DM} = \overline{DL} \quad (\text{given}) \end{array}$$

$$\overline{DE} = \overline{DF} \quad (\text{By SAS})$$

12. $\triangle ADE$, $\triangle BCF$ (given)

But $\triangle ABC$ not $\triangle DEF$ because even in two equilateral triangles angles are equal but sides can be different.

13. In $\triangle ABN$ and $\triangle ACM$

$$\begin{array}{l} \overline{AB} = \overline{AC} \quad (\text{given}) \\ \angle A = \angle A \quad (\text{Common}) \\ \overline{AN} = \overline{AM} \quad (\text{given}) \\ \triangle ABN = \triangle ACM \quad (\text{by SAS}) \\ \overline{BN} = \overline{CM} \quad (\text{CPCTC}) \end{array}$$

14. (i) Yes $\triangle ABC \cong \triangle CDA$

(ii) SSS Congruence condition

(iii) Yes $\overline{AC} = \overline{AC}$ (common)

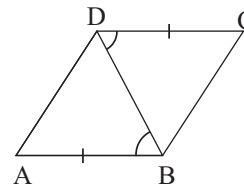
15. In $\triangle ABC$ and $\triangle DBC$

$$\begin{array}{l} \angle A = \angle D = 90^\circ \quad (\text{given}) \\ \overline{BC} = \overline{BC} \quad (\text{common}) \\ \overline{AC} = \overline{BD} \quad (\text{given}) \\ \triangle ABC = \triangle DBC \quad (\text{by RHS}) \end{array}$$

16. $\triangle ABD \cong \triangle ACD$ (by ASA)

$$\begin{array}{l} \therefore \angle CAD = \angle BAD \quad (\text{angle bisector}) \\ \overline{AD} = \overline{AD} \quad (\text{common}) \\ \angle CDA = \angle BDA \quad (\text{angle bisector}) \end{array}$$

17. Given : $ABCD$ is a parallelogram



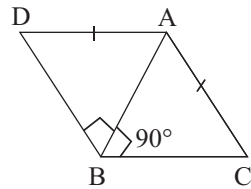
To prove : $\triangle ABD \cong \triangle CDB$

In $\triangle ABD$ and $\triangle CDB$

$$\begin{array}{l} \overline{AB} = \overline{CD} \\ (\text{opposite sides of parallelogram}) \\ \overline{AD} = \overline{BC} \\ \overline{BD} = \overline{BD} \quad (\text{common}) \\ \triangle ABD = \triangle CDB \quad \text{by SSS} \end{array}$$

diagonal of parallelogram bisect the parallelogram.

18. In $\triangle ABC$ and $\triangle ABD$



$\angle ABC = \angle ABD = 90^\circ$
 $AC = AD$ (given)

$AB = AB$ (common)
 $\angle ABC = \angle ABD$ (by RHS)

19. (i) They are of equal lengths.
 (ii) Their measure are equal.
 (iii) They have the same side length.
 (iv) Their dimensions are same.
 (v) They have the same radii.
20. (i) False (ii) True (iii) False (iv) False

