

$$\Rightarrow b = \frac{14 \times 18}{1} \quad (\text{by transposition})$$

$$\Rightarrow b = 16$$

Hence,  $b = 16$  is a solution.

$$\text{Check : } \text{L.H.S.} = \frac{7b}{8} - 15 = \frac{7 \times 16}{8} - 15 = 7 \times 2 - 15 = 14 - 15 = -1 = \text{R.H.S.}$$

18.  $\frac{x}{4} = \frac{x}{5} + 1$

We have,  $\frac{x}{4} = \frac{x}{5} + 1$

$$\Rightarrow \frac{x}{4} - \frac{x}{5} = 1 \quad (\text{by transposition})$$

$$\Rightarrow \frac{5x - 4x}{20} = 1$$

$$\Rightarrow \frac{x}{20} = 1$$

$$\Rightarrow x = 1 \times 20 \quad (\text{by transposition})$$

$$\Rightarrow x = 20$$

Hence,  $x = 20$  is a solution.

$$\text{Check : } \text{L.H.S.} = \frac{x}{4} = \frac{20}{4} = 5$$

$$\begin{aligned} \text{R.H.S.} &= \frac{x}{5} + 1 \\ &= \frac{20}{5} + 1 = 4 + 1 = 5 \end{aligned}$$

$$\therefore \text{L.H.S.} = \text{R.H.S.}$$

19.  $34 - 5(n - 1) = 4$

We have,  $34 - 5(n - 1) = 4$

$$\Rightarrow 34 - 5n + 5 = 4$$

$$\Rightarrow 39 - 5n = 4$$

$$\Rightarrow -5n = 4 - 39 \quad (\text{by transposition})$$

$$\Rightarrow -5n = -35$$

$$\Rightarrow n = \frac{-35}{(-5)} \quad (\text{by transposition})$$

$$\Rightarrow n = 7$$

Hence,  $n = 7$  is a solution.

$$\begin{aligned} \text{Check : } \text{L.H.S.} &= 34 - 5(n - 1) = 34 - 5(7 - 1) = 34 - 5 \times 6 \\ &= 34 - 30 = 4 = \text{R.H.S.} \end{aligned}$$

20.  $3P - 2(2P - 5) = 2(P + 3) - 8$

We have,  $3P - 2(2P - 5) = 2(P + 3) - 8$

$$\Rightarrow 3P - 4P + 10 = 2P + 6 - 8$$

$$\Rightarrow -P + 10 = 2P - 2$$

$$\begin{aligned} \Rightarrow & 10 = 2p - 2 + P && \text{(by transposition)} \\ \Rightarrow & 10 = 3p - 2 \\ \Rightarrow & 10 + 2 = 3P && \text{(by transposition)} \\ \Rightarrow & 12 = 3P \\ \Rightarrow & \frac{12}{3} = P && \text{(by transposition)} \\ \Rightarrow & 4 = P \quad \text{or} \quad P = 4 \end{aligned}$$

Hence,  $P = 4$  is a solution.

**Check :** L.H.S. =  $3P - 2(2P - 5) = 3 \times 4 - 2(2 \times 4 - 5)$   
 $= 12 - 2(8 - 5) = 12 - 2 \times 3 = 12 - 6 = 6$   
R.H.S. =  $2(P + 3) - 8 = 2(4 + 3) - 8 = 2 \times 7 - 8 = 14 - 8 = 6$   
 $\therefore$  L.H.S. = R.H.S.

### Exercise 8.5

1. Let the number be  $x$ . 35 added to  $x$  gives  $x + 35$ .

So, the following equation is obtained.

$$x + 35 = 217$$

or,  $x = 217 - 35 = 182$

Hence, the number is 182.

**Check :**  $182 + 35 = 217$

2. Let the number be  $x$ . twice the number is  $2x$ .

7 added to  $2x$  gives 59, so we obtain the following equation.

$$2x + 7 = 59$$

$$\Rightarrow 2x = 59 - 7$$

$$\Rightarrow 2x = 52$$

$$\Rightarrow x = \frac{52}{2}$$

$$\Rightarrow x = 26$$

Hence, the required number is 26.

**Check :**  $2 \times 26 + 7 = 52 + 7 = 59$

3. Let the number be  $x$ . 5 times the number =  $5x$ ,

Subtracting 3 from it, we get  $5x - 3$ . so, the following eqn is obtained

$$5x - 3 = 42$$

$$\Rightarrow 5x = 42 + 3 = 45$$

$$\Rightarrow \frac{5x}{5} = \frac{45}{5}$$

$$\Rightarrow x = 9$$

Hence, the required number is 9.

**Check :** Do yourself as above.

4. Let the number be  $x$ . Multiplication by  $\frac{5}{6}$  is  $\frac{5x}{6}$ ,

So we obtain the following equation.

$$\frac{5}{6}x = 60$$

$$\Rightarrow 5x = 60 \times 6$$



$$\Rightarrow x = \frac{12 \times 6}{1} = 12 \times 6$$

$$\Rightarrow x = 72$$

Hence, the required number is 72.

5. Let the number be  $x$ . Two-third of the number is  $\frac{2}{3}x$ .

one-third of the number is  $\frac{x}{3}$ . So, the equation is

$$\frac{2}{3}x = \frac{x}{3} + 3 \quad \Rightarrow \quad \frac{2x}{3} - \frac{x}{3} = 3$$

$$\Rightarrow \frac{2x - x}{3} = 3 \quad \Rightarrow \quad \frac{x}{3} = 3$$

$$\Rightarrow x = 3 \times 3 = 9$$

Hence, the required number is 9.

6. Let the number be  $x$ . Its three-fourth is  $\frac{3}{4}x$ .

So, the equation is  $x + \frac{3x}{4} = 91$

$$\Rightarrow \frac{4x + 3x}{4} = 91 \quad \Rightarrow \quad \frac{7x}{4} = 91$$

$$\Rightarrow 7x = 91 \times 4 \quad \Rightarrow \quad x = \frac{13 \times 91 \times 4}{7} = 13 \times 4$$

$$\Rightarrow x = 52$$

Hence, the required number is 52.

7. Let one of the numbers be  $x$ . Then, the second number will be  $(x + 1)$ .

$$\text{Then, } x + (x + 1) = 203 \quad \Rightarrow \quad 2x + 1 = 203$$

$$\Rightarrow 2x = 203 - 1 \quad \Rightarrow \quad 2x = 202$$

$$\Rightarrow x = \frac{202}{2} \quad \Rightarrow \quad x = 101$$

$\therefore$  one number = 101 and the second number =  $101 + 1 = 102$

8. Let one of the odd numbers be  $x$

Then, the next consecutive odd number =  $x + 2$

Sum of 2 consecutive odd number = 136

$$\therefore x + (x + 2) = 136$$

$$\text{or, } 2x + 2 = 136$$

$$\text{or, } 2x = (136 - 2) = 134$$

$$\text{or, } x = \frac{134}{2} = 67$$

Hence, one odd number = 67

and the second odd number =  $67 + 2 = 69$

9. Let one the even number be  $x$ .

Then, the next consecutive even number =  $x + 2$

Sum of 2 consecutive even number = 502

$$\therefore x + (x + 2) = 502$$

$$2x + 2 = 502$$

$$2x = 502 - 2 = 500$$

$$\Rightarrow x = 250$$

Hence, one even number = 250 and the second even number =  $250 + 2 = 252$

10. Let the 3 consecutive integers be  $x, x + 1, x + 2$

Sum of all the integers is  $x + (x + 1) + (x + 2)$ .

$$\therefore x + (x + 1) + (x + 2) = 24$$

$$\text{or, } 3x + 3 = 24$$

$$\text{or, } 3x = 24 - 3 = 21$$

$$\text{or, } x = \frac{21}{3} = 7 \quad \Rightarrow \quad x = 7$$

$\therefore$  First integer = 7 Second =  $7 + 1 = 8$  and the third integer =  $7 + 2 = 9$

11. Let the number of boys in the class be  $x$ .

$$\text{then, the number of girls} = \frac{5}{6} \text{ of the number of boys} = \frac{5}{6} \times x = \frac{5x}{6}$$

Total number of students = 44

Now, the number of girls + The number of boys = Total number of students

$$\Rightarrow \frac{5x}{6} + x = 44 \quad \Rightarrow \quad \frac{5x + 6x}{6} = 44$$

$$\Rightarrow \frac{11x}{6} = 44 \quad \Rightarrow \quad x = \frac{44 \times 6}{11}$$

$$\Rightarrow x = 24$$

Hence, the number of girls in the class =  $\frac{5}{6} \times 24 = 20$

12. Let the number be  $x$ . half of the number is  $\frac{x}{2}$ .

$$\therefore x + \frac{x}{2} = 45$$

$$\Rightarrow \frac{2x + x}{2} = 45$$

$$\Rightarrow \frac{3x}{2} = 45$$

$$\Rightarrow 3x = 45 \times 2$$

$$\Rightarrow x = \frac{45 \times 2}{3} = 15 \times 2 = 30$$

$\therefore$  The number = 30

13. Let Sahil's age be  $x$  years. Then his mother's age is  $5x$ .

Sum of their ages is  $(x + 5x)$  years.

$$\therefore x + 5x = 48 \quad \Rightarrow \quad 6x = 48 \quad \Rightarrow \quad x = \frac{48}{6} = 8$$

Hence, Sahil age = 8 years and his mother's age =  $5 \times 8 = 40$  years



14. Let Manayk's present age =  $x$  years

Then, after 15 years, Manayk's age =  $(x + 15)$  years

$$\therefore x + 15 = 4 \times (\text{Present age}) = 4x$$

$$\Rightarrow x + 15 = 4x$$

$$\Rightarrow 15 = 4x - x = 3x$$

$$\Rightarrow \frac{15}{3} = x \quad \Rightarrow \quad 5 = x$$

$$\Rightarrow x = 5$$

$\therefore$  Manayk's present age = 5 years

15. Let Isha's brother age be  $x$  years.

Then, Isha's age =  $(x - 5)$  years.

After 4 years, Isha's brother age will be  $(x + 4)$  years

and Isha's age will be =  $(x - 5) + 4 = (x - 1)$  years

$$\therefore \frac{(x + 5) + 4}{x + 4} = \frac{2}{3} \quad \Rightarrow \quad \frac{x - 1}{x + 4} = \frac{2}{3}$$

$$\Rightarrow 3(x - 1) = 2(x + 4)$$

$$\Rightarrow 3x - 3 = 2x + 8$$

$$\Rightarrow 3x - 2x = 8 + 3$$

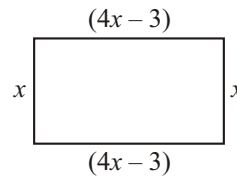
$$\Rightarrow x = 11$$

Hence, Isha's brother age =  $x = 11$  years and Isha's age =  $(x - 5) = (11 - 5) = 6$  years

16. Let breadth of rectangle =  $x$  m. Then length of rectangle =  $(4x - 3)$  m

Perimeter of rectangle = 94 m. Perimeter of rectangle =  $2(l + b)$

$$\begin{aligned} 94 &= 2(4x - 3 + x) \\ \Rightarrow \frac{94}{2} &= 5x - 3 \\ \Rightarrow 47 &= 5x - 3 \\ \Rightarrow 47 + 3 &= 5x \\ \Rightarrow 50 &= 5x \\ \Rightarrow \frac{50}{5} &= x \quad \Rightarrow \quad x = 10 \end{aligned}$$



$\therefore$  Breadth =  $x = 10$  m

Length =  $(4x - 3) = 4 \times 10 - 3 = 40 - 3 = 37$  m

17. Let Yuvraj scored =  $x$  runs and Gautam scored =  $2x$

Together, their run fell five short of a double century =  $(100 + 100 - 5) = 195$

$$\therefore x + 2x = 195$$

$$\Rightarrow 3x = 195$$

$$\Rightarrow x = \frac{195}{3}$$

$$\Rightarrow x = 65$$

$\therefore$  Yuvraj scored =  $x = 65$  runs

Gautam scored =  $2x = 2 \times 65 = 130$  runs

18. Let angle are  $\angle A = x^\circ$ ,  $\angle B = 2x^\circ$ ,  $\angle C = 3x^\circ$

We know that the sum of 3 angles of a triangle is  $180^\circ$ .



∴ The equation is.  $\angle A + \angle B + \angle C = 180^\circ$

i.e.,  $x + 2x + 3x = 180$

⇒  $6x = 180$

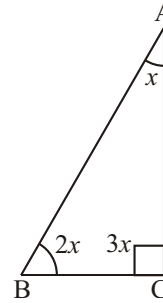
⇒  $x = \frac{180}{6}$

⇒  $x = 30^\circ$

$\angle A = x^\circ = 30^\circ$

$\angle B = 2x^\circ = 2 \times 30^\circ = 60^\circ$

$\angle C = 3x^\circ = 3 \times 30^\circ = 90^\circ$



19. Let the number of 2-rupee coins be  $x$

∴ the number of 1-rupee coins =  $3x$

value of one-rupee coin = ₹ 1

value of  $x$  2-rupee coin = ₹  $2x$

value of one 1-rupee coin = ₹ 1

value of  $3x$  1-rupee coin = ₹  $3x$

Total value of (2-rupee + 1-rupee) coins = ₹  $(2x + 3x)$

Hence, the equation is  $2x + 3x = ₹ 50$

⇒  $5x = 50$

⇒  $x = \frac{50}{5} = 10$  ⇒  $x = 10$

∴ number of 2 rupee coins =  $x = 10$

number of 1-rupee coins =  $3x = 3 \times 10 = 30$

20. Total number of notes = 30

Let the number of ₹ 100 notes be  $x$

∴ The number of ₹ 500 notes be =  $(30 - x)$

Total rupees in the purse is ₹ 5000.

∴ The equation is  $x \cdot 100 + (30 - x) \cdot 500 = 5000$

⇒  $100x + 15000 - 500x = 5000$

⇒  $15000 - 400x = 5000$  ⇒  $10000 = 400x$

⇒  $\frac{10000}{400} = x$  ⇒  $x = 25$

Hence, the number of ₹ 100 = 25

and the number of ₹ 500 =  $(30 - 25) = 5$

21. Let base angle be  $\angle B = x$  and  $\angle C = x$

Then, vertex angle  $\angle A = 3x$

The sum of 3 angles of a triangle is  $180^\circ$ .

i.e.,  $\angle A + \angle B + \angle C = 180^\circ$

⇒  $3x + x + x = 180^\circ$

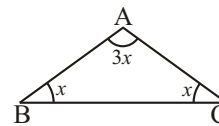
⇒  $5x = 180^\circ$

⇒  $x = \frac{180^\circ}{5} = 36^\circ$

∴ measure of  $\angle B = x^\circ = 36^\circ$

measure of  $\angle C = x^\circ = 36^\circ$

measure of  $\angle A = 3x^\circ = 3 \times 36 = 108^\circ$



22. Let Garima's age be  $x$  years  
 Then mother's age =  $3x$   
 Hence, the equation is,  $x + 3x = 72$   
 $\Rightarrow 4x = 72$   
 $\Rightarrow x = \frac{72}{4} = 18$   
 $\Rightarrow x = 18$   
 Hence, Garima's age = 18 years and mother age =  $3 \times 18 = 54$  years

### MCQ's

- 1.(d) 2. (c) 3. (c) 4. (b) 5. (a) b. (c)

### Formative Assessment-2

Tick (✓) the correct answer.

1. (c) 2. (b) 3. (c) 4. (b) 5. (a) 6. (a) 7. (b) 8. (b) 9. (b) 10. (c) 11. (a) 12. (b) 13. (c) 14. (a)  
 15. (b) 18. (a) 19. (d) 20. (b).

### Summative Assessment-1

Tick (✓) the correct answer.