13

Perimeter and Area

Exercise-13.1

1. (i) Perimeter of Rectangle

$$2(l + b)$$

$$2[5 + 4]$$

$$18 \text{ cm}$$

- (ii) Perimeter of rectangle

$$2(l + b)$$

$$2[6 + 2]$$

$$2(8)$$

$$16 \text{ cm}$$

- (iii) Perimeter of rectangle $2(7 + 1.5)$

$$2(8.5) = 17 \text{ cm}$$

2. (i) Perimeter of square $4 \times \text{side}$

$$10 \times 4 \text{ side}$$

$$\frac{10}{4} \text{ side}$$

$$2.5 \text{ cm} \text{ side of square}$$

- (ii) side of square $\frac{\text{Perimeter of square}}{4}$

$$\frac{16}{4} = 4 \text{ m}$$

- (iii) Side of square

$$\frac{\text{Perimeter of square}}{4}$$

$$\frac{40}{4} = 10 \text{ cm}$$

- (iv) Side of square

$$\frac{\text{Perimeter of square}}{4}$$

$$\frac{22}{4} = 5.5 \text{ cm}$$

3. (i) Perimeter of rectangle

$$2(l + b)$$

$$360 = 2[100 + b]$$

$$180 = 100 + b$$

$$80 \text{ cm} = b$$

- (ii) Perimeter of rectangle

$$2(l + b)$$

$$360 = 2[116 + b]$$

$$180 = 116 + b$$

$$64 \text{ cm} = b$$

- (iii) Perimeter of rectangle

$$2(l + b)$$

$$360 = 2[140 + b]$$

$$180 = 140 + b$$

$$40 \text{ cm} = b$$

- (iv) Perimeter of rectangle $2(l + b)$

$$360 = 2(102 + b)$$

$$180 = 102 + b$$

$$78 \text{ cm} = b$$

4. \therefore diagonal of square $\sqrt{2} \times \text{side}$

$$10\sqrt{2} = \sqrt{2} \times \text{side}$$

$$10 \text{ cm} = \text{side}$$

$$\text{Perimeter of square}$$

$$4 \times \text{side}$$

$$4 \times 10 = 40 \text{ cm}$$

5. (i) Diagonal of Rectangle

$$\sqrt{l^2 + b^2}$$

$$\sqrt{16^2 + 12^2}$$

$$\sqrt{256 + 144}$$

$$\sqrt{400}$$

$$\sqrt{20^2}$$

diagonal of rectangle = 20 cm

(ii) Similarly, diagonal of Rectangle

$$\sqrt{40^2 + 90^2}$$

$$\sqrt{1600 + 8100}$$

$$\sqrt{9700}$$

$$\sqrt{41^2}$$

Length of diagonal of rectangle = 41 cm

6. Perimeter of rectangular playground

$$2(l + b)$$

$$2[120 + 70]$$

$$2(190)$$

$$380 \text{ cm}$$

7. Perimeter of rectangle

$$2(l + b)$$

$$2(l + 3)$$

$$9 + l + 3$$

Length of rectangle = 6 cm

8. ∴ Perimeter of building = $2(l + b)$

$$320 + 2[125 + b]$$

$$160 + 125 + b$$

$$35 \text{ m} + b$$

breadth of building = 35 m

9. ∴ Perimeter of field = $2(l + b)$

$$932 + 2[l + 125]$$

$$466 + l + 125$$

$$466 + 125 + l$$

341 m lengths

length of field = 341 m

10. Perimeter of foot ball ground = $2(l + b)$

$$324 + 2[95 + b]$$

$$162 + 95 + b$$

$$67 \text{ m} + b$$

Length of football ground = 67 m

11. Iron wire required to fence the triangular park

Perimeter

$$60 + 40 + 20$$

$$120 \text{ m}$$

Cost of the wire to fence

$$(25 \times 120)$$

$$₹ 3000$$

12. Perimeter of triangle

$$a + b + c$$

$$64 + 15 + 24 = c$$

$$64 + 39 = c$$

$$25 = c$$

length of third side = 25 m

13. Distance travelled by a boy in going round a square = Perimeter of square

$$4 \times \text{side}$$

$$4 \times 20$$

distance covered by a boy = 80 m

14. Perimeter of equilateral triangle

$$3 \times \text{side}$$

$$3 \times 12.5 = 37.5 \text{ cm}$$

15. Perimeter of regular hexagon

$$6 \times \text{side}$$

$$6 \times 8.3$$

$$49.8 \text{ cm}$$

16. Perimeter of 8 sided polygon

$$8 \times \text{side}$$

$$53.6 \times 8 = \text{side}$$

$$6.7 \text{ cm} = \text{side}$$

17. Wire required = Perimeter of park

$$2(l + b)$$

$$2[30 + 20]$$

$$100 \text{ m}$$

$$\text{Cost of fencing} = 15 \times 100$$

$$₹ 1500$$

18. Perimeter of triangle = $a + b + c$

$$5 + 3 + 7$$

$$15 \text{ cm}$$

19. Perimeter of Rectangular park

$$2(l + b)$$

$$2[200 + 150]$$

$$700 \text{ m}$$

$$\text{cost of fencing} = 20 \times 700$$

$$₹ 14000$$