1. (c) 2. (a) 3. (b) 4. (d) 5. (a) 6. (c) 7. (b) 8. (d)
9.  $\frac{11}{2} + 2\frac{1}{3} = \frac{11}{2} + \frac{7}{3} = \frac{33+14}{6} = \frac{47}{6} = 7\frac{5}{6}$
10.  $19.267 - 31.01 + 29.21 = (19.267 + 29.21) - 31.01 = 48.477 - 31.01 = 17.467$
11. Product of  $(-13) \times (-7) = (+)13 \times 7 = 91$  [ $\cdot - x - = +$ ]
12.  $\frac{-6}{13} = \frac{-6 \times 6}{13 \times 6} = \frac{-36}{78}$
13. Value of  $3^\circ - 4^\circ + 2^\circ = 5^\circ - 4^\circ = 1^\circ$
14.  $3x^2 + (-7x^2) + 5x^2 = (3x^2 + 5x^2) - 7x^2 = 8x^2 - 7x^2 = x^2$
15.  $12x - 11 = 5x + 3 \Rightarrow 12x - 5x = 11 + 3$   
 $7x = 14 \Rightarrow x = \frac{14}{7} = 2$   
 $x = 2$
16.  $8 \text{ hr} : 1 \text{ day} = \frac{8 \text{ hr}}{1 \text{ day}} = \frac{8 \text{ hr}}{24 \text{ hr}} = \frac{1}{3} = 1 : 3$
17. Male teachers = 51 Let total teachers =  $x$   
 Then female teachers = 25% of  $x = \frac{25}{100} \times x = \frac{x}{4}$   
 Now, female teachers + male teachers = Total teachers  
 $\Rightarrow \frac{x}{4} + 51 = x$

$$\Rightarrow 51 = x - \frac{x}{4} \quad (\text{by transposition})$$

$$\Rightarrow 51 = \frac{3x}{4}$$

$$\Rightarrow x = \frac{51 \times 4}{3} = 68$$

$\therefore$  Total teacher i.e., both male + female are 68.

$$\begin{aligned} 18. \quad & \left(5x^2 - \frac{x}{4} + \frac{2y}{3}\right) + \left(\frac{2x^2}{5} + \frac{x}{3} + \frac{2y}{3}\right) + \left(-x^2 + \frac{x}{2} - y\right) \\ &= \left(5x^2 + \frac{2x^2}{5} - x^2\right) + \left(\frac{x}{3} + \frac{x}{2} - \frac{x}{4}\right) + \left(\frac{2y}{3} + \frac{2y}{3} - \frac{y}{5}\right) \\ &= \left(\frac{4x^2}{1} + \frac{2}{5}x^2\right) + \left(\frac{4x + 6x - 3x}{12}\right) + \left(\frac{2y + 2y - 3y}{3}\right) \\ &= \left(\frac{20x^2 + 2x^2}{5}\right) + \left(\frac{10x - 3x}{12}\right) + \left(\frac{4y - 3y}{3}\right) \\ &= \frac{22}{5}x^2 + \frac{7}{12}x + \frac{y}{3} \end{aligned}$$

$$19. \quad 52 \text{ lakh} = 52,00000 = 50,00000 + 2,00000$$

$$20. \quad \text{Product of two numbers} = \frac{10}{3} \text{ one of them number} = \left(\frac{-15}{4}\right)$$

$$\therefore \text{The other number} = \left(\frac{10}{3}\right) \div \left(\frac{-15}{4}\right) = \frac{10}{3} \times \left(\frac{-4}{15}\right) = \frac{-8}{9}$$

Hence, the required number is  $\left(\frac{-8}{9}\right)$

$$21. \quad \text{Ascending order is } \left(\frac{-9}{10}\right) < \left(\frac{-11}{30}\right) < \left(\frac{-2}{15}\right) < 0$$

$$22. \quad 36 \div 3 + 4 \times 3 - 4 = \left(\frac{36}{3}\right) + 4 \times 3 - 4 = 12 + 12 - 4 = 24 - 4 = 20$$

$$23. \quad 11.5 \times 1.5 \times 1.5 = \frac{15 \times 15 \times 15}{10 \times 10 \times 10} = \frac{3375}{1000} = 3.375$$

$$\begin{aligned} 24. \quad & \left(\frac{7}{9} - \frac{5}{27}\right) \times \left(\frac{1}{3} - \frac{5}{18}\right) = \left(\frac{21-5}{27}\right) \times \left(\frac{6-5}{18}\right) \\ &= \frac{16}{27} \times \frac{1}{18} = \frac{8}{243} \end{aligned}$$

$$25. \quad \left(9\frac{7}{3}\right) \times 5\frac{4}{9} - \left(1\frac{2}{3} \div 8\frac{1}{3}\right) = \left(\frac{22}{7} \times \frac{49}{9}\right) - \left(\frac{5}{3} \div \frac{25}{3}\right)$$



$$\begin{aligned}
&= \left( \frac{22 \times 7}{3} \right) - \left( \frac{1}{3} \times \frac{3}{5} \right) = \frac{154}{3} - \frac{1}{5} \\
&= \frac{770 - 3}{15} \quad [\because \text{LCM of } (3, 5) = 15] \\
&= \frac{767}{15} \text{ or } 51 \frac{2}{15}
\end{aligned}$$

26. The cost of 2.5 kg of tomatoes = ₹ 20.625  
 $\therefore$  The cost of 1 kg of tomatoes = ₹ 20.625  $\div$  2.5  
 $= \frac{20.625}{2.5} = ₹ 8.25$

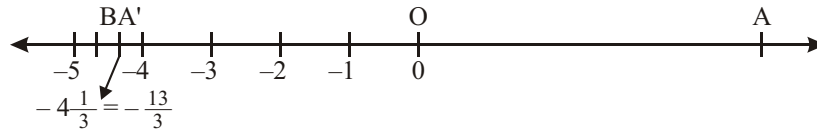
and the cost of 4 kg of tomatoes  $4 \times 8.25 = ₹ 33$

27. Given pattern  $\frac{15}{-6}, \frac{10}{-12}, \frac{5}{-18}, \frac{20}{-24}$ .

Therefore, 4 next numbers will be

$$\begin{aligned}
\therefore \frac{15 \times (-1)}{-6 \times (-1)}, \frac{10 \times (-1)}{-12 \times (-1)}, \frac{5 \times (-1)}{-18 \times (-1)}, \frac{20 \times (-1)}{-24 \times (-1)} &= \frac{-15}{6}, \frac{-10}{12}, \frac{-5}{18}, \frac{-20}{24} \\
\frac{15 \times 2}{-6 \times 2}, \frac{10 \times 2}{-12 \times 2}, \frac{5 \times 2}{-18 \times 2}, \frac{20 \times 2}{-24 \times 2} &= \frac{30}{-12}, \frac{20}{-24}, \frac{10}{-36}, \frac{40}{-48} \\
\frac{15 \times 3}{-6 \times 3}, \frac{10 \times 3}{-12 \times 3}, \frac{5 \times 3}{-18 \times 3}, \frac{20 \times 3}{-24 \times 3} &= \frac{45}{-18}, \frac{30}{-36}, \frac{15}{-54}, \frac{60}{-72} \\
\frac{15 \times 4}{-6 \times 4}, \frac{10 \times 4}{-12 \times 4}, \frac{5 \times 4}{-18 \times 4}, \frac{20 \times 4}{-24 \times 4} &= \frac{60}{-24}, \frac{40}{-48}, \frac{20}{-72}, \frac{80}{-96}
\end{aligned}$$

28.  $\frac{-13}{3} = -4 \frac{1}{3} = -4.33$



29.  $(4^{-1} - 5^{-1}) + (5^{-1} - 6^{-1}) = \left( \frac{1}{4} - \frac{1}{5} \right) + \left( \frac{1}{5} - \frac{1}{6} \right)$   
 $= \left( \frac{5-4}{20} \right) + \left( \frac{1-30}{5} \right) = \frac{1}{20} + \left( \frac{-29}{5} \right)$   
 $= \frac{1}{20} - \frac{29}{5} = \frac{1-116}{20} = \frac{-115}{20} = \frac{-23}{4}$

30.  $[5z - (x + 2y)] - [3x - (y - 2z)] = [5z - x - 2y] - [3x - y + 2z]$   
 $= 5z - x - 2y - 3x + y - 2z$   
 $= (5z - 2z) - x - 3x + (y - 2y)$   
 $= 3z - 4x - y$

31.  $2a(a^2 + b^2 - 2b^2(b + a)) + 2 = 2a^3 + 2ab^2 - 2b^3 - 2ab^2 + 2$   
 $= 2a^3 - 2b^3 + 2ab^2 - 2ab^2 + 2$

32. Let sister's age be  $x$  years then Saurab's age will be  $(x + 6)$  years

sum of their age is  $x + (x + 6)$

$\therefore$  The equation will be  $x + (x + 6) = 24$

or  $2x + 6 = 24$  or  $2x + 24 - 6 = 18$

or  $x = \frac{18}{2} = 9$

Hence, sister's Age = 9 years and Saurabh's Age =  $(9 + 6) = 15$  year

**Check :** Sum of their ages =  $9 + 15 = 24$  which is true.

33.  $8 - 7x = -20(x - 2) \Rightarrow 8 - 7x = -20x + 40$   
 $\Rightarrow 8 - 7 + 20x = 40 \Rightarrow 20x - 7x = 40 - 8$   
 $\Rightarrow 13x = 32 \Rightarrow x = \frac{32}{13}$

**Check :** LHS =  $8 - 7x = 8 - 7 \times \frac{32}{13} = \frac{104 - 224}{13} = \frac{-120}{13}$

RHS =  $-20(x - 2) = -20\left(\frac{32}{13} - 2\right)$   
 $= -20\left(\frac{32 - 26}{13}\right) = -20 \times \frac{6}{13} = \frac{-120}{13}$

34. The original price of the cell phone = ₹ 3500  
 reduced price of the cellphone = ₹ 3100  
 Decrease in price of the cell phone = ₹ 3500 - ₹ 3100 = ₹ 400

$\therefore$  Decrease % =  $\frac{\text{Decrease in price}}{\text{Original Price}} \times 100$

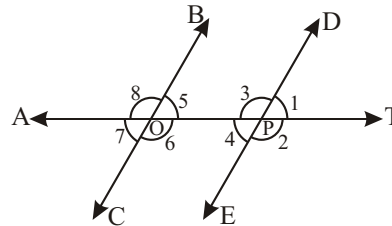
$= \frac{400}{3500} \times 100 = \frac{80}{7}$

$= 11.42\% \text{ or } 11\frac{3}{7}\%$

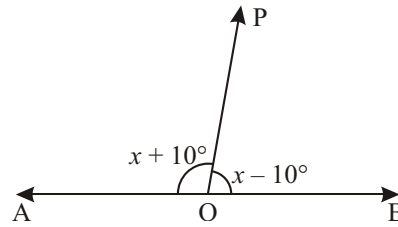
## 9. Understanding Shapes

### Exercise 9.1

- (a) Linear pairs will be :  
 $(\angle 5, \angle 8)$  and  $(\angle 1, \angle 3)$   
 $(\angle 8, \angle 7)$  and  $(\angle 3, \angle 4)$   
 $(\angle 7, \angle 6)$  and  $(\angle 4, \angle 2)$   
 $(\angle 6, \angle 5)$  and  $(\angle 2, \angle 1)$
- (b) Vertically opposite angles are :  
 $(\angle 1, \angle 4)$ , and  $(\angle 5, \angle 7)$   
 $(\angle 2, \angle 3)$  and  $(\angle 8, \angle 6)$
- Since  $AOB$  is a straight line.  
 $\therefore \angle AOB = 180^\circ$   
 $\Rightarrow x + 10^\circ + x - 10^\circ = 180^\circ$   
 $\Rightarrow 2x = 180^\circ$

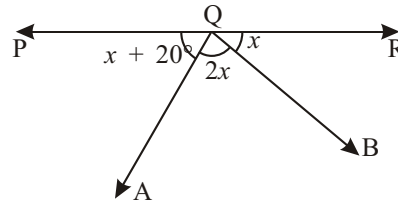


- $\Rightarrow x = \frac{180^\circ}{2} = 90^\circ$   
 (a)  $\angle AOP = x + 10^\circ = 90^\circ + 10^\circ = 100^\circ$   
 (b)  $\angle BOP = x - 10^\circ = 90 - 10 = 80^\circ$   
 (c) Since  $80^\circ < 90^\circ$   
 $\therefore \angle BOP$  is acute angle.  
 (d) Since  $100^\circ > 90^\circ$ .  
 $\therefore \angle AOP$  is obtuse angle.



3. Since  $PQR$  is a straight line.

$\therefore \angle PQR = 180^\circ$   
 $\Rightarrow x + 20^\circ + 2x + x = 180^\circ$   
 $\Rightarrow 4x + 20^\circ = 180^\circ$   
 $\Rightarrow 4x = 180^\circ - 20^\circ = 160^\circ$   
 $\Rightarrow x = \frac{160^\circ}{4} = 40^\circ$



- (a)  $\angle AQB = 2x = 2 \times 40^\circ = 80^\circ$   
 (b)  $\angle BQP = 2x + x + 20 = 3x + 20 = 3 \times 40^\circ + 20^\circ = 140^\circ$   
 (c)  $\angle AQR = 2x + x = 3x = 3 \times 40 = 120^\circ$

4. (a) Since  $AOB$  is a straight line

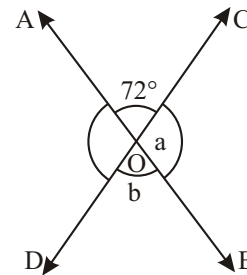
$\therefore \angle AOB = 180^\circ$   
 $\Rightarrow 72^\circ + \angle a = 180^\circ$   
 $\Rightarrow \angle a = 180 - 72 = 108^\circ$

- (b) Adjacent angles are  $\angle BOC, \angle COA, \angle AOD, \angle DOB$

- (c) Vertically opposite angles are  $(\angle AOC$  and  $\angle DOB)$   
 $(\angle AOD$  and  $\angle BOC)$ .

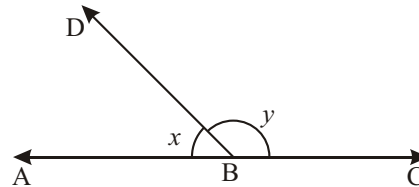
- (d)  $\angle DOB = \angle AOC = 72^\circ$   
 $\angle BOC = \angle AOD$   
 $a = \angle AOD$

(vertically opposite angles)  
 (vertically opposite angles)  
 $108^\circ = \angle AOD$



5. If  $x = 45^\circ, y = ?$

Since  $ABC$  is a straight line  
 $\therefore \angle ABC = 180^\circ$   
 $\Rightarrow x + y = 180^\circ$   
 $\Rightarrow 45^\circ + y = 180^\circ$   
 $\Rightarrow y = 180 - 45 = 135^\circ$



6. If  $y = 2x, x = ?, y = ?$

Since  $ABC$  is a straight line  
 $\therefore \angle ABC = 180^\circ$   
 $\Rightarrow x + y = 180^\circ$   
 $\Rightarrow x + 2x = 180^\circ$   
 $\Rightarrow 3x = 180^\circ$   
 $\Rightarrow x = \frac{180}{3} = 60^\circ$   
 $\Rightarrow y = 2 \times x = 2 \times 60 = 120^\circ$

[ $\because y = 2x$  given]

7.  $y = ?$ , IF  $x = \frac{y}{2}$  Since  $ABC$  is a straight line (from the figure)

$$\therefore \angle ABC = 180^\circ$$

$$\Rightarrow x + y = 180^\circ$$

$$\Rightarrow \frac{y}{2} + y = 180^\circ$$

$$\left[ \because x = \frac{y}{2} \text{ (given)} \right]$$

$$\Rightarrow \frac{3y}{2} = 180^\circ$$

$$\Rightarrow y = \frac{180 \times 2}{3} = 120^\circ$$

8. if  $y = 1\frac{1}{2}$  right angle,  $x = ?$

$$y = \frac{3}{2} \text{ right angle}$$

$$= \frac{3}{2} \times 90 = 3 \times 45 = 135^\circ$$

$$[\because 1 \text{ Right angle} = 90]$$

Since  $ABC$  is a straight line (from the fig.)

$$\therefore \angle ABC = 180^\circ \Rightarrow x + y = 180^\circ$$

$$x + 135^\circ = 180^\circ \Rightarrow x = 180 - 135 = 45^\circ$$

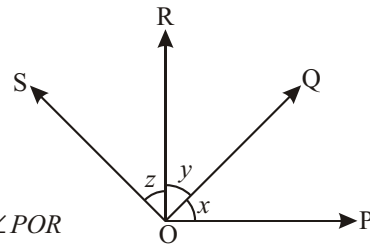
$$\Rightarrow x = 45^\circ$$

9. (a)  $\angle POR = \angle POQ + \angle QOR = x + y$

$$(b) \angle POR - \angle QOR = x + y - y = x$$

$$(c) \angle QOS - \angle SOR \\ = \angle QOR + \angle ROS - \angle SOR \\ = y + z - z = y$$

$$(d) \angle POS - \angle QOR - \angle POQ \\ = \angle POQ + \angle QOR + \angle ROS - \angle QOR - \angle POQ \\ = \angle ROS = z$$



10. (a)  $x + y = \angle POQ + \angle QOR = \angle POR$

$$(b) x + y + z = \angle POQ + \angle QOR + \angle ROS = \angle POS$$

$$(c) y + z = \angle QOR + \angle ROS = \angle QOS$$

$$(d) x + y + z - z = x + y = \angle POQ + \angle QOR = \angle POR$$

11. If  $x = 25^\circ$ ,  $y = 60^\circ$ ,  $\angle POR = ?$

$$\angle POR = x + y$$

$$= 25 + 60 = 85^\circ$$

(by figure)

12. If  $\angle SOQ = 100^\circ$ ,  $\angle QOR = 55^\circ$ ,  $\angle SOR = ?$

$$\angle SOR + \angle QOR = \angle SOQ$$

$$\angle SOR + 55^\circ = 100^\circ$$

$$\angle SOR = 100^\circ - 55^\circ = 45^\circ$$

13. If  $x = \frac{1}{3}$  right angle  $= \frac{1}{3} \times 90^\circ = 30^\circ$

$$y = \frac{2}{3} \text{ right angle} = \frac{2}{3} \times 90^\circ = 2 \times 30 = 60^\circ$$

$$z = \frac{1}{2} \text{ right angle} = \frac{1}{2} \times 90^\circ = 45^\circ$$

$$\begin{aligned}\angle POS &= x + y + z \\ &= 30 + 60 + 45 = 135^\circ\end{aligned}$$

14. (a) Given,  $x = y = 80$ ,  $z = 30^\circ$

$$\begin{aligned}\angle ABC &= x + y + z \\ &= 80 + 80 + 30 = 190^\circ\end{aligned}$$

Since  $\angle ABC = 190^\circ \neq 180^\circ$ .  
Hence,  $ABC$  is not a straight line.

- (b) Given,  $x = y = z = \frac{2}{3}$

$$\text{Right angle} \quad \frac{2}{3} \times 90 = 60^\circ$$

$$\begin{aligned}\angle ABC &= x + y + z \\ &= 60 + 60 + 60 = 180^\circ\end{aligned}$$

Since  $\angle ABC = 180^\circ$ .  
Hence,  $ABC$  is a straight line.

- (c) Given,  $x = \frac{2}{3}$

$$\text{Right angle} = \frac{2}{3} \times 90 = 60^\circ$$

$$\begin{aligned}y &= 1 \\ \text{Right angle} &= 90^\circ\end{aligned}$$

$$z = \frac{1}{2}$$

$$\text{Right angle} = \frac{1}{2} \times 90^\circ = 45^\circ$$

$$\begin{aligned}\angle ABC &= x + y + z \\ &= 60 + 90 + 45 = 195^\circ\end{aligned}$$

Since  $\angle ABC = 195^\circ \neq 180^\circ$ .  
Hence,  $ABC$  is not a straight line.

- (d)  $z = 1\frac{1}{2}$

$$\text{Right angle} = \frac{3}{2}$$

$$\text{Right angle} = \frac{3}{2} \times 90 = 135^\circ$$

$$\begin{aligned}\angle ABC &= x + y + z \\ &= 30 + 30 + 135^\circ = 195^\circ\end{aligned}$$

Since  $\angle ABC = 195^\circ \neq 180^\circ$ .  
Hence,  $ABC$  is not a straight line.

15. (a) if  $a = 110^\circ$ ,  $b = ?$

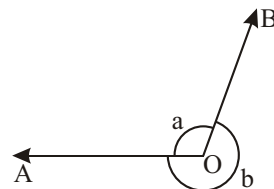
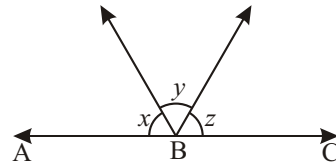
$$\angle AOB + \angle BOA = 360^\circ \quad (\text{Angles at a point})$$

$$a + b = 360$$

$$110 + b = 360$$

$$\Rightarrow b = 360^\circ - 110^\circ = 250^\circ$$

$$\Rightarrow b = 250^\circ$$



(b) If  $b = 200$ ,  $a = ?$

$$\begin{aligned} \angle AOB + \angle BOA &= 360^\circ && \text{(sum of all the angles at a point is } 360^\circ\text{)} \\ a + b &= 360^\circ \\ a + 200 &= 360 \\ \Rightarrow a &= 360 - 200 = 160^\circ \\ \Rightarrow a &= 160^\circ \end{aligned}$$

(c) If  $a = \frac{5}{3}$  right angle  $= \frac{5}{3} \times 90 = 5 \times 30 = 15^\circ$   $b = ?$

$$\begin{aligned} \therefore a + b &= 360^\circ && \text{(sum of all the angles at a point is } 360^\circ\text{)} \\ 150 + b &= 360^\circ \\ b &= 360 - 150 = 210^\circ \end{aligned}$$

16. (a)  $30^\circ$

$$\begin{aligned} a + b &= 90^\circ && \text{(Sum of two angles is } 90^\circ\text{)} \\ a + 30 &= 90 && \Rightarrow a = 90 - 30 \\ \Rightarrow a &= 60^\circ \end{aligned}$$

(b)  $80^\circ$

$$\begin{aligned} a + b &= 90^\circ \\ a &= 90^\circ - 80^\circ && \Rightarrow a = 10^\circ \end{aligned}$$

(c)  $15^\circ$

$$\begin{aligned} a + b &= 90^\circ \\ a + 15 &= 90^\circ && \Rightarrow a = 90 - 15 = 75^\circ \end{aligned}$$

(d)  $75^\circ$

$$\begin{aligned} a + b &= 90^\circ \\ a + 75^\circ &= 90^\circ && \Rightarrow a + 90^\circ - 75^\circ \\ \Rightarrow a &= 15^\circ \end{aligned}$$

(e)  $45^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ && \text{(Sum of two angles is } 90^\circ\text{)} \\ a + 45 &= 90^\circ && \Rightarrow a = 90^\circ - 45^\circ \\ \Rightarrow a &= 45^\circ \end{aligned}$$

(f)  $x^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ \\ a + x^\circ &= 90^\circ && \Rightarrow a = 90 - x^\circ \end{aligned}$$

(g)  $35^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ \\ a + 35^\circ &= 90^\circ && \Rightarrow a = 90 - 35^\circ \\ \Rightarrow a &= 55^\circ \end{aligned}$$

(h)  $10^\circ + y^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ \\ a + (10 + y) &= 90^\circ && \Rightarrow a = 90 - 10 - y && \Rightarrow a = 80y \end{aligned}$$

17. (a)  $\frac{1}{3}$  of  $90^\circ = \frac{1}{3} \times 90 = 30^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ && \Rightarrow a + 30 = 90 \\ a &= 90 - 30 && \Rightarrow a = 60^\circ \end{aligned}$$

(b)  $\frac{1}{4}$  of  $80^\circ = \frac{1}{4} \times 80 = 20^\circ$

$$\begin{aligned} \therefore a + b &= 90^\circ && \Rightarrow a + 20 = 90 \\ a &= 90 - 20 && \Rightarrow a = 70^\circ \end{aligned}$$

$$(c) \frac{1}{2} \text{ of } 60^\circ = \frac{1}{2} \times 60^\circ = 30^\circ$$

$$\therefore a + b = 90^\circ$$

$$\Rightarrow a + 30 = 90^\circ$$

$$a = 90 - 30 = 60^\circ \Rightarrow a = 60^\circ$$

$$(d) \frac{2}{5} \text{ of } 70 = \frac{2}{5} \times 70 = 28^\circ$$

$$\therefore a + b = 90^\circ$$

$$\Rightarrow a + 28 = 90$$

$$a = 90 - 28 \Rightarrow a = 62^\circ$$

18. (a)  $70^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + 70 = 180^\circ \Rightarrow a = 180^\circ - 70^\circ = 110^\circ$$

(b)  $80^\circ$

$$\therefore a + b = 180^\circ$$

$$a + 80 = 180 \Rightarrow a = 180^\circ - 80^\circ = 100^\circ$$

(c)  $195^\circ$

$$\therefore a + b = 180$$

$$a + 195^\circ = 180 \Rightarrow a = 180^\circ - 195^\circ = -15^\circ$$

(d)  $135^\circ$

$$\therefore a + b = 180^\circ$$

$$a + 135 = 180 \Rightarrow a = 180^\circ - 135^\circ = 45^\circ$$

(e)  $40^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + 40 = 180^\circ \Rightarrow a = 180^\circ - 40^\circ = 140^\circ$$

(f)  $121^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + 121 = 180 \Rightarrow a = 180 - 121 = 59^\circ$$

(g)  $x^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + x^\circ = 180 \Rightarrow a = 180^\circ - x^\circ$$

(h)  $20^\circ + y^\circ$

$$\therefore a + b = 180 \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + (20 + y) = 180 \Rightarrow a = 180 - 20 - y = 160 - y^\circ$$

19. (a)  $\frac{3}{4} \text{ of } 160^\circ = \frac{3}{4} \times 160^\circ = 120^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two angles is } 180^\circ)$$

$$a + 120^\circ = 180 \Rightarrow a = 180 - 120 = 60^\circ$$

(b)  $\frac{1}{2} \text{ of } 120^\circ = \frac{1}{2} \times 120 = 60^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + 60 = 180 \Rightarrow a = 180 - 60 = 120^\circ$$

(c)  $\frac{1}{3} \text{ of } 150 = \frac{1}{3} \times 150^\circ = 50^\circ$

$$\therefore a + b = 180^\circ \quad (\because \text{Sum of two supplement angles is } 180^\circ)$$

$$a + 50 = 180 \Rightarrow a = 180 - 50 = 130^\circ$$



$$(d) \frac{3}{5} \text{ of } 100 = \frac{3}{5} \times 100 = 3 \times 20 = 60^\circ$$

$$\begin{aligned} \therefore a + b &= 180^\circ && (\because \text{Sum of two supplement angles is } 180^\circ) \\ a + 60 &= 180 && \Rightarrow a = 180^\circ - 60^\circ = 120^\circ \end{aligned}$$

20. Let angles be  $7x^\circ$ ,  $8x^\circ$

$$\begin{aligned} \therefore \text{Angles are complementary} &&& (\because \text{Sum of two complementary angles is } 90^\circ) \\ \therefore 7x^\circ + 8x^\circ &= 90^\circ \\ 15x^\circ &= 90^\circ \\ x &= \frac{90}{15} = 6^\circ \end{aligned}$$

Thus, the angles are  $7x^\circ = 7 \times 6 = 42^\circ$  and  $8x^\circ = 8 \times 6 = 48^\circ$

21. Let angles be  $7x^\circ$ ,  $11x^\circ$  ( $\because$  Angles are supplementary)

$$\begin{aligned} \therefore 7x^\circ + 11x^\circ &= 180^\circ && (\because \text{Sum of two supplementary angles is } 180^\circ) \\ 18x^\circ &= 180 \\ x &= \frac{180^\circ}{18} = 10^\circ \end{aligned}$$

Thus, the angles are  $7x^\circ = 7 \times 10^\circ = 70^\circ$  and  $11x^\circ = 11 \times 10^\circ = 110^\circ$

22. (a) Let both the angles be  $x^\circ$ . ( $\because$  Angles are complement)

$$\begin{aligned} \therefore x^\circ + x^\circ &= 90^\circ && \Rightarrow 2x = 90 \\ x &= \frac{90^\circ}{2} = 45 && \Rightarrow x = 45^\circ \end{aligned}$$

(b) Let both the angles be  $x^\circ$  ( $\because$  Angles are supplementary)

$$\begin{aligned} x + x &= 180^\circ && \Rightarrow 2x = 180 \\ x &= \frac{180}{2} = 90^\circ && \Rightarrow x = 90^\circ \end{aligned}$$

23. (a) No, (b) No

$$(c) a + b = 180 \quad (\text{Sum of linear pair is } 180^\circ)$$

$$a + 90 = 180 \quad \Rightarrow a = 180 - 90 = 90^\circ$$

$\therefore$  other angle is  $90^\circ$

$$(d) a + b = 180$$

$$\text{obtuse angle} + b = 180^\circ$$

$$b = 180 - \text{obtuse angle} = \text{acute angle}$$

24. Let  $\angle a = 3x + 15^\circ$ ,  $\angle b = (2x + 5)^\circ$ ,  $x = ?$

$$\begin{aligned} \angle a + \angle b &= 180^\circ && (\because \text{Sum of two supplementary angles is } 180^\circ) \\ 3x + 15 + 2x + 5 &= 180^\circ \\ 5x + 20 &= 180^\circ \\ 5x &= 180 - 20 = 160^\circ \\ x &= \frac{160^\circ}{5} = 32^\circ \end{aligned}$$

25. Let  $\angle A = (2x - 7)^\circ$ ,  $\angle B = (x + 4)^\circ$

$$\begin{aligned} \therefore \angle A + \angle B &= 90^\circ && (\because \text{Sum of two complementary angles is } 90^\circ) \\ (2x - 7) + (x + 4) &= 90^\circ && \Rightarrow (2x + x) + (4 - 7) = 90 \\ 3x - 3 &= 90 && \Rightarrow 3x = 90 + 3 \\ \Rightarrow x &= \frac{93}{3} && \Rightarrow x = 31^\circ \end{aligned}$$





26. (a) Let  $\angle a = \angle b$ , then

$$\begin{aligned} a + b &= 180 \\ \Rightarrow a + a &= 180 \\ 2a &= 180 \\ \Rightarrow a &= \frac{180}{2} = 90 \\ \therefore a &= b = 90^\circ \end{aligned}$$

$\Rightarrow$  The given angles are vertical and supplementary.

(b) Given,  $a + b = 150^\circ$  ( $\because$  Sum of adjacent angles)  
 $a - b = 30$  ( $\because$  Difference of both angles is  $30^\circ$ )

Adding both equation,

$$2a = 150 + 30 = 180^\circ \quad \Rightarrow \quad a = \frac{180}{2} = 90^\circ$$

Putting  $a = 90^\circ$  in equation (1), we get

$$\begin{aligned} 90 + b &= 150^\circ \\ \Rightarrow b &= 150 - 90 \\ b &= 60^\circ \end{aligned}$$

$\therefore a = 90^\circ$  and  $b = 60^\circ$

(c) Let smaller angle  $= x^\circ$   
 then larger angle  $= 4x^\circ$

$$\because x + 4x = 90^\circ$$

$$5x = 90$$

$$x = 18^\circ$$

$\therefore$  smaller angle  $= 18^\circ$  and larger scale  $= 4 \times 18 = 72^\circ$

(d) Let the larger angle  $= x^\circ$

Then the smaller angle  $= (x - 30)^\circ$

$$\because x + (x - 30^\circ) = 90 \quad (\text{by complementary angles property})$$

$$2x = 90 + 30$$

$$x = \frac{120}{2} = 60$$

$$x = 60^\circ$$

$\therefore$  The larger angle  $= 60^\circ$  and The smaller angle  $= (60^\circ - 30^\circ) = 30^\circ$

(e) Let the smaller angle  $= x^\circ$

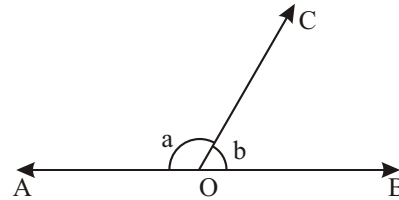
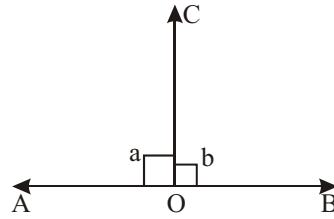
Then the larger angle  $= x + 60^\circ$

$$\because x + (x + 60^\circ) = 180^\circ \quad (\text{by supplementary angles property})$$

$$2x + 60 = 180^\circ$$

$$2x = 180 - 60 = 120^\circ$$

$$x = \frac{120}{2} = 60$$



(by complementary angles property)

$$x = \frac{18}{1} = 18^\circ$$

$$\Rightarrow x = 60$$

$$\therefore \text{smaller angle} = 60^\circ \text{ and larger angle} = 60 + 60 = 120^\circ$$

(f) Let the number angle =  $x^\circ$  Then the smaller angle =  $\frac{x^\circ}{2}$

$$\therefore x^\circ + \frac{x^\circ}{2} = 180^\circ \quad (\text{by supplementary angles property})$$

$$\frac{3x^\circ}{2} = 180$$

$$x^\circ = \frac{60}{3} \times 2 = 120^\circ$$

$$\therefore \text{The larger angle of } 120^\circ \text{ and the smaller angle} = \frac{120}{2} = 60^\circ$$

(g) Let the smaller angle =  $x^\circ$

Then the larger angle =  $(3x^\circ - 20^\circ)$

$$\therefore x^\circ + (3x^\circ - 20^\circ) = 180^\circ \quad (\text{by supplementary angles property})$$

$$4x^\circ - 20^\circ = 180^\circ$$

$$4x = 180 + 20 = 200^\circ$$

$$x = \frac{200^\circ}{4} = 50^\circ$$

$$\therefore \text{The smaller angle} = 50^\circ \text{ and the larger angle} = (3 \times 50^\circ - 20^\circ) = 130^\circ$$

27. Given  $\angle BAD = (5x^\circ - 30^\circ)$ ,  $\angle CAD = 2x^\circ$

$\therefore \angle CAB$  is a straight angle

$\therefore \angle CAD + \angle BAD = 180^\circ$

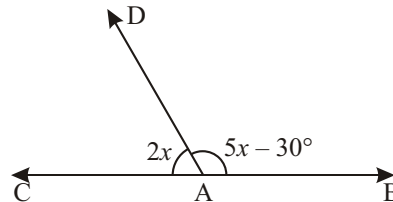
$$2x + (5x - 30) = 180$$

$$7x - 30 = 180$$

$$7x = 180 + 130 = 210$$

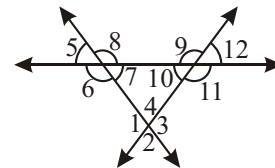
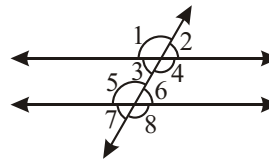
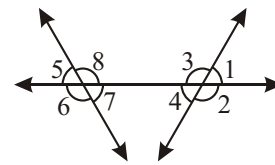
$$x = \frac{210^\circ}{7} = 30^\circ$$

$$\therefore x = 30^\circ$$



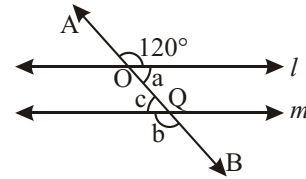
### Exercise 9.2

- $\angle 2$  and  $\angle 7$  = Alternate interior angles
  - $\angle 4$  and  $\angle 8$  = Corresponding angles
  - $\angle 1$  and  $\angle 8$  = Alternate exterior angles
  - $\angle 1$  and  $\angle 5$  = Corresponding angles
  - $\angle 4$  and  $\angle 7$  = None
- $(\angle 2, \angle 4)$  = None
  - $(\angle 1, \angle 8)$  = Alternate exterior angles
  - $(\angle 4, \angle 5)$  = Alternate interior angles
  - $(\angle 3, \angle 5)$  = None
- $(\angle 1, \angle 10)$  = Corresponding angles
  - $(\angle 6, \angle 2)$  = Alternate exterior
  - $(\angle 8, \angle 10)$  = Alternate interior
  - $(\angle 4, \angle 11)$  = Alternate interior
  - $(\angle 2, \angle 8)$  = Alternate interior
  - $(\angle 5, \angle 7)$  = None



4. (a)  $\because AOB$  is a straight line  
 $\therefore \angle AOB = 180^\circ$   
 $\Rightarrow 120 + a = 180^\circ$   
 $\Rightarrow a = 180^\circ - 120^\circ$   
 $\Rightarrow a = 60^\circ$   
 $\angle c = \angle a$   
 $\angle c = 60^\circ$

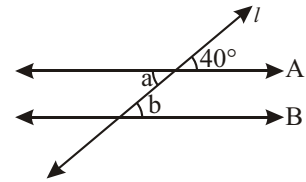
(Interior alternate angle)



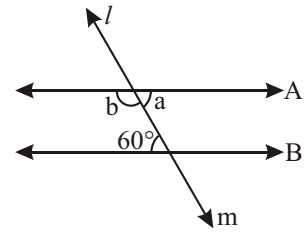
Now,  $AQB$  is a straight line

$\therefore \angle AQB = 180^\circ \Rightarrow c + b = 180^\circ$   
 $60 + b = 180$   
 $\Rightarrow b = 180 - 60 = 120^\circ$   
 $b = 120^\circ$

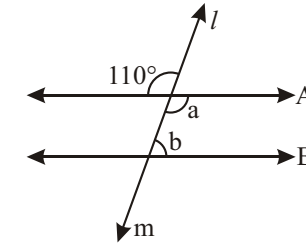
(b)  $\because \angle b = 40^\circ$   
 (corresponding angles)  
 $\Rightarrow b = 40^\circ$   
 $\because a = b$   
 (alternate angles)  
 $\Rightarrow a = 40^\circ$



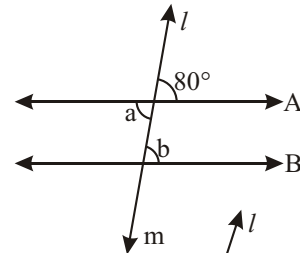
(c)  $\because a = 60$   
 (Alternate interior angles)  
 $b + 60^\circ = 180^\circ$   
 (Allied or conjoined angled)  
 $b = 180 - 60$   
 $\therefore b = 120^\circ$



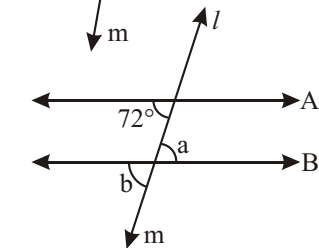
(d)  $\because a = 110^\circ$   
 (Vertically opposite angle)  
 $a + 10 = 180^\circ$   
 (Allied or conjoined angled)  
 $110^\circ + b = 180^\circ$   
 $b = 180 - 110^\circ$   
 $\therefore b = 70^\circ$



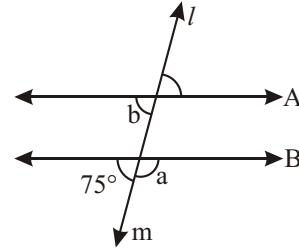
(e)  $\because b = 80^\circ$   
 (Corresponding angles)  
 $a = b$   
 (Alternative interior angles)  
 $\therefore a = 80^\circ$



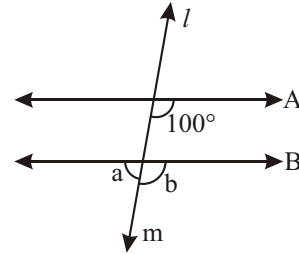
(f)  $\because a = 72^\circ$   
 (Alternate interior angles)  
 $b = a$   
 (Vertically opposite angles)  
 $\therefore b = 72^\circ$



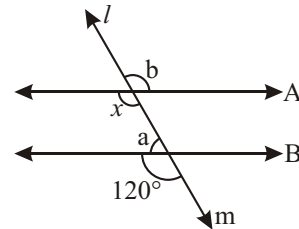
(g)  $\therefore b = 75^\circ$   
 (Corresponding angles)  
 $a + 75^\circ = 180^\circ$   
 (straight angles)  
 $a = 180^\circ - 75^\circ$   
 $\therefore a = 105^\circ$



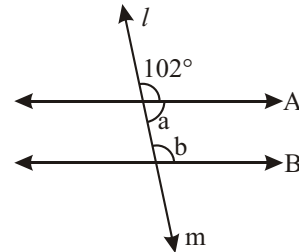
(h)  $\therefore b = 100^\circ$   
 (Corresponding angles)  
 $a + b = 180^\circ$   
 (straight line)  
 $a + 100 = 180^\circ$   
 $a = 180 - 100 = 80^\circ$   
 $\Rightarrow a = 80^\circ$



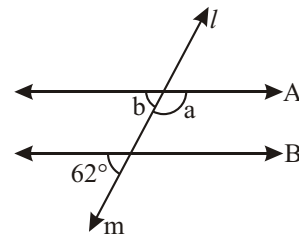
(i)  $\therefore lm$  is a straight line  
 $\therefore a + 120 = 180^\circ$   
 (by straight line property)  
 $= 180^\circ - 120^\circ$   
 $\Rightarrow a = 60^\circ$   
 $\therefore a + x = 180^\circ$   
 (Allied or conjoined angles)  
 $60 + x = 180^\circ$   
 $\Rightarrow x = 180 - 60 = 120^\circ$   
 Now,  $b = x$  (vertically opposite angle)  
 $\therefore b = 120^\circ$



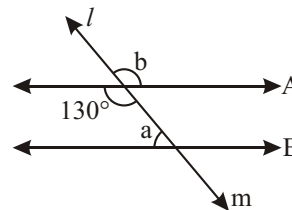
(j)  $\therefore b = 102^\circ$   
 (Corresponding angle)  
 $\therefore lm$  is a straight line.  
 $\therefore a + 102 = 180^\circ$   
 (by straight line property)  
 $a = 180^\circ - 102^\circ = 78^\circ$   
 $\therefore a = 78^\circ$



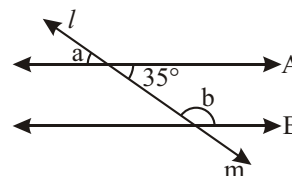
(k)  $\therefore b = 62^\circ$   
 (Corresponding angle)  
 $\therefore a + b = 180^\circ$   
 (straight line)  
 $a = 180^\circ - 62^\circ$   
 $\therefore a = 118^\circ$



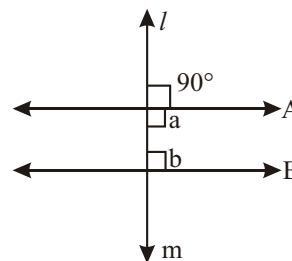
(l)  $\therefore b = 130^\circ$   
 (vertically opposite angle)  
 $a + 130^\circ = 180^\circ$   
 (Allied or conjoined angles)  
 $a = 180^\circ - 130^\circ$   
 $\Rightarrow a = 50^\circ$



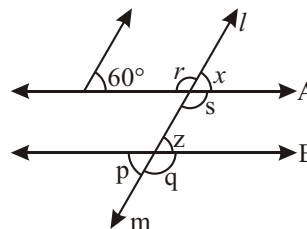
(m)  $\therefore a = 35$   
 (Vertically opposite angle)  
 $b + 35^\circ = 180^\circ$   
 (Allied or conjoined angles)  
 $b = 180^\circ - 35^\circ = 145^\circ$   
 $\therefore b = 145^\circ$



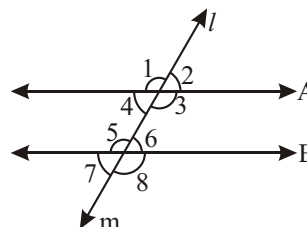
(n)  $b = 90^\circ$   
 (Corresponding angle)  
 $\therefore lm$  is a straight line  
 $\therefore a + 90^\circ = 180^\circ$   
 (straight line)  
 $a = 180 - 90 = 90^\circ$   
 $\Rightarrow a = 90^\circ$



5.  $\angle x = 60^\circ$  (corresponding angle)  
 $\angle z = \angle x$  (corresponding angle)  
 $\therefore \angle z = 60^\circ$   
 $\angle p = \angle z$  (vertically opposite angle)  
 $\therefore \angle p = 60^\circ$   
 $\angle r + 60 = 180^\circ$  (straight line)  
 $\angle r + 60 = 180^\circ$   
 $\Rightarrow \angle r = 180^\circ - 60^\circ = 120^\circ$   
 $\therefore \angle r = 120^\circ$   
 $\angle s = \angle r$  (vertically opposite angle)  
 $\therefore \angle s = 120^\circ$   
 $\angle q = \angle s$  (corresponding angle)  
 $= 120^\circ$   
 $x = 60^\circ \quad z = 60^\circ$   
 Hence,  $p = 60^\circ \quad q = 120^\circ \quad r = 120^\circ \quad s = 120^\circ$



6. given  $\angle 1 = 120^\circ, \angle 8 = 60^\circ$   
 $\angle 3 = \angle 1$  (vertically opposite angle)  
 $\therefore \angle 3 = 120^\circ$  [ $\because \angle 1 = 120^\circ$ ]  
 $\therefore \angle 1 + \angle 2 = 180^\circ$  [straight line]  
 $120^\circ + \angle 2 = 180^\circ$   
 $\Rightarrow \angle 2 = 180^\circ - 120^\circ = 60^\circ$   
 $\angle 2 = 60^\circ$   
 similarly,  $\angle 5 + \angle 6 = 180^\circ$   
 (straight line)  
 $\angle 5 + \angle 6 = 180^\circ$



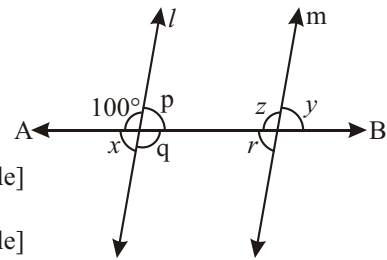
$$\begin{aligned} \Rightarrow \quad \angle 6 &= 180^\circ - 120^\circ = 60^\circ \\ \Rightarrow \quad \angle 6 &= 60^\circ \\ \angle 4 &= \angle 2 && \text{(vertically opposite angle)} \\ \therefore \quad \angle 4 &= 60^\circ \\ \because \quad \angle 5 + \angle 6 &= 180^\circ && \text{(straight line)} \\ \angle 5 + 60^\circ &= 180^\circ \\ \Rightarrow \quad \angle 5 &= 180 - 60^\circ = 120^\circ \\ \Rightarrow \quad \angle 5 &= 120^\circ \end{aligned}$$

Now, since given,

$$\begin{aligned} \angle 8 &= 60^\circ && \text{(Note)} \\ \therefore \quad \angle 7 + \angle 8 &= 180^\circ && \text{(straight line)} \\ \angle 7 + 60^\circ &= 180^\circ \\ \Rightarrow \quad \angle 7 &= 180^\circ - 60^\circ = 120^\circ \\ \Rightarrow \quad \angle 7 &= 120^\circ \end{aligned}$$

7.  $\because AB$  is a straight line

$$\begin{aligned} \therefore \quad 100 + P &= 180 && \text{[straight line]} \\ P &= 180^\circ - 100^\circ = 80^\circ \\ \Rightarrow \quad P &= 80^\circ \\ \therefore \quad q &= 100^\circ && \text{[vertically opp. angle]} \\ \Rightarrow \quad q &= 100^\circ \\ \therefore \quad x &= P && \text{[vertically opp. angle]} \\ \Rightarrow \quad x &= 80^\circ \\ \therefore \quad z &= 100^\circ && \text{[corresponding angle]} \\ \Rightarrow \quad z &= 100^\circ \\ \therefore \quad r &= z && \text{[vertically opp. angle]} \\ \Rightarrow \quad r &= 100^\circ \\ \therefore \quad z + y &= 180^\circ && \text{[straight line]} \\ 100 + y &= 180^\circ \\ y &= 180 - 100 = 80^\circ \\ \Rightarrow \quad y &= 80^\circ \end{aligned}$$



8.  $a = 30^\circ$

$$\begin{aligned} d &= a && \text{(vertically opp. angles)} \\ \Rightarrow \quad d &= 130^\circ && \text{(corresponding angles)} \\ c &= 150^\circ && \text{(Alternative angles)} \\ b &= c && \text{(coresponding angles)} \\ \Rightarrow \quad b &= 150^\circ \\ \text{Hence } a &= 130^\circ, \\ b &= 150^\circ, \\ c &= 150^\circ, \\ d &= 130^\circ \end{aligned}$$